

# CS 61C: Great Ideas in Computer Architecture

*(Brief) Review Lecture*

**Instructor:** Alan Christopher

# Number Representation (1/5)

- Anything can be represented as a number!
  - Different *interpretations* of the same numeral
  - $n$  digits in base B can represent at most  $B^n$  things
- **Bases:** binary (2), decimal (10), hex (16)
- **Bit sizes:** nybble (4), byte (8), word (32)
- **Overflow:** result of operation can't be properly represented
  - Signed vs. Unsigned

# Number Representation (2/5)

- **Integers**

- Unsigned vs. Signed: sign & magnitude, 1's complement, 2's complement, biased
- Negation procedures vs. representation names
- Sign Extension vs. Zero Extension

- **Characters**

- Smallest unit of data (1 byte)
- ASCII standard maps characters to small numbers (e.g. '0' = 48, 'a' = 97)

# Number Representation (3/5)

- **Floating Point**

- Binary point encoded in scientific notation



$$(-1)^S \times (1 . \text{Mantissa}) \times 2^{(\text{Exponent}-127)}$$

- Exponent uses *biased notation* (bias of  $2^7-1 = 127$ )
- Can only save 23 bits past binary point in Mantissa (rest gets rounded off)
- Double precision uses 1 | 11 | 52 | split

# Number Representation (4/5)

- **Floating Point Special Cases:**

Exponent	Significand	Meaning
0	0	$\pm 0$
0	non-zero	$\pm$ Denorm Num
1-254	anything	$\pm$ Norm Num
255	0	$\pm \infty$
255	non-zero	NaN

Exponent  
of  $2^{-126}$



- What numbers can we can represent?
  - Watch out for exponent *overflow* and *underflow*
  - Watch out for *rounding* (and loss of associativity)

# Number Representation (5/5)

- **Powers of 2** (IEC Prefixes)
  - Convert  $2^{XY}$ :

Y (Digit)	Value
0	1
1	2
2	4
3	8
4	16
5	32
6	64
7	128
8	256
9	512

+

X (Digit)	Value
0	--
1	Kibi (Ki)
2	Mebi (Mi)
3	Gibi (Gi)
4	Tebi (Ti)
5	Pebi (Pi)
6	Exbi (Ei)
7	Zebi (Zi)
8	Yobi (Yi)

Things

# C Topics (1/4)

- **Pointer:** data type that holds an *address*
  - Visually can draw an arrow to another variable
  - NULL (0x00000000) means pointer to nothing
  - & (address of) and \* (dereference) operators
  - *Pointer arithmetic* moves correct number of bytes for data type (e.g. 1 for char, 4 for int)
  - Trying to access invalid, un-owned, or unaligned addresses causes errors
  - Use pointers to *pass by reference* (C functions naturally *pass by value*)

# C Topics (2/4)

- **Array:** sequential collection of objects of the same data type
  - Must be initialized with a size, cannot be changed

type array[SIZE]; or

Size implicit in initialization

type array[] = {d1, ..., dn};

- Bounds checking done manually (pass size)
- Access array:  $\text{array}[i] \leftrightarrow *(\text{array} + i)$



# C Topics (3/4)

- **Strings**

- Array of characters; null terminated (`'\0'` = `0`)
- Don't need to pass length because can look for null terminator (`strlen` does not count it)
- For  $n$  characters, need space for  $n+1$  bytes (`sizeof(char)=1`)

# C Topics (4/4)

- **Structs**

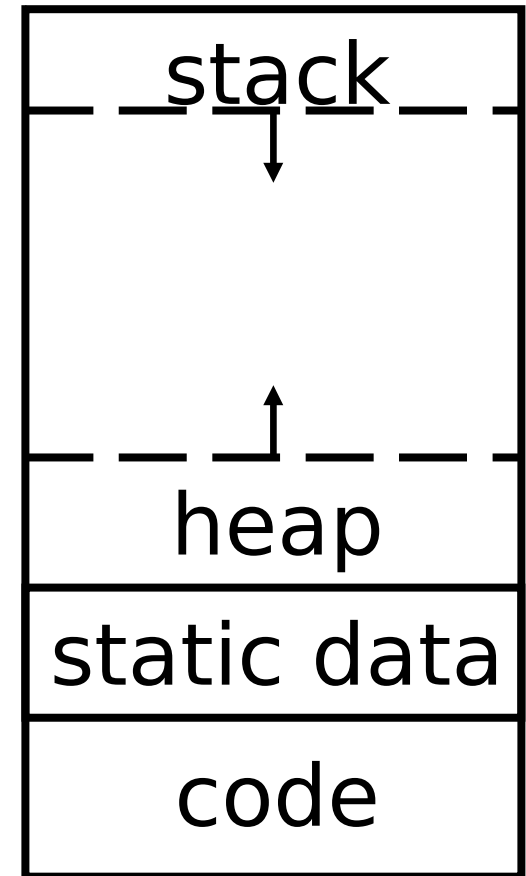
- Collection of variables (stored together in mem)
- Definition: `struct name { ... fields ... };`
- Variable type is `struct name` (2 words)
- Access field `(.)`
- With pointers: `x->field`  $\leftrightarrow$  `(*x).field`

- **Typedef**

- Rename an existing variable type
- `typedef nameorig namenew;`

# Memory Management (1/4)

- Program's *address space* contains 4 regions:
  - **Stack:** local variables, grows downward
  - **Heap:** space requested for pointers via `malloc()`; resizes dynamically, grows upward
  - **Static Data:** global and static variables, does not grow or shrink
  - **Code:** loaded when program starts, does not change size



# Memory Management (2/4)

- **Stack** grows in *frames* (1 per function)
  - Hold local variables (these disappear)
  - Bottom of Stack tracked by `$sp`
  - LIFO action (pop/push)
- Stack holds what we can't fit in registers
  - *Spilling* if more variables than registers
  - Large local variables (arrays, structs)
  - Old values we want to save (saved or volatile registers)

# Memory Management (3/4)

- **Heap** managed with `malloc` and `free`
  - Pointers to chunks of memory of requested size (in bytes); use `sizeof` operator
  - Check pointer; `NULL` if allocation failed
  - Don't lose original address (need for `free`)
  - With structs, free allocated fields before freeing struct itself
  - Avoid memory leaks!

# Memory Management (4/4)

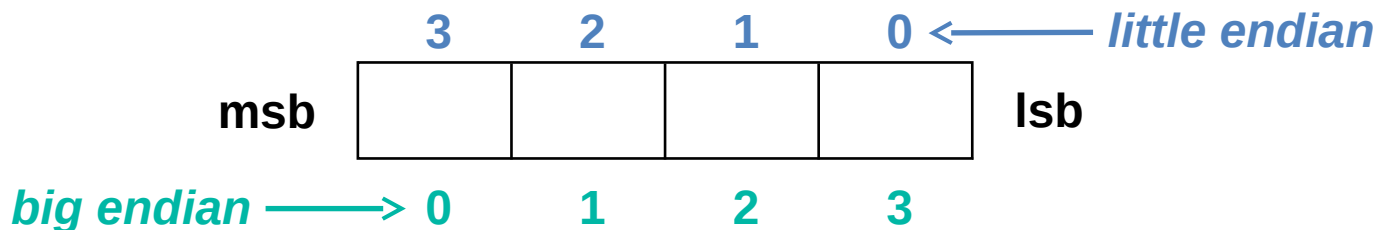
- Memory management
  - Want fast with minimal memory overhead
  - Avoid *fragmentation*
- Basic **allocation strategies**
  - *Best-fit*: Choose smallest block that fits request
  - *First-fit*: Choose first block that is large enough (always starts from beginning)
  - *Next-fit*: Like first-fit, but resume search from where we last left off

# MIPS Topics (1/6)

- MIPS is a **RISC** ISA
  - “Smaller is faster” and “Keep is simple”
  - Goal is to produce faster hardware
  - *Pseudo-instructions* help programmer, but not actually part of ISA (MAL vs. TAL)
- 32 32-bit registers are extremely fast
  - Only operands of instructions
  - Need lw/sw/lb/sb for memory access
- **Remember to use your Green Card!**
  - It has sooooooooooooo much info on it

# MIPS Topics (2/6)

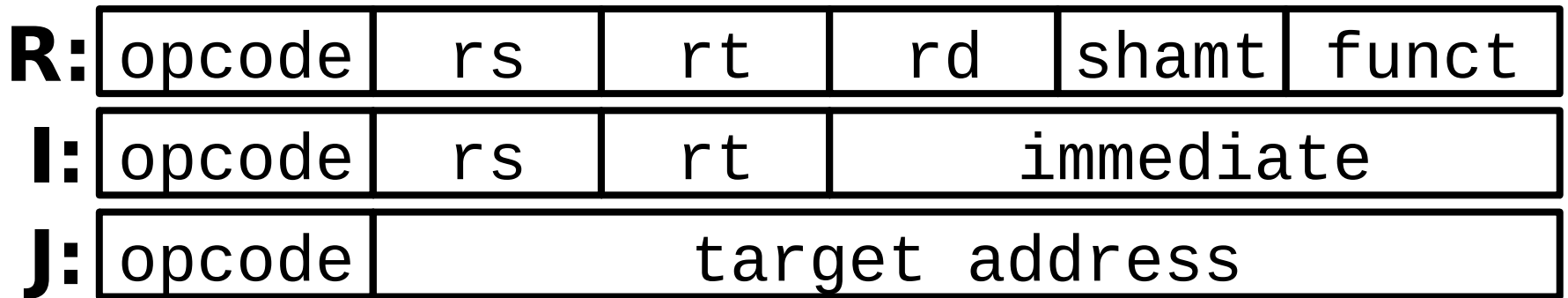
- **Stored Program Concept**
  - Instructions are data, too!
- **Memory is *byte-addressed***
  - Most data (including instructions) in words and *word-aligned*, so all word addresses are multiples of 4 (end in 0b00)
  - *Endianness*:





# MIPS Topics (3/6)

## • Instruction Formats



- Determine format/instr using opcode/funct (6)
- Register fields (5): rs/rt/rd
- Shift amount (5): shamt
- Constants/addresses: immediate (16), target address (26)

# MIPS Topics (4/6)

- **Relative addressing:**

signed

- Branch instructions relative to PC
- $PC = (PC+4) + (\text{immediate} * 4)$
- Can count *by instruction* for immediate
- Max forward:  
 $2^{15}$  instr =  $2^{17}$  bytes
- Max backwards:  
 $-2^{15} + 1$  instr =  $-2^{17} + 4$  bytes
- Do not need to be relocated

Relative to  
current  
instruction

# MIPS Topics (5/6)

- **Pseudo-absolute addressing:**
  - Jump instructions try to specify exact address
  - j/jal:  $PC = \{ (PC+4)[31..28], \text{target address}, 00 \}$
  - jr:  $PC = R[rs]$
  - Target address field is desired byte address/4
  - j/jal can specify  $2^{26}$  instr =  $2^{28}$  bytes
  - jr can specify  $2^{32}$  bytes =  $2^{30}$  instr
  - Always need to be relocated

# MIPS Topics (6/6)

- **MIPS functions**

- jal invokes function, jr \$ra returns
- \$a0-\$a3 for args, \$v0-\$v1 for return vals

- **Saved** registers: \$s0-\$s7, \$sp, \$ra

**Volatile** registers: \$t0-\$t9, \$v0-\$v1, \$a0-\$a3

- Caller saves volatile registers it is using before making a procedure call
- Caller saves saved registers it intends to use

# C.A.L.L.

- **Compiler** converts a single HLL file into a single assembly file `.c --> .s`
- **Assembler** removes pseudo-instructions, converts what it can to machine language, and creates symbol and relocation tables `.s --> .o`
  - Resolves addresses by making 2 passes (for internal forward references)
- **Linker** combines several object files and resolves absolute addresses `.o --> .out`
  - Enable separate compilation and use of libraries
- **Loader** loads executable into memory and begins execution

# Performance

- Performance measured in *latency* or *bandwidth*

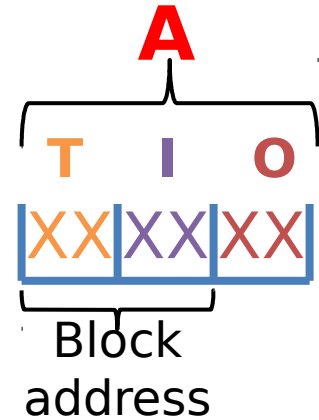
$$\text{Perf}_x = \frac{1}{\text{Program Execution Time}_x}$$

- Latency measurement:
  - CPU Time = Instructions  $\times$  CPI  $\times$  Clock Cycle Time
  - Affected by different components of the computer

# Caches (1/4)

- Why cache?
  - Take advantage of temporal/spatial locality to improve memory performance
- Cache Terminology
  - Block: unit of data transfer between \$ and Mem
  - Slot: place to hold block of data in \$
  - Set: set of slots an address can map into
  - Hit, Miss, Replacement
  - Hit Rate, Miss Rate, Hit:Miss Ratio

# Caches (2/4)



- Request is an address:
  - Search by Index, check Valid & Tag(s) for match
- Cache Parameters
  - Address space  $2^A$  bytes  $\leftrightarrow$  **A** address bits
  - Block size **K** bytes  $\leftrightarrow$  **O** =  $\log_2(\mathbf{K})$  offset bits
  - Associativity **N**  $\leftrightarrow$  N slots/set
  - Cache size **C** bytes  $\leftrightarrow$  **C/K/N** sets  
 $\leftrightarrow$  **I** =  $\log_2(\mathbf{C/K/N})$  index bits
  - $2^T$  blocks map to set  $\leftrightarrow$  **T** = **A** - **I** - **O**



# Caches (3/4)

- Policies
    - Write hit: write-back / write-through
    - Write miss: write allocate / no-write allocate
    - Replacement: random / LRU
  - Implementation
    - Valid bit
    - Dirty bit (if write-back)
    - Tag (identifier)
    - Block data ( $8 \cdot \mathbf{K}$  bits)
    - LRU management bits
- } per *slot*
- } per *set*

# Caches (4/4)

- 3 C's of Cache Misses
  - Compulsory, Capacity, Conflict
- Performance
  - $AMAT = HT + MR \times MP$
  - $AMAT = HT_1 + MR_1 \times (HT_2 + MR_2 \times MP_2)$
  - $CPI_{stall} = CPI_{base} + \frac{Accesses}{Instr} \times MR \times MP$
  - $CPI_{stall} = CPI_{base} + \frac{Accesses}{Instr} (MR_1 \times HT_2 + MR_1 \times MR_2 \times MP_2)$ 
    - Extra terms if L1\$ split among I\$ and D\$
  - $MR_{global} = \text{product of all } MR_i$

# Technology Break

# Other Questions?