1 Whatever Floats Your Boat

1.1 Overview

The IEEE 754 standard defines a binary representation method for floating point values that uses several encodings that you have already seen before. It’s a sign and magnitude representation, with the magnitude portion further split into exponent and significand. The exponent is in bias notation (with a bias of 127) and the significand is akin to unsigned, but used to store a fraction instead of an integer.

<table>
<thead>
<tr>
<th>s</th>
<th>eeeeeee</th>
<th>mmmmmmmmmmmmmmmmmmmmm</th>
</tr>
</thead>
<tbody>
<tr>
<td>Sign</td>
<td>Exponent</td>
<td>Significand (Mantissa)</td>
</tr>
<tr>
<td>1 bit</td>
<td>8 bits</td>
<td>23 bits</td>
</tr>
</tbody>
</table>

The above table shows the bit breakdown for the single precision (32-bit) representation defined by the standard. There is also a double precision encoding format that uses 64 bits. This behaves the same as the single precision but uses 11 bits for the exponent (and thus a bias of 1023) and 52 bits for the significand.

1.2 Conversion

Use this table to decode the value of the represented number:

<table>
<thead>
<tr>
<th>Single Precision</th>
<th>Double Precision</th>
<th>Encoded Value</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Exponent</td>
<td>Mantissa</td>
</tr>
<tr>
<td>0</td>
<td>0</td>
<td>nonzero</td>
</tr>
<tr>
<td>0</td>
<td>nonzero</td>
<td>anything</td>
</tr>
<tr>
<td>[1,254]</td>
<td>anything</td>
<td></td>
</tr>
<tr>
<td>255</td>
<td>nonzero</td>
<td></td>
</tr>
</tbody>
</table>

For normalized values, \( \text{float} = (-1)^{\text{sign}} \times 2^{\text{exponent} - \text{bias}} \times \text{mantissa}_2 \)

For denormalized values, \( \text{float} = (-1)^{\text{sign}} \times 2^{-\text{bias}+1} \times 0.\text{mantissa}_2 \)

1.3 Exercises

1. How many zeroes can be represented using a float?

2. What is the largest finite positive value that can be stored using a single precision float?

3. What is the smallest positive value that can be stored using a single precision float?

4. What is the smallest positive normalized value that can be stored using a single precision float?

5. Convert the following numbers from binary to decimal or from decimal to binary:
   
   0x0  
   8.25  
   0xF00  
   39.5625  
   0xFF94BEEF  
   -\infty
2 Compile, Assemble, Link, Load, and Go!

2.1 Overview

2.2 Exercises

1. What is the Stored Program concept and what does it enable us to do?

2. How many passes through the code does the Assembler have to make? Why?

3. What are the different parts of the object files output by the Assembler?

4. Which step in CALL resolves relative addressing? Absolute addressing?

5. What step in CALL may make use of the $at register?

6. What does RISC stand for? How is this related to pseudoinstructions?