# EECS 42 - Introduction to Electronics for Computer Science 

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## Problem Set \# 4 Due 2:30 PM Feb 19th, 240 Cory

Reading: Week \#4 Section 8.1 Schwarz and Oldham, Viewgraphs in HANDOUT_RC available on the web. Week \#5 Feb. $17^{\text {th }}$ is a UC Holiday, Feb $19^{\text {th }}$ Node Eq.
4.1 Sketch/Trend. Consider the circuit in Fig. P4.1. At $t=0$, the capacitor voltage $V_{C}=1 \mathrm{~V}$.
a) Find $V_{\text {Out }}$ as $t$ goes to infinity.
b) Evaluate the time constant RC in ns.
c) Evaluate the initial slope $\mathrm{dV} / \mathrm{dt}=(1 / \mathrm{C})\left(\mathrm{V}_{\text {FINAL }}-\mathrm{V}_{\text {INITIAL }}\right) / \mathrm{R}$
d) Draw axes for $V_{\text {out }}(t)$ vs $t$ where $t$ goes from 0 to 20 ns . Draw horizontal lines for $\mathrm{V}_{\text {Intitial }}$ and $\mathrm{V}_{\text {Initial }}$. Draw a slanted line with the slope found in part c ).


Fig. P4.1
e) Sketch $V_{\text {out }}(t)$ on the graph.
f) What one-by-one fractional changes (i.e. doubling or reduction by half) of the individual parameters $\mathrm{C}, \mathrm{V}_{\mathrm{FINAL}}-\mathrm{V}_{\text {INITIAL }}$ and R will cause the slope to double?
4.2 General Exponential Form. Use the circuit in Fig. P4.1 and values from Problem 4.1.
a) Assume that $\mathrm{V}_{\text {Out }}(\mathrm{t})$ is an known function and find an equation
for the current through the resistor in terms of $\mathrm{V}_{\text {out }}(\mathrm{t})$.
b) Assume that $\mathrm{V}_{\text {Out }}(\mathrm{t})$ is an known function and find an equation for the current through the capacitor in terms of the time derivative of $\mathrm{V}_{\text {OUT }}(\mathrm{t})$.
c) Equate $a$ ) and b) to obtain a differential equation for $V_{\text {OuT }}(t)$.
d) Substitute $\mathrm{V}_{\text {OUT }}(\mathrm{t})=\mathrm{A}+\mathrm{B} \mathrm{e}^{-(\mathrm{t} \tau)}$ and carry out the derivatives.
e) Group the equations into constant terms and terms times $\mathrm{e}^{-(\mathrm{t} \tau)}$.

Set these two groups of terms equal to zero to get two equations.
Which two of the three parameters A, B and $\tau$ do they determine?
$\mathrm{I}_{\mathrm{SS}}=1 \mathrm{~mA}, \mathrm{R}_{1}=1 \mathrm{k} \Omega, \mathrm{R}_{2}=2 \mathrm{k} \Omega, \mathrm{R}_{3}=3 \mathrm{k} \Omega$
f) Use the initial value to determine the third parameter.
4.3 Nonzero levels and resistors. A capacitor is precharged to -1.0 volts and connected at $\mathrm{t}=0$ to the circuit in Fig. P4.3. This makes $\mathrm{V}_{\text {Out }}(0)=-1 \mathrm{~V}$.
a) Find the voltage on the capacitor as t goes to infinity.
b) Determine theThevenin resistance seen by the capacitor by setting $\mathrm{I}_{\mathrm{SS}}=0$.


Fig. P4.3
These values are the same as in Problem 4.1
c) Find $\mathrm{I}_{\text {out }}$ and $\mathrm{dV}_{\text {OUT }} / \mathrm{dt}$ at $\mathrm{t}=0$.
d) Assume $\mathrm{V}_{\text {out }}(\mathrm{t})=\mathrm{A}+\mathrm{B} \mathrm{e}^{-(\mathrm{t} / \tau)}$ and use th initial condition and a ) and b ) to find $\mathrm{A}, \mathrm{B}$, and $\tau$.
4.4 Pulse shape. In the circuit in Fig. P4.4 the switch has been in the upward position connecting to $R_{U}$ for a long time. At $t=0$ the switch changes such that it is connected to $R_{D}$.
a) Find $V_{\text {out }}(t)$ as $t$ goes to infinity and the RC time constant.
b) Find $V_{\text {out }}(t)$ for $t>0$.
c) Determine the fraction of a time constant and the actual time that it takes for $\mathrm{V}_{\text {out }}(\mathrm{t})$ to reach 2.5 V .
d) Find $V_{\text {OUT }}(t=1.5 \mathrm{~ns})$.
e) Assume the switch returns to the upward position a $\mathrm{t}=1.5 \mathrm{~ns}$ and determine $V_{\text {out }}(t)$ for $t>1.5 \mathrm{~ns}$. (Be aware that there is a different time constant going upward.)

Brain teaser for fun for good students: determine the time at which $V_{\text {OuT }}(\mathrm{t})$ reach 4 V on its way back upward!

