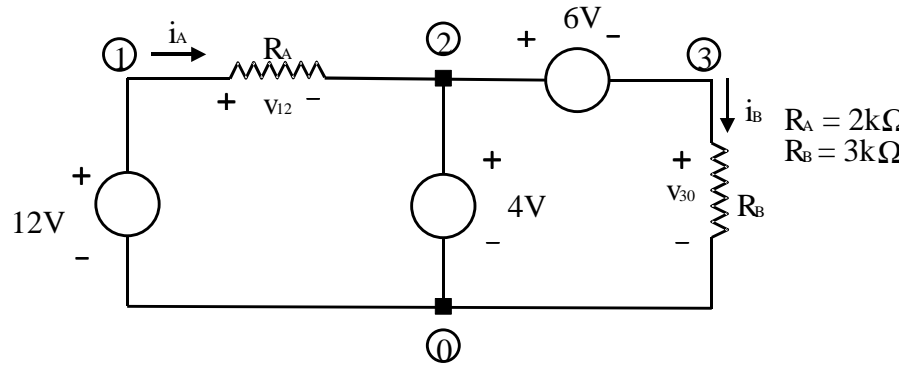


Problem Set 3  
(Due Mon July 8 at 12PM)

**Problem 1** Give the values of the DC current and voltages indicated in the following circuit. Warning: you must get the sign correct to get the right answer!



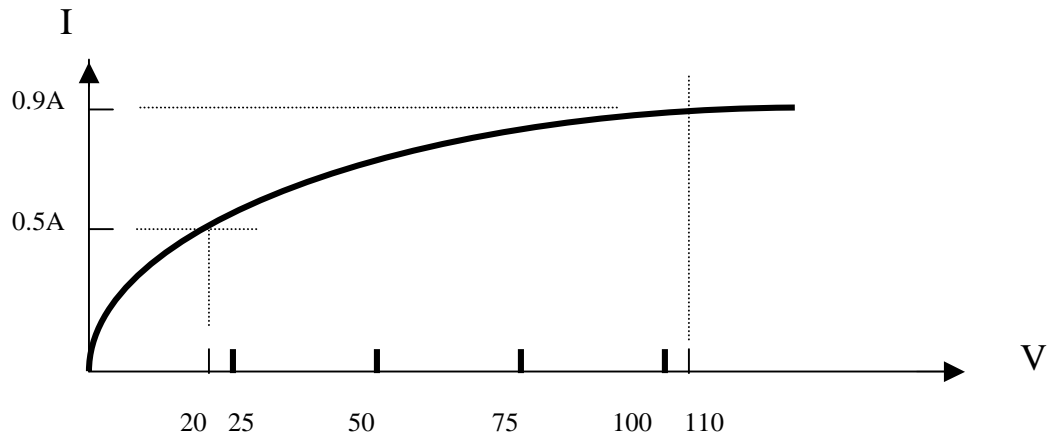
In this problem let Node 0 be the reference node (that's where you put the "common" or black probe of your voltmeter when you measure node voltages).

- (a)  $v_1 =$
- (b)  $v_2 =$
- (c)  $v_{12} =$
- (d)  $v_{30} =$
- (e)  $v_{32} =$
- (f)  $i_A =$
- (g)  $i_B =$
- (h) Find the power flowing into  $R_A$ .
- (i) Find the power supplied by the 12V source.
- (j) Find the power supplied by the 4V source.

**Problem 2** 1) The weird non-linear circuit element  $N_1$  of Figure 3.17 on page 106 of the text is placed across a power supply with voltage  $V_s$ . Thus  $V_{AB} = V_s$ . How much power does the power supply deliver to  $N_1$  if  $V_s$  is:

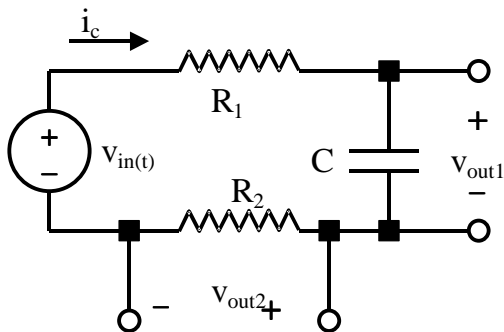
- a) 5V (Note: just read the graph as accurately as you can, the answer is of course approximate.),
- b) 0V. (Can you explain this answer - after all the current is not zero is it?)

**Problem 3** A light bulb has the I-V characteristics shown below. It is normally used at 110V .



- What should be the nominal wattage rating of this bulb (i.e. the power dissipated when it is in a 110V circuit) (Round off to the nearest multiple of 5W in all parts of this problem).
- How much power does it dissipate when it has only 20V across it?
- If you had only the data points for current at  $V = 0$  and  $V=110$ , you might assume this was a resistor. What would you estimate the resistance value to be?
- Calculate the current and the power for a resistor that has the resistance of part c, at a voltage of 20V.
- So does Ohm's law work for a nonlinear device like the light bulb? (answer is NO) Why not?

**Problem 4** The circuit below has a time varying voltage source  $v_{in}$  which is a simple 3V step function at  $t = t_1$  (i.e.  $v_{in} = 0$  for all  $t < t_1$  and  $v_{in} = 3V$  for all  $t > t_1$ ). In this problem  $t_1 = 50\text{msec}$ .



$$R_1 = 5\text{k}\Omega; R_2 = 5\text{k}\Omega; C = 1\mu\text{F}$$

- How could you construct the source  $V_{in}(t)$  from a 3V battery and a switch (draw the circuit)?
  - What is the initial value of  $V_{out1}$  (that is the value of the capacitor voltage for  $t < t_1$ )?
  - Find  $v_{out1}(t)$  at  $t = t_{1+}$  (that is just at the very start of the transient).
  - Given the answer to part (c) can you say how much voltage is dropped across each of the resistors at this same instant  $t = t_{1+}$ ? (Hint: Each resistor drops half the difference of  $V_{in}$  less  $V_{out1}$ ).
  - What is the circuit time constant?
- Plot:
- $V_{out1}(t)$
  - $i_c(t)$ . (Hint: Combine the resistors together to simplify the circuit and make use of your knowledge of capacitors to be able to find  $i_c(t)$  at  $t = t_1$  and  $t \gg RC$ )
  - $V_{out2}(t)$  Same axes as in (c) (Hint: apply ohm's law on resistor  $R_2$  only.)
- (i) Write equations for the capacitor voltages  $V_{out1}(t)$ ,  $V_{out2}(t)$  and current  $i_c(t)$ .

### Problem 5

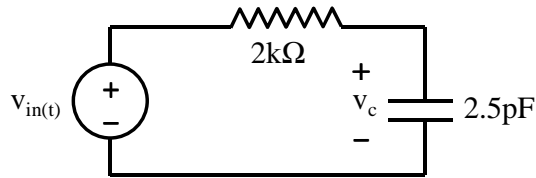


Figure 5.1

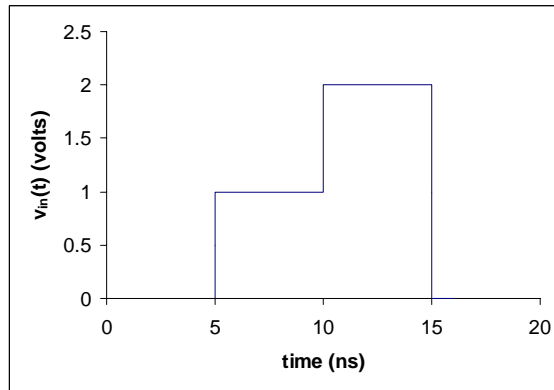


Figure 5.2

The circuit in Figure 5.1 has a  $v_{in}$  waveform shown in Figure 5.2. Assume that the capacitor is uncharged at  $t = 0$ .

(a) Sketch  $v_c(t)$ . That means find initial and asymptotic values, sketch, and write the equation for  $V_c(t)$ . Hint: There are three transient problems here! First solve the problem for the first voltage step ignoring the second step, and so forth. Calculate  $X$ , the voltage at  $t = 10\text{ns}$  based on the first transient solution. This is of course the initial capacitor voltage for the second part of the problem (a capacitor having an initial voltage of  $X$ , with an input voltage of  $2\text{V}$  applied at  $t = 10\text{ns}$ ). Then there is a third problem in which the input drops to zero, so you must again calculate the exact voltage at  $t=15\text{ns}$  (from the solution to the second part) which is the initial condition for the third part.

(b) Write the equations for the curves in the different time regions:  $t < 5\text{ns}$ ,  $5\text{ns} < t < 10\text{ns}$ ,  $10\text{ns} < t < 15\text{ns}$ , and  $t > 15\text{ns}$