## PROBLEM SET \#3

Issued: Tuesday, Feb.8, 2011
Due: Tuesday, Feb.15, 2011, 5:00 p.m. in the EE 140 homework box in 240 Cory

1. Multi-stage analysis

Fig. PS3.1 shows a three-stage amplifier in which the stages are directly coupled. The amplifier, however, utilizes bypass capacitors, and, as such, its frequency response falls off at low frequencies. For our purpose here, we shall assume that the capacitors are large enough to act as perfect short circuits at all signal frequencies of interest.
a. Find the dc bias current in each of the three transistors. Also find the dc voltage at the output. Assume $\left|V_{B E}\right|=0.7 \mathrm{~V}, \beta=100$, and neglect the Early effect;
b. Find he input and output resistance;
c. Use the current-gain method to evaluate the voltage gain vo/vi;
d. Find the high frequency pole formed at the interface between the first and the second stages. Assume that $C_{\mu 2}=2 \mathrm{pF}$ and $C_{\pi 2}=10 \mathrm{pF}$.


Fig. PS3.1
2. Cascode stage analysis

The ac schematics of a common-source stage and a cascode stage are shown in Fig. PS3.2 with $\mathrm{R}_{\mathrm{S}}=10 \mathrm{k} \Omega$ and $\mathrm{R}_{\mathrm{L}}=20 \mathrm{k} \Omega$. Using the transistor and operating point data below,
a. Calculate the low-frequency, small signal voltage gain $v_{o} / v_{i}$ for each circuit.
b. Calculate the -3 dB frequencies of the two circuits.

Data: $\mathrm{I}_{\mathrm{D}}=0.5 \mathrm{~mA}, \mathrm{~W}=100 \mu \mathrm{~m}, \mathrm{~L}_{\mathrm{drwn}}=2 \mu \mathrm{~m}, \mathrm{~L}_{\mathrm{d}}=0.2 \mu \mathrm{~m}, \mathrm{X}_{\mathrm{d}}=0, \lambda=0, \mathrm{k}_{\mathrm{n}}=60$ $\mu \mathrm{A} / \mathrm{V}^{2}, \gamma=0, \mathrm{C}_{\mathrm{sb}}=\mathrm{C}_{\mathrm{db}}=0, \mathrm{C}_{\mathrm{ox}}=0.7 \mathrm{fF} / \mu \mathrm{m}^{2}$, and $\mathrm{C}_{\mathrm{gd}}=14 \mathrm{fF}$.


Fig. PS3.2
3. Single-stage design

Use the following parameters:

$$
\begin{array}{llll}
\mu_{\mathrm{n}} \mathrm{C}_{\mathrm{ox}}=100 \mu \mathrm{~A} / \mathrm{V}^{2} & \mu_{\mathrm{p}} \mathrm{C}_{\mathrm{ox}}=50 \mu \mathrm{~A} / \mathrm{V}^{2} & \mathrm{~V}_{\mathrm{T}}=0.5 \mathrm{~V} & \mathrm{~V}_{\mathrm{DD}}=3 \mathrm{~V} \\
\mathrm{~L}=1 \mu \mathrm{~m} & \mathrm{~W}_{\mathrm{p}}=2 \mathrm{~W}_{\mathrm{n}} & \left(\mathrm{~V}_{\mathrm{GS}}-\mathrm{V}_{\mathrm{T}}\right)_{\min }=100 \mathrm{mV} \text { for strong inversion } \\
\mathrm{C}_{\mathrm{L}}=4 \mathrm{pF} & \mathrm{C}_{\mathrm{gs}}=1 \mathrm{pF} & \mathrm{C}_{\mathrm{gd}}=0 \mathrm{pF} & \mathrm{C}_{\mathrm{db}}=1 \mathrm{pF}
\end{array}
$$

a. What is the maximum midband voltage gain of a resistively loaded common source amplifier operating in strong inversion? Use $\lambda_{n, p}=0$.
b. How about with an active (PMOS) load? $\lambda_{\mathrm{n}, \mathrm{p}}=0.1 \mathrm{~V}^{-1}$.
c. If $I_{D}=1 \mathrm{~mA}$, how would you size each of the devices?
d. With $\mathrm{I}_{\mathrm{D}}=1 \mathrm{~mA}$, what is the dominant pole frequency of each of these amplifiers?
4. PNP-input active load stage analysis

An amplifier is shown in Fig. PS3.4. $\mathrm{I}_{\mathrm{B}}$ is adjusted such that $\mathrm{V}_{\mathrm{O}}=0 \mathrm{~V}$ dc. $\mathrm{V}_{\text {SUpply }}=10$ V. Calculate the low-frequency, small signal transresistance $v_{o} / v_{i}$, and estimate the -3 dB frequency.
npn:
$\beta=100, \mathrm{f}_{\mathrm{T}}=500 \mathrm{MHz}$ at $\mathrm{I}_{\mathrm{C}}=1 \mathrm{~mA}, \mathrm{C}_{\mu 0}=0.7 \mathrm{pF}, \mathrm{C}_{\mathrm{je}}=3 \mathrm{pF}$ (at the bias point), $\mathrm{C}_{\mathrm{c} 50}=2$ $\mathrm{pF}, \mathrm{r}_{\mathrm{b}}=0$, and $\mathrm{V}_{\mathrm{A}}=120 \mathrm{~V}$. Assume $\mathrm{n}=0.5$ and $\psi_{0}=0.55 \mathrm{~V}$ for all junctions.
pnp:
$\beta=50, \mathrm{f}_{\mathrm{T}}=4 \mathrm{MHz}$ at $\mathrm{I}_{\mathrm{C}}=-0.5 \mathrm{~mA}, \mathrm{C}_{\mu 0}=1.0 \mathrm{pF}, \mathrm{C}_{\mathrm{je}}=3 \mathrm{pF}$ (at the bias point), $\mathrm{C}_{\mathrm{bs} 0}=2$ $\mathrm{pF}, \mathrm{r}_{\mathrm{b}}=0$, and $\mathrm{V}_{\mathrm{A}}=50 \mathrm{~V}$. Assume $\mathrm{n}=0.5$ and $\psi_{0}=0.55 \mathrm{~V}$ for all junctions.


Fig. PS3.4

