

# EECS 126: Probability and Random Processes

## Discussion 14

Note: Please work on the problems before the discussion session.

**Problem 4.** Chernoff bound for a Poisson random variable. Let  $X$  be a Poisson random variable with parameter  $\lambda$ .

(a) Show that for every  $s \geq 0$ , we have

$$\mathbf{P}(X \geq k) \leq e^{\lambda(e^s - 1)} e^{-sk}.$$

(b) Assuming that  $k > \lambda$ , show that

$$\mathbf{P}(X \geq k) \leq \frac{e^{-\lambda} (e\lambda)^k}{k^k}.$$

**Problem 7.** Suppose that a sequence  $X_n$  of random variables satisfies

$$\lim_{n \rightarrow \infty} \mathbf{E}[|X_n - c|^\alpha] = 0,$$

where  $\alpha$  is a positive number. Show that the sequence  $X_n$  converges to  $c$  in probability.

**Problem 16.** The adult population of Nowhereville consists of 300 males and 196 females. Each male (respectively, female) has a probability of 0.4 (respectively, 0.5) of casting a vote in the local elections, independently of everyone else. Find a good numerical approximation for the probability that more males than females cast a vote.