

EE105 Midterm-2 : 4/9 (Next Tuesday) in class  
same format as Midterm-1

Sample midterms posted

practice. Solution posted Wed.

4/4 class. Q&A

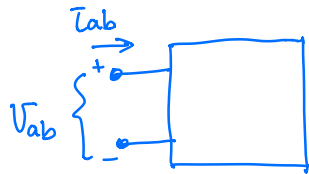
Topics in midterm, up to today's lectures

Emphasis on materials after Midterm 1

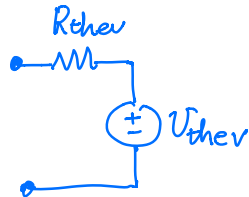
Single Stage Amplifier

↓  
Transistor

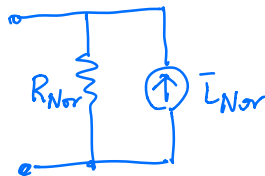
From 16A/B: Circuit model of "one port" circuit



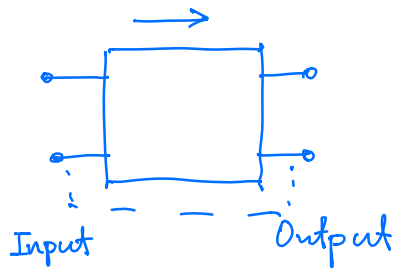
Thevenin Equivalent circuit (small signal)



Norton Equivalent circuit



## Two-Port Equivalent Circuit (Small Signal)

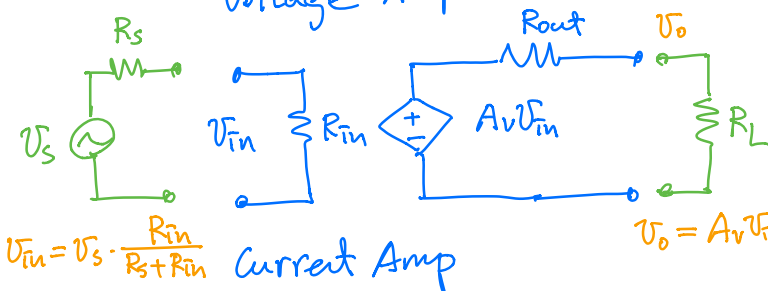


For amplifiers:

- Linear
- Unilateral: output dep. on input, but input is not affected by output. General true.

Input	Type	Output	Transfer fx
Voltage	Voltage Amp	Voltage	$V_o/V_i$
Current	Current Amp	Current	$i_o/i_i$
Voltage	Transconductance Amp.	Current	$i_o/V_i$ [S]
Current	Transresistance Amp (Transimpedance Amp)	Voltage	$V_o/i_i$ [ $\Omega$ ]

### Voltage Amp



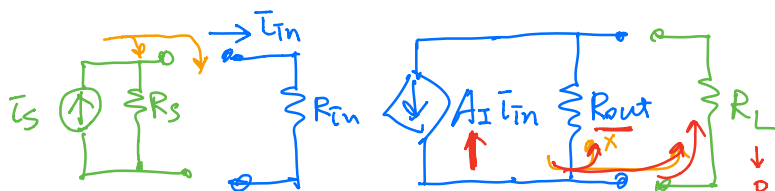
$$V_{in} = V_s \cdot \frac{R_{in}}{R_s + R_{in}}$$

$$V_o = A_v V_{in} \frac{R_L}{R_{out} + R_L}$$

Ideal Values

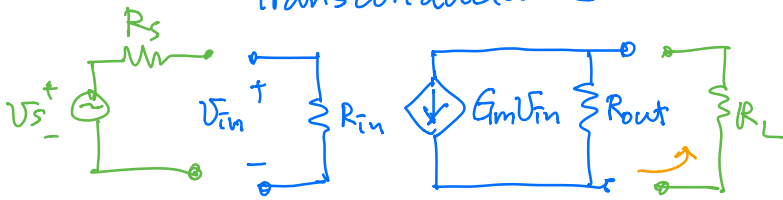
$$R_{in} = \infty \quad R_{out} = 0$$

### Current Amp



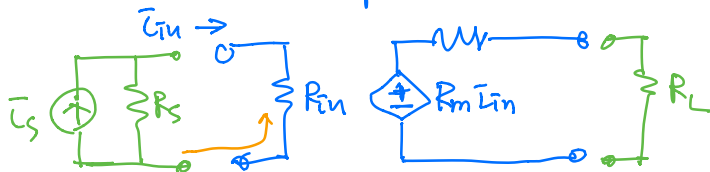
$$R_{in} = 0 \quad R_{out} = \infty$$

Transconductance



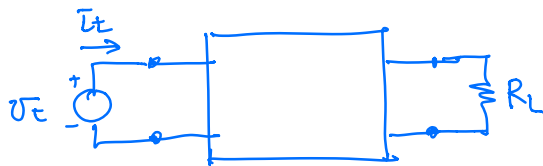
$R_{in} = \infty$     $R_{out} = \infty$

Transimpedance



$R_{in} = 0$     $R_{out} = 0$

How do we calculate  $R_{in}$ ?



$R_{in} = \frac{V_T}{I_T} \left| \begin{array}{l} \text{No } R_S \\ \text{Include } R_L \end{array} \right.$

$R_{out}$ ?



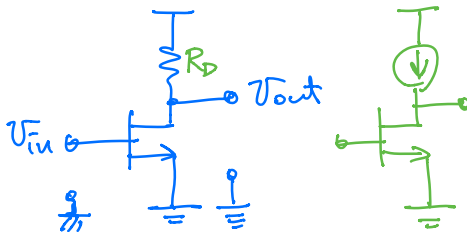
$R_{out} = \frac{V_T}{I_T} \left| \begin{array}{l} \text{No } R_L \\ \text{Include } R_S \end{array} \right.$

Single Transistor Circuit, 3 terminals (S, D, G)  
 2-port circuit 4 "

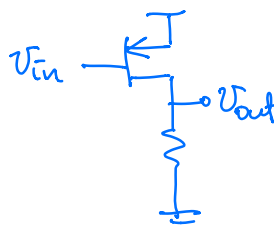
↳ One terminal is used in both input and output

↳ common

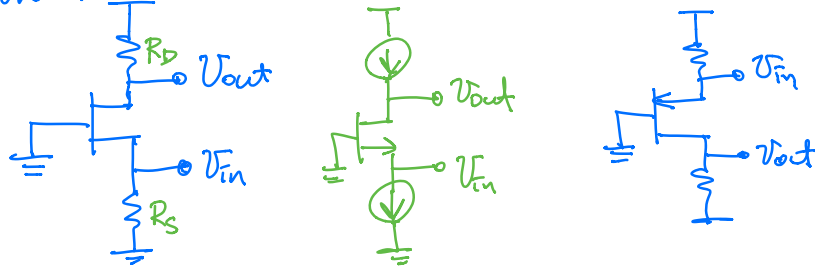
Common Source Amp



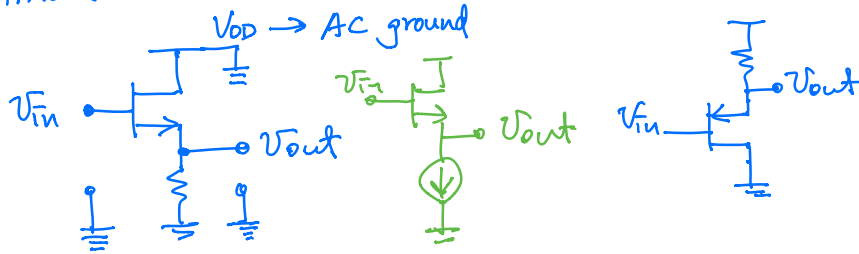
PMOS



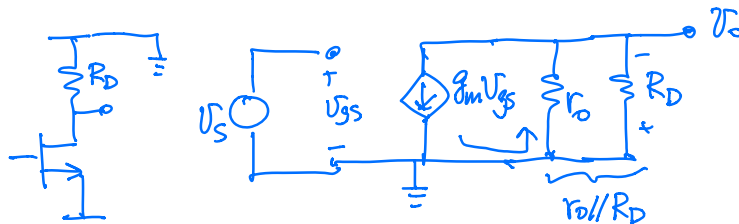
### Common Gate



### Common Drain



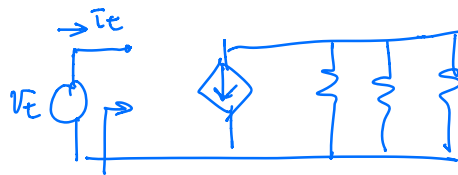
### Common Source



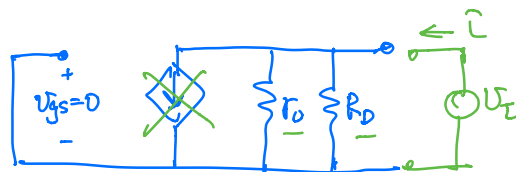
$$V_o = -g_m V_{gs} (r_o // R_D) = -g_m V_s (r_o // R_D)$$

$$A_v = \frac{V_o}{V_s} = -g_m (r_o // R_D)$$

$$R_{in} = \infty$$



$$R_{out} = r_o // R_D$$



Typical values.

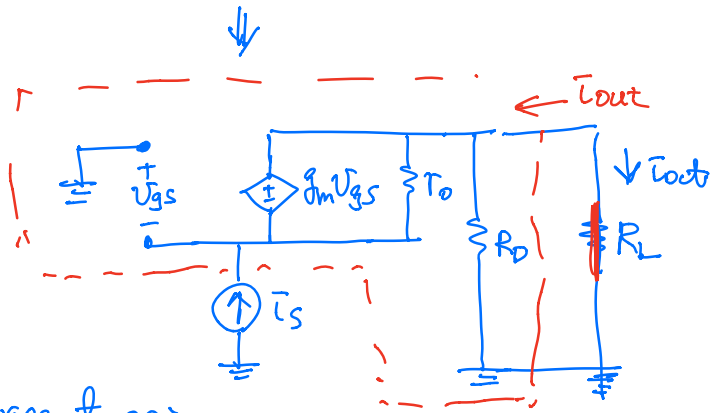
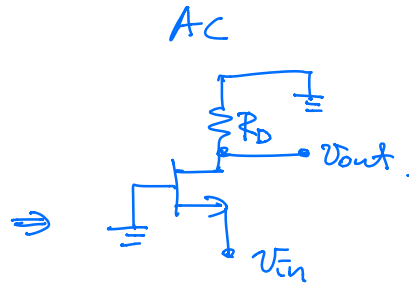
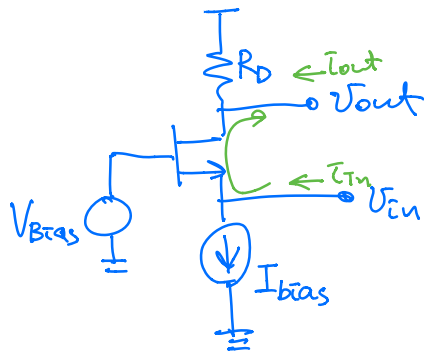
$$r_o \sim 200k\Omega. \quad R_D = \text{a few } k\Omega$$

$$\Rightarrow r_o // R_D \approx R_D$$

Replace  $R_D$  by  $\downarrow$   $R_D \rightarrow \infty$

$$R_{out} = r_o // \infty = r_o$$

## Common Gate

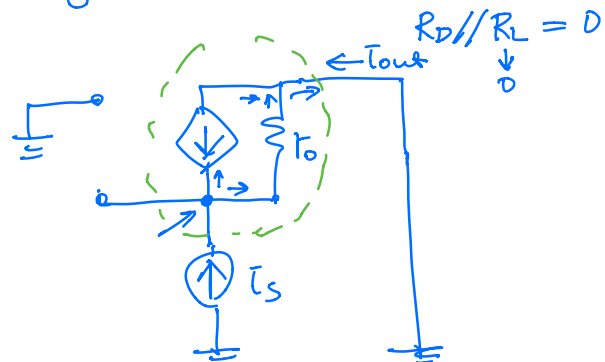


To evaluate  $A_I = \text{current gain}$

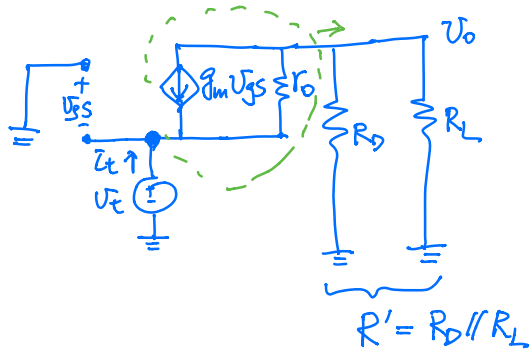
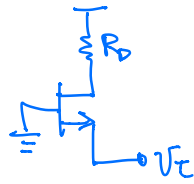
Make  $R_L = 0$

$$\bar{i}_{out} = -\bar{i}_s$$

$$A_I = \frac{\bar{i}_{out}}{\bar{i}_s} = -1$$



$R_{in}$ :



KCL at Source

$$\bar{I}_t + g_m V_{gs} = \frac{V_t - V_o}{r_o}$$

$$\begin{cases} V_{gs} = 0 - V_t = -V_t \\ V_o = \bar{I}_t \cdot R' \end{cases}$$

$$\bar{I}_t - g_m V_t = \frac{V_t}{r_o} - \bar{I}_t R' \frac{1}{r_o}$$

$$\bar{I}_t \left(1 + \frac{R'}{r_o}\right) = \left(g_m + \frac{1}{r_o}\right) V_t$$

$$R_{in} = \frac{V_t}{\bar{I}_t} = \frac{1 + \frac{R'}{r_o}}{g_m + \frac{1}{r_o}} \approx \frac{1}{g_m}$$

Typical values

$$g_m \sim 0.5 \text{ mS}$$

$$r_o \sim 200 \text{ k}\Omega \quad \cdot \frac{1}{r_o} = \frac{1}{2 \times 10^5} = 5 \mu\text{S}$$

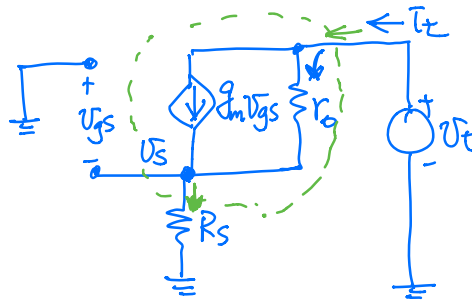
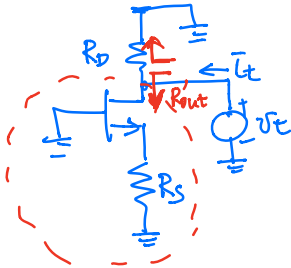
$$R' = R_D \parallel R_L$$

$$\hookrightarrow \sim \text{k}\Omega$$

$$R' \ll r_o$$

↑ small input resistance

$R_{out}$ :



KCL at Drain

$$\bar{I}_t = g_m V_{gs} + \frac{V_t - V_s}{r_o}$$

$$\begin{cases} V_{gs} = 0 - V_s = -V_s \\ V_s = \bar{I}_t \cdot R_s \end{cases}$$

$$\bar{I}_t = -g_m \bar{I}_t \cdot R_s + \frac{V_t - \bar{I}_t R_s}{r_o}$$

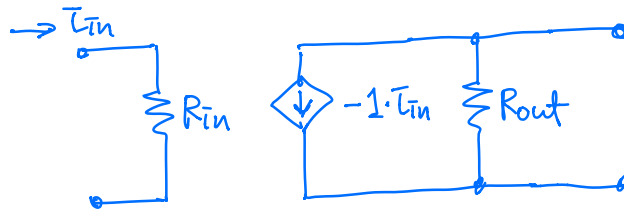
$$\bar{I}_t \left(1 + g_m R_s + \frac{R_s}{r_o}\right) = \frac{V_t}{r_o} \Rightarrow R'_{out} = \frac{V_t}{\bar{I}_t} = r_o + \frac{g_m R_s r_o + R_s}{1}$$

$$\left. \begin{array}{l} r_o \sim 200 \text{ k}\Omega \\ g_m \sim 0.5 \text{ mS} \end{array} \right\} g_m r_o \sim 100 \Rightarrow 1$$

$$R_s \sim \text{k}\Omega (?)$$

$$R'_{out} = r_o + g_m r_o R_s \Rightarrow \text{Very large out resistance}$$

2-Port for CG:



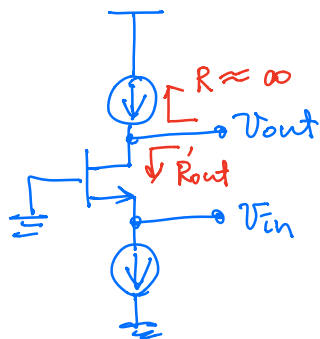
$$R_{in} = \frac{1}{g_m} \quad \text{small}$$

$$R'_{out} = r_o + g_m r_o R_s \quad \text{large}$$

$$R_{out} = R'_{out} \parallel R_D = R_D \parallel (r_o + g_m r_o R_s)$$

$$R_D \sim \text{k}\Omega \ll r_o$$

$$R_{out} \approx R_D$$

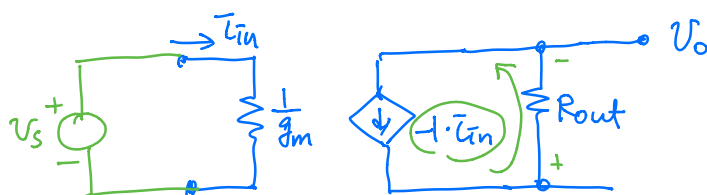


$$R_{out} = R'_{out} \parallel \infty = R'_{out}$$

$$= r_o + g_m r_o R_s$$

Preserve large output resistance.

CG as a voltage amplifier



$$V_o = -(-1 \cdot \bar{i}_{in}) \cdot R_{out} \Rightarrow V_o = \bar{i}_{in} \cdot R_{out} = g_m V_s \cdot R_{out}$$

$$\bar{i}_{in} = \frac{V_s}{\left(\frac{1}{g_m}\right)} = g_m V_s$$

$$R_{out} = r_o + g_m r_o \cdot R_s \gg r_o$$

$\Rightarrow$  higher gain in CG

$$A_v = \frac{V_o}{V_s} = g_m R_{out}$$

Recall for CS amplifier.  $A_v = -g_m (r_o \parallel R_D)$

$$= -g_m r_o \quad \downarrow \infty \text{ for } \textcircled{\downarrow}$$