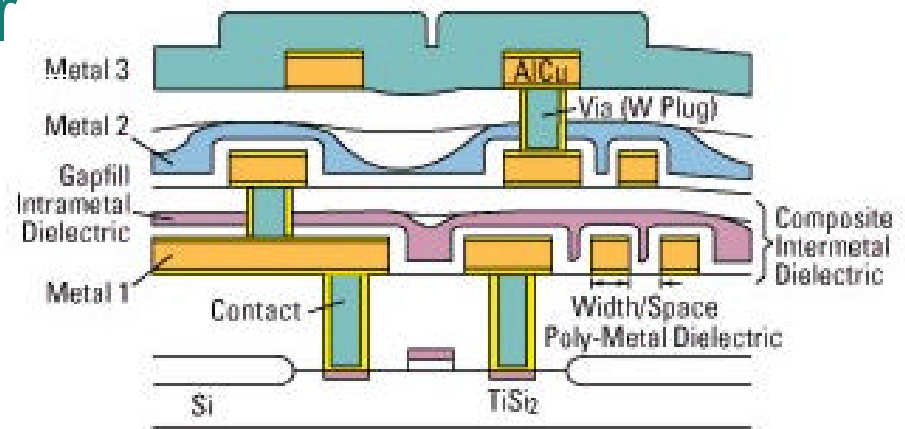


Week 2, Lectures 3-5, February 22-26, 2001

EECS 105 Microelectronics Devices and Circuits, Spring 2001

Andrew R. Neureuther

Topics: Practice Loop and Node Eqns., Two-Ports, Silicon Physics – Carriers, Process Flow and Layout, Sheet Resistance, Squares



Reading for week: (review of EE 40), HS 8.2.2, 9.1, 2.1-2.4, 2.5.4-2.6, 4.1.1, 4.5.7, 6.2, 7.1.1, 7.7,

Version 1/21/01

Outline: Week 2 Lectures 3-5

L3: More Basic Circuits (HS 8.2.2, 9.1)

Loop and Node Equations, Two-Ports

L4: Silicon Physics (HS 2.1-2.4, 2.5.4, 4.1.1, 5.4.7, 6.2, 7.1.1, 7.1)

Carriers, Process Flow and Layout

L5: IC Resistors (HS 2.6)

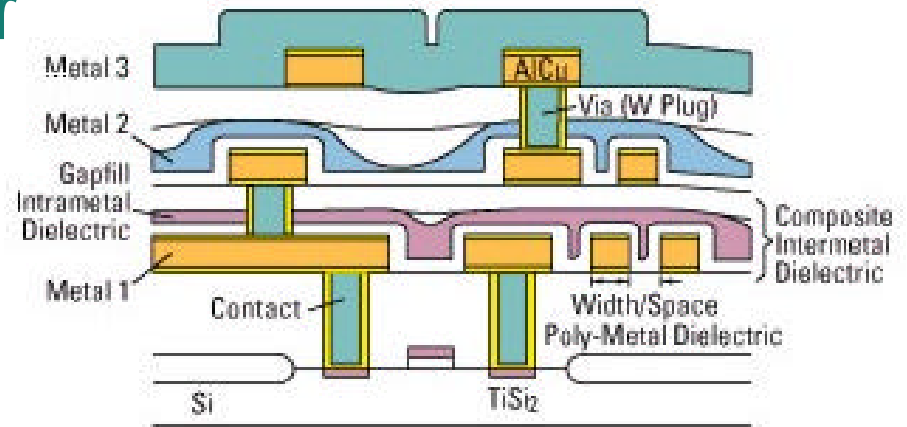
Sheet resistance and Number of Squares

Lecture 3, February 22, 2001

EECS 105 Microelectronics Devices and Circuits, Spring 2001

Andrew R. Neureuther

Topics:
Practice Circuit Analysis,
Two-Ports



**Reading: (review of EE
40), HS 8.2.2, 9.1**

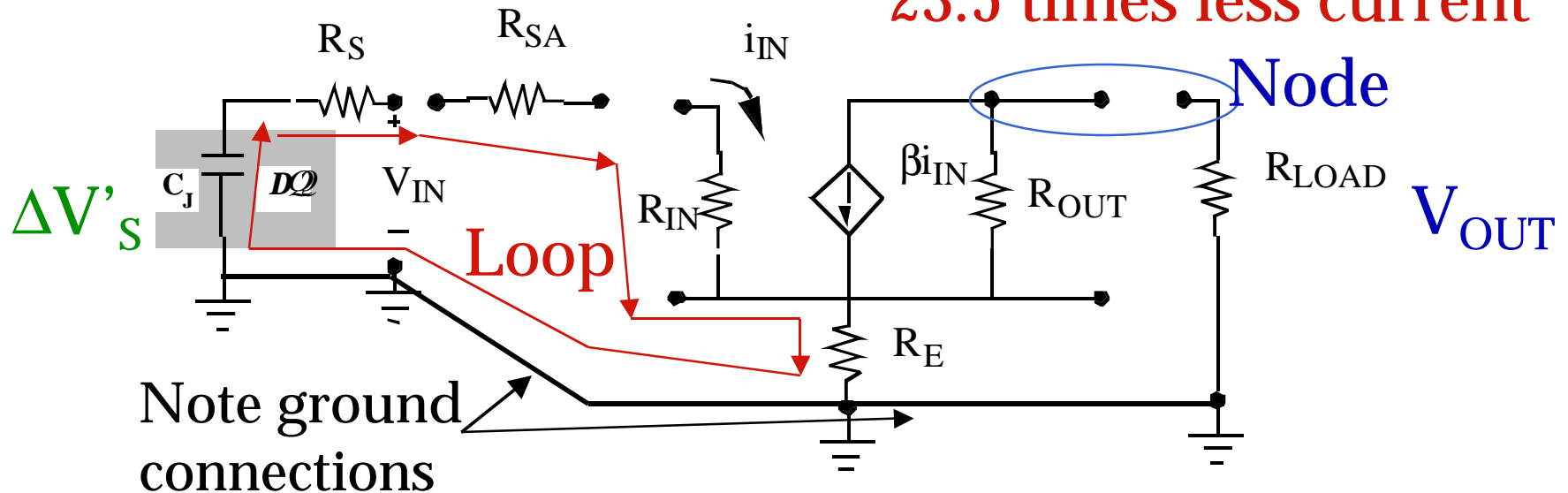
W2 M L3 : More Basic Circuits

- Practice circuit analysis
 - » R_{IN} with R_E
 - » Gain or R_{out} with R_E
- Standard Two-ports
- Difficulty of two-ports with output coupled back to input

High Input Impedance Circuit

$$R_E = 30 \text{ k}\Omega \quad R_{IN \text{ EQ}} = R_{IN} + (\beta + 1)R_E = 3.06 \text{ M}\Omega$$

23.5 times less current

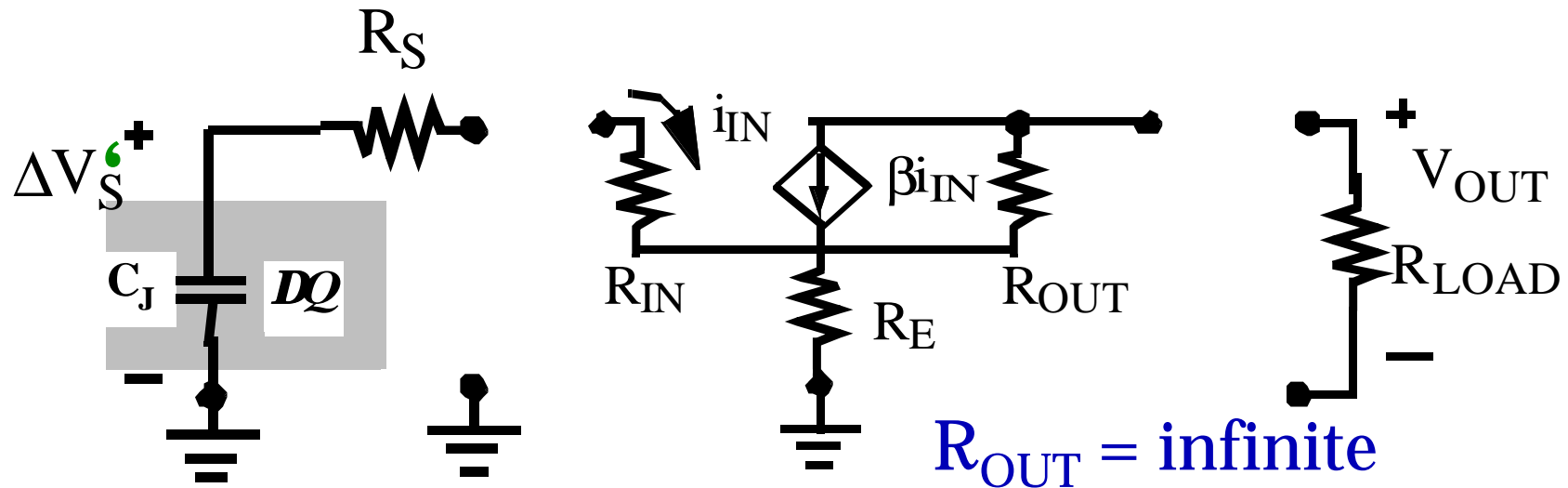


$$V_{OUT} = \left[\frac{\Delta V'_S}{(R_S + R_{SA} + R_{IN \text{ EQ}})} \right] (-\beta) R_{LOAD} = 5 \text{ mV}$$

$$\Sigma V_i = 0 \Rightarrow i_{IN}$$

23.5 times smaller gain

High Input Impedance Circuit

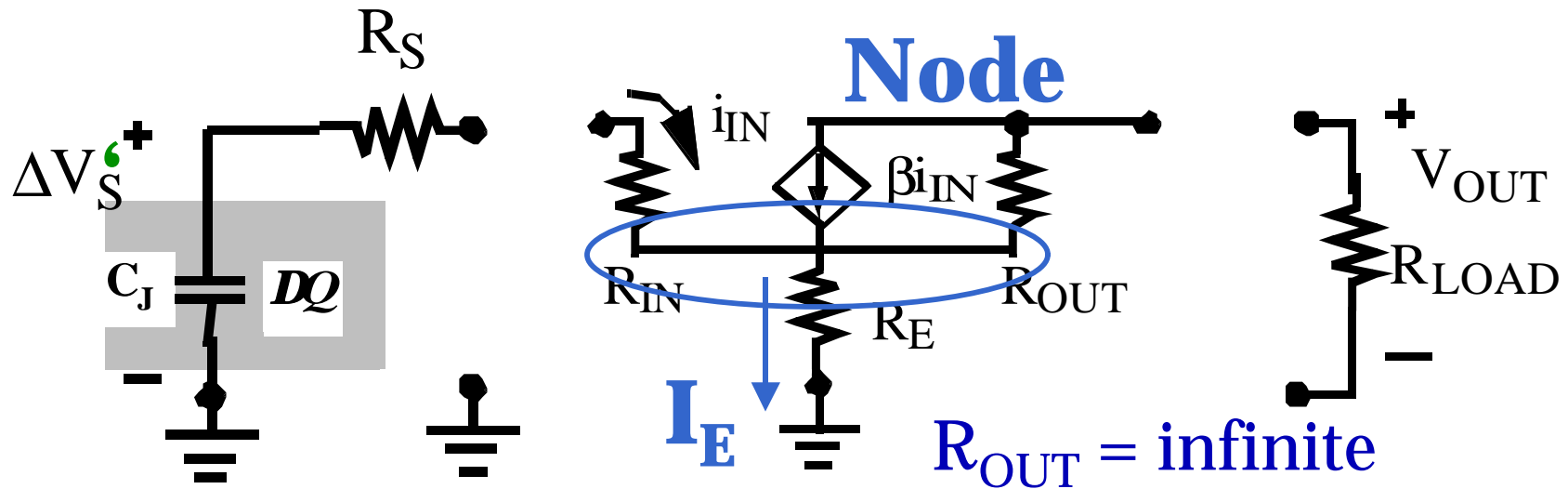


Result:

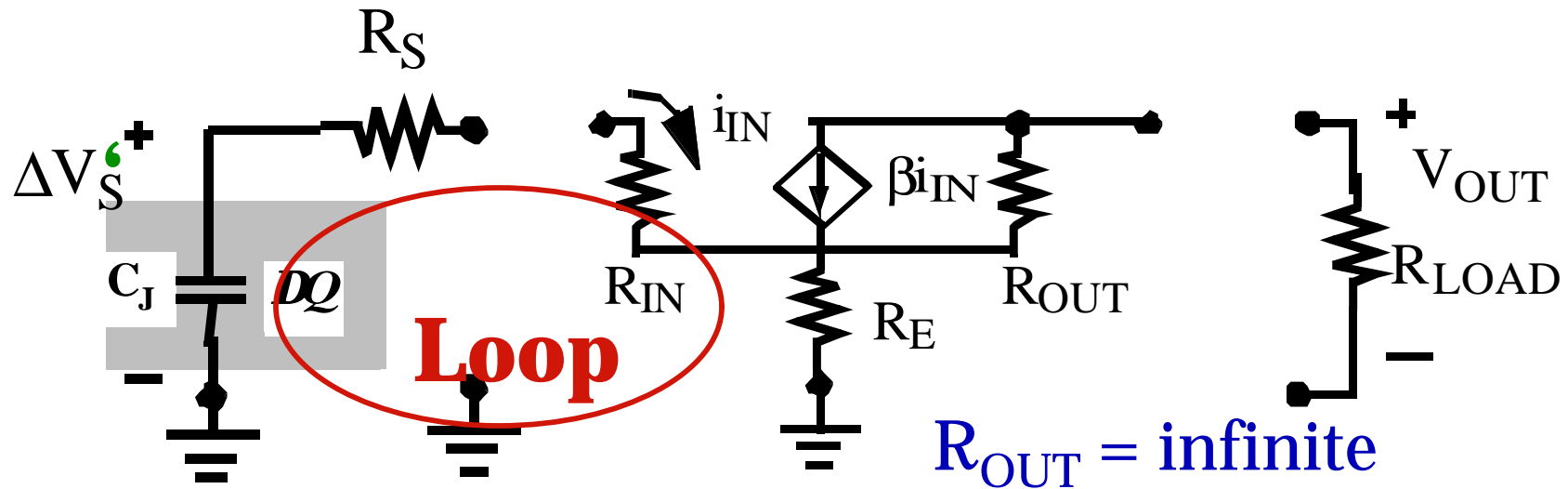
$$V_{OUT} = [\Delta V'_S / (R_S + R_{SA} + R_{IN\ EQ})] (-\beta) R_{LOAD}$$

How is the circuit analysis done?

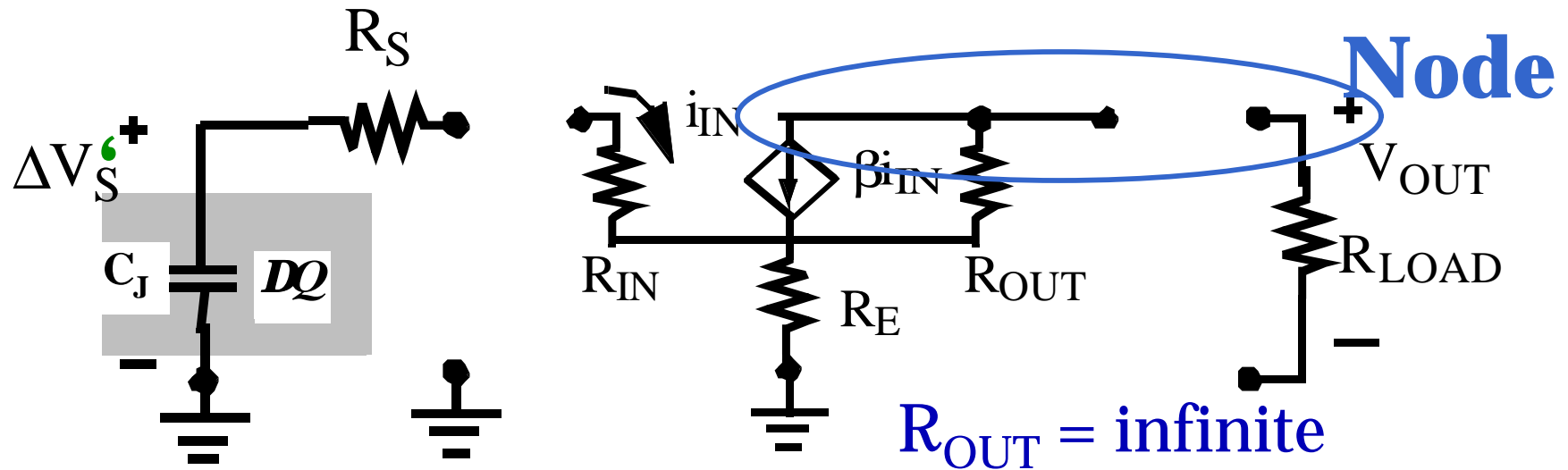
Write a Node Equation for I_E



Write a Loop Equation for I_{IN}

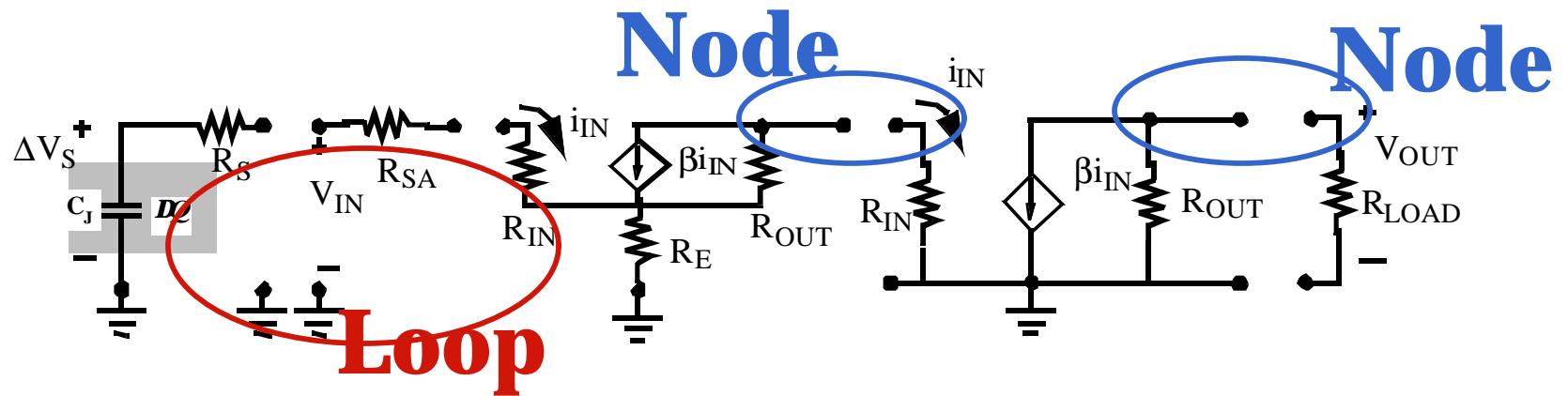


Find $V_{OUT}/\Delta V'_s$



$$V_{OUT}/\Delta V'_s = [1/(R_S + R_{SA} + R_{IN\ EQ})](-\beta)R_{LOAD}$$

Analysis of Multistages



Background on Two-Ports

- Designed for cascading components
 - » Hi-Fi components
 - » IC stages of amplifier circuit
- Based on Matrix Multiplication

$$V_1 = Z_{11}I_1 + Z_{12}I_2$$

$$I_1 = Y_{11}V_1 + Y_{12}V_2$$

$$V_1 = H_{11}I_1 + H_{12}V_2$$

$$V_2 = Z_{21}I_1 + Z_{22}I_2$$

$$I_2 = Y_{21}V_1 + Y_{22}V_2$$

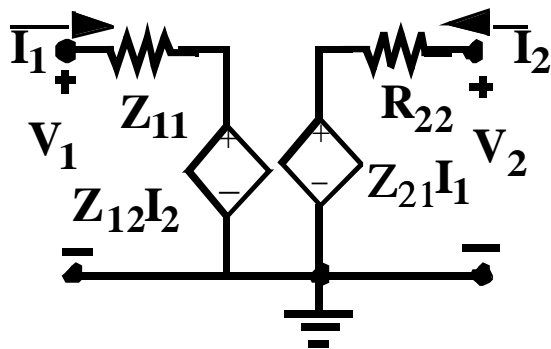
$$I_2 = H_{21}I_1 + H_{22}V_2$$

Impedance
(transresistance)

Admittance
(transconductance)

Hybrid_1
(current 1-2)

Two-Port Equivalent Circuits

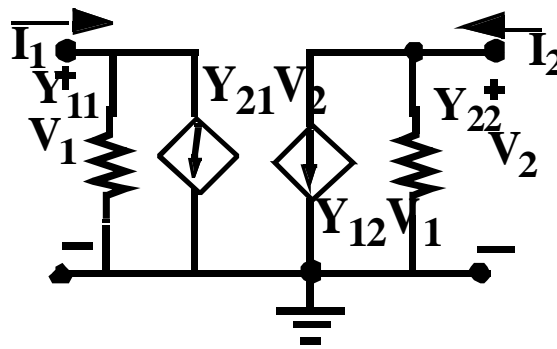


$$V_1 = Z_{11}I_1 + Z_{12}I_2$$

$$V_2 = Z_{21}I_1 + Z_{22}I_2$$

Two Thevenin

(transresistance)

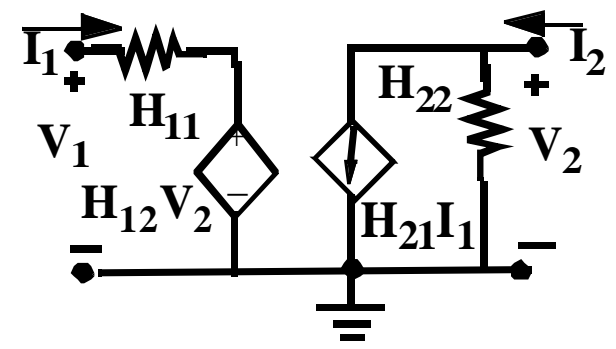


$$I_1 = Y_{11}V_1 + Y_{12}V_2$$

$$I_2 = Y_{21}V_1 + Y_{22}V_2$$

Two Norton

(transconductance)



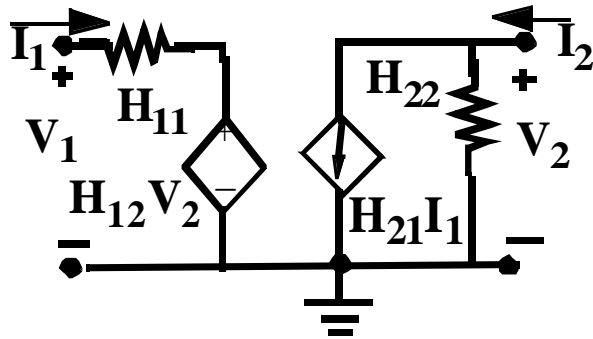
$$V_1 = H_{11}I_1 + H_{12}V_2$$

$$I_2 = H_{21}I_1 + H_{22}V_2$$

**Thevenin input
Norton output**

(current 1-2)

Finding the Two-Port Parameters



$$V_1 = H_{11}I_1 + H_{12}V_2$$

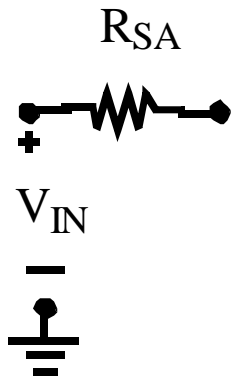
$$I_2 = H_{21}I_1 + H_{22}V_2$$

H_{11} is found by taking V_1 over I_1 when V_2 is zero.

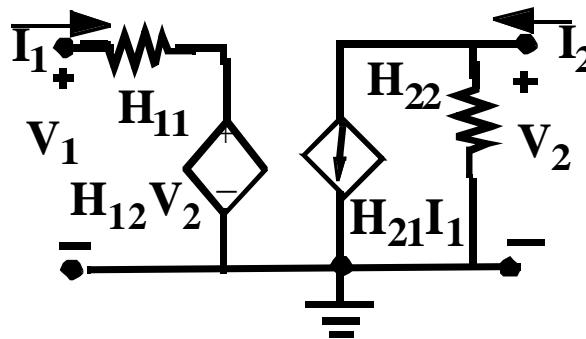
H_{12} is found by taking V_1 over V_2 when I_1 is zero.

Note: The conditions to determine each matrix element arise from the terminal variables multiplying the right hand side.

Hybrid Two-Port for a Resistor



=



$$V_1 = H_{11}I_1 + H_{12}V_2$$

$$I_2 = H_{21}I_1 + H_{22}V_2$$

$$V_2 = 0:$$

$$V_1 = H_{11}I_1 = R_{SA}I_1$$

$$H_{11} = R_{SA}$$

$$I_2 = H_{21}I_1 = -1I_1$$

$$H_{21} = -1$$

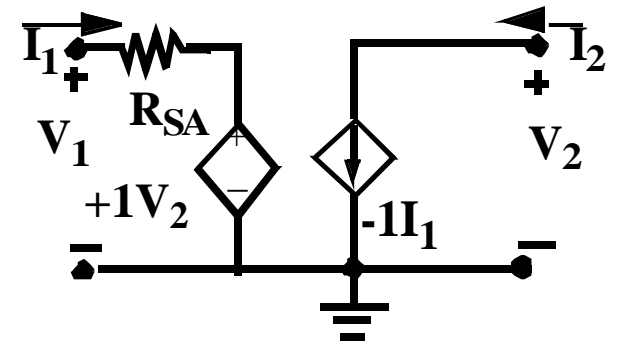
$$I_1 = 0:$$

$$V_1 = H_{12}V_2 = +1V_2$$

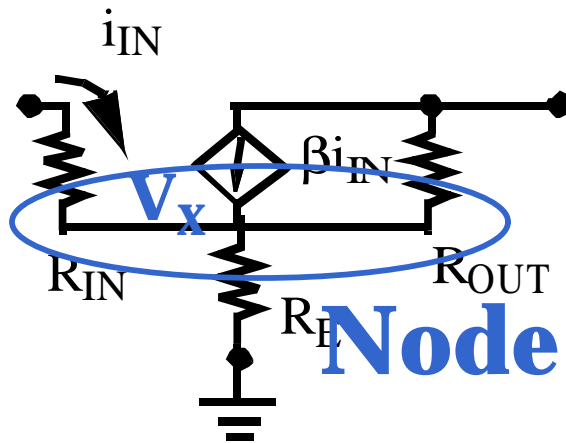
$$H_{12} = +1$$

$$I_2 = H_{22}V_2 = 0V_2$$

$$H_{22} = 0$$



Find H_{11} with R_E and R_{OUT}



$$V_1 = H_{11} I_1 + H_{12} V_2$$

$$I_2 = H_{21} I_1 + H_{22} V_2$$

$$V_X = (\beta + 1) i_{IN} / (1/R_S + 1/R_{OUT})$$

$$V_{IN} = i_{IN} R_{IN} + V_X$$

$$H_{11} = (V_{IN} / i_{IN}) |_{V_2=0} =$$

$$R_{IN} + (\beta + 1) (R_S R_{OUT}) / (R_S + R_{OUT})$$

$V_2 = 0$:

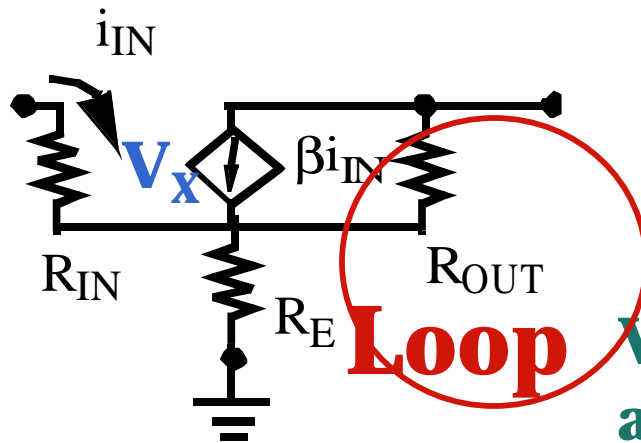
R_{OUT} in || with R_E

Node Eq. For V_X

$$i_{IN} - V_X/R_S - V_X/R_{OUT} + \beta i_{IN} = 0$$

Note: R_{IN} depends on R_{OUT} when the output feeds back to the input.

Find H_{12} with R_E and R_{OUT}



$$\boxed{V_1 = H_{11}I_1 + \mathbf{H_{12}}V_2}$$

$$I_2 = H_{21}I_1 + H_{22}V_2$$

Voltage V_2 is divided across R_{OUT} and R_E

$$I_1 = 0:$$

$$i_{IN} = 0$$

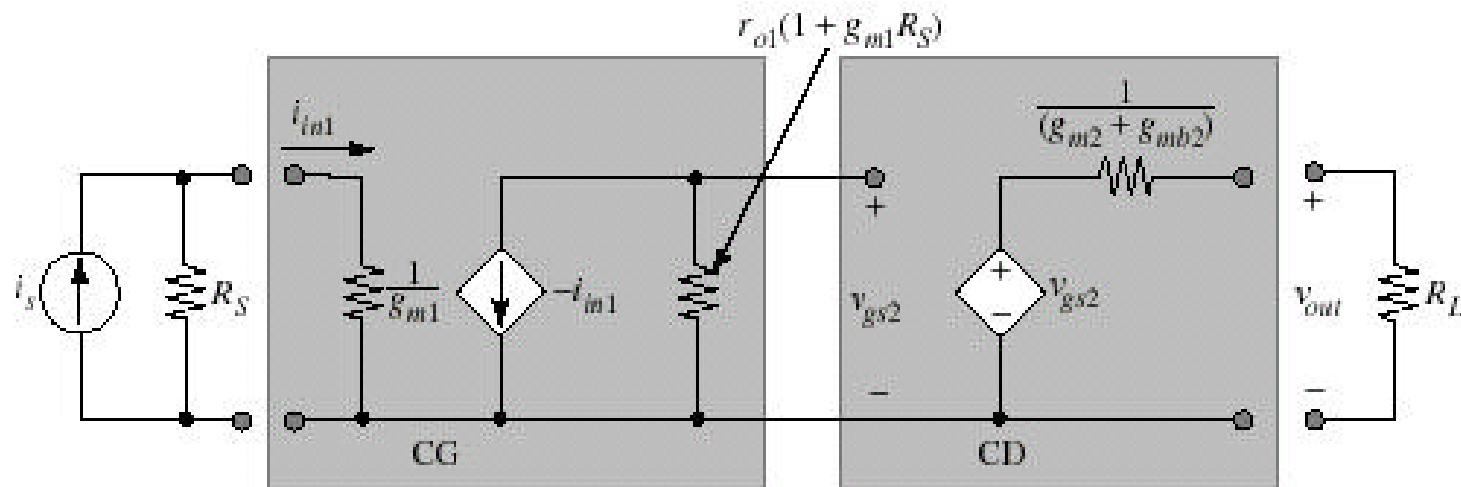
$$V_1 = V_X$$

$$V_1 = V_2 R_E / (R_E + R_{OUT})$$

$$\mathbf{H_{12}} = (V_1 / V_2) |_{I_1=0} = R_E / (R_E + R_{OUT})$$

Note: The voltage source in the input port is not zero when R_E is not zero.

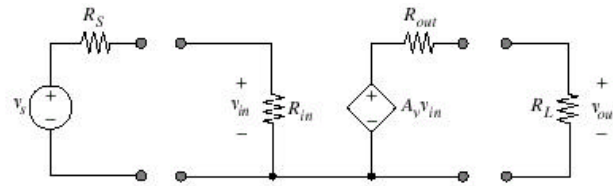
Multistage Amplifiers



This example from the reading
in Chapter 8 this week.

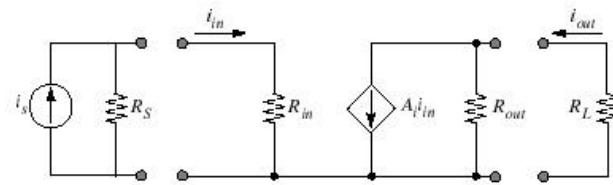
Classification of Two-Port Amplifiers

Voltage Amplifier



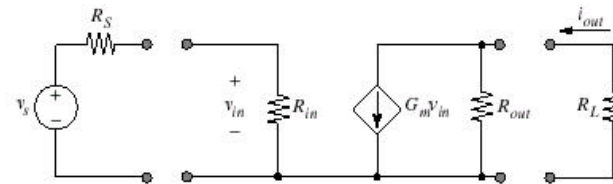
Voltage

Current Amplifier



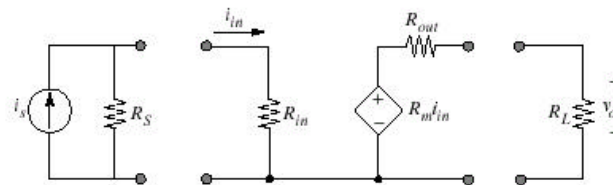
Current

Transconductance Amplifier



Transconductance

Transresistance Amplifier



Transresistance

Figure 8.2

Analog Integrated Circuits

Overview and Circuit Value Added