Floating Point
The IEEE 754 standard defines a binary representation for floating point values using three fields:

- The sign determines the sign of the number (0 for positive, 1 for negative)
- The exponent is in biased notation with a bias of 127
- The significand is akin to unsigned, but used to store a fraction instead of an integer.

The below table shows the bit breakdown for the single precision (32-bit) representation:

<table>
<thead>
<tr>
<th>Sign</th>
<th>Exponent</th>
<th>Significand</th>
</tr>
</thead>
<tbody>
<tr>
<td>1 bit</td>
<td>8 bits</td>
<td>23 bits</td>
</tr>
</tbody>
</table>

There is also a double precision encoding format that uses 64 bits. This behaves the same as the single precision but uses 11 bits for the exponent (and thus a bias of 1023) and 52 bits for the significand.

How a float is interpreted depends on the values in the exponent and significand fields:

For normalized floats:

<table>
<thead>
<tr>
<th>Exponent</th>
<th>Significand</th>
<th>Meaning</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>Anything</td>
<td>Denorm</td>
</tr>
<tr>
<td>1-254</td>
<td>Anything</td>
<td>Normal</td>
</tr>
<tr>
<td>255</td>
<td>0</td>
<td>Infinity</td>
</tr>
<tr>
<td>255</td>
<td>Nonzero</td>
<td>NaN</td>
</tr>
</tbody>
</table>

Value = \((-1)^{\text{Sign}} \times 2^{(\text{Exponent} - \text{Bias})} \times 1.\text{significand}_2\

For denormalized floats:

Value = \((-1)^{\text{Sign}} \times 2^{(\text{Exponent} - \text{Bias} + 1)} \times 0.\text{significand}_2\

Exercises
1. How many zeroes can be represented using a float?
2. What is the largest finite positive value that can be stored using a single precision float?
3. What is the smallest positive value that can be stored using a single precision float?
4. What is the smallest positive normalized value that can be stored using a single precision float?
5. Convert the following numbers from binary to decimal or from decimal to binary:
   0x00000000 8.25 0x000000F0 39.5625 0xFF94BEEF -∞
Representation Exercise

Not every number can be represented perfectly using floating point. For example $\frac{1}{3}$ can only be approximated and thus must be rounded in any attempt to represent it. Sometimes even numbers we may expect to be representable may not be. We will look at analysing those numbers in this next question. For this question we will only look at positive numbers.

1. What is next smallest number larger than 2 that can be represented completely? Next smallest number larger than 4 that can be represented completely? Next smallest number larger than 4 - $2^{22}$ that can be represented completely?

2. Define the stepsize to be the distance between some value $x$ and the smallest value larger than $x$ that can be completely represented. What is the step size for 2? 4? 4 - $2^{22}$?

3. Now let’s see if we can generalize the stepsize for normalized numbers (we can do so for denormalized numbers as well but we won’t in this question). If we are given a normalized number that is not the largest representable normalized number with exponent value $x$ and with significand value $y$ what is the stepsize at that value? Hint: There are 23 significand bits.

4. Now let’s apply this technique. What is the largest odd number that we can represent. Part 3 should be very useful in finding this answer.
AMAT
AMAT is the average (expected) time it takes for memory access. It can be calculated using this formula:
\[
AMAT = \text{hit time} + \text{miss rate} \times \text{miss penalty}
\]

Miss rates can be given in terms of either local miss rates or global miss rates. The *local miss rate* of a cache is the percentage of accesses into the particular cache that miss at the cache, while the *global miss rate* is the percentage of all accesses that miss at the cache.

**Exercises**
Suppose your system consists of:
- A L1$ that hits in 2 cycles and has a local miss rate of 20%
- A L2$ that hits in 15 cycles and has a global miss rate of 5%
- Main memory hits in 100 cycles

1. What is the local miss rate of L2$?

2. What is the AMAT of the system?

3. Suppose we want to reduce the AMAT of the system to 8 or lower by adding in a L3$. If the L3$ has a local miss rate of 30%, what is the largest hit time that the L3$ can have?

Flynn Taxonomy
1. Explain SISD and give an example if available.

2. Explain SIMD and give an example if available.

3. Explain MISD and give an example if available.

4. Explain MIMD and give an example if available.