## Discussion 13: ECC/Parity, RAID

## Hamming ECC

Recall the basic structure of a Hamming code. Given bits $1, \ldots, m$, the bit at position $2^{n}$ is parity for all the bits with a 1 in position $n$. For example, the first bit is chosen such that the sum of all odd-numbered bits is even.

| Bit | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Data | $\underline{\mathrm{P} 1}$ | $\underline{\mathrm{P} 2}$ | D 1 | $\underline{\mathrm{P} 4}$ | D 2 | D 3 | D 4 | $\underline{\mathrm{P}} 8$ | D 5 | D 6 | D 7 | D 8 | D 9 | D 10 | D 11 |
| P 1 | X |  | X |  | X |  | X |  | X |  | X |  | X |  | X |
| P 2 |  | X | X |  |  | X | X |  |  | X | X |  |  | X | X |
| P 4 |  |  |  | X | X | X | X |  |  |  |  | X | X | X | X |
| P 8 |  |  |  |  |  |  |  | X | X | X | X | X | X | X | X |

i. How many bits do we need to add to $0011_{2}$ to allow single error correction?
ii. Which locations in $0011_{2}$ would parity bits be included?
iii. Which bits does each parity bit cover in $0011_{2}$ ?
iv. Write the completed coded representation for $0011_{2}$ to enable single error correction.
v. How can we enable an additional double error detection on top of this?
vi. Find the original bits given the following SEC Hamming Code: $0110111_{2}$
vii.Find the original bits given the following SEC Hamming Code: $1001000_{2}$
viii.Find the original bits given the following SEC Hamming Code: $010011010000110_{2}$

## RAID

Fill out the following table:

|  | Configuration | Pro / Good for... | Con / Bad for... |
| :--- | :--- | :--- | :--- |
| RAID 0 |  |  |  |
| RAID 1 |  |  |  |
| RAID 2 |  |  |  |
| RAID 3 |  |  |  |
| RAID 4 |  |  |  |
| RAID 5 |  |  |  |

