CS 61C:
Great Ideas in Computer Architecture
MIPS Datapath

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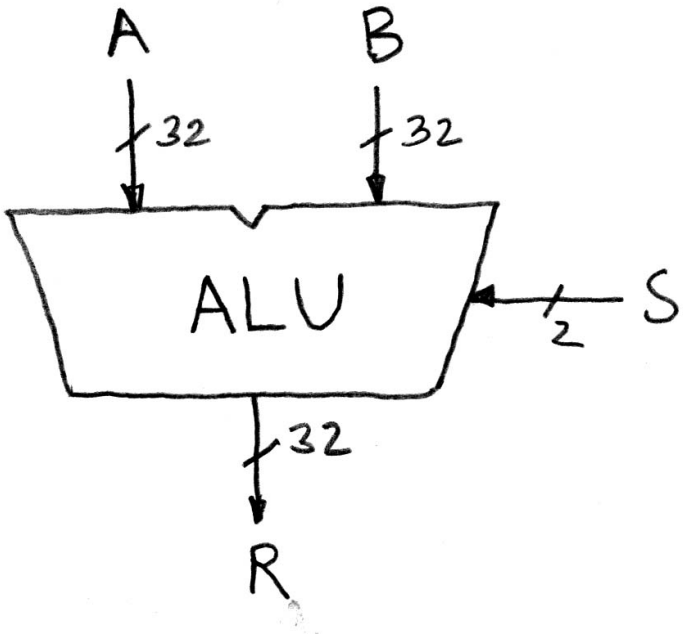
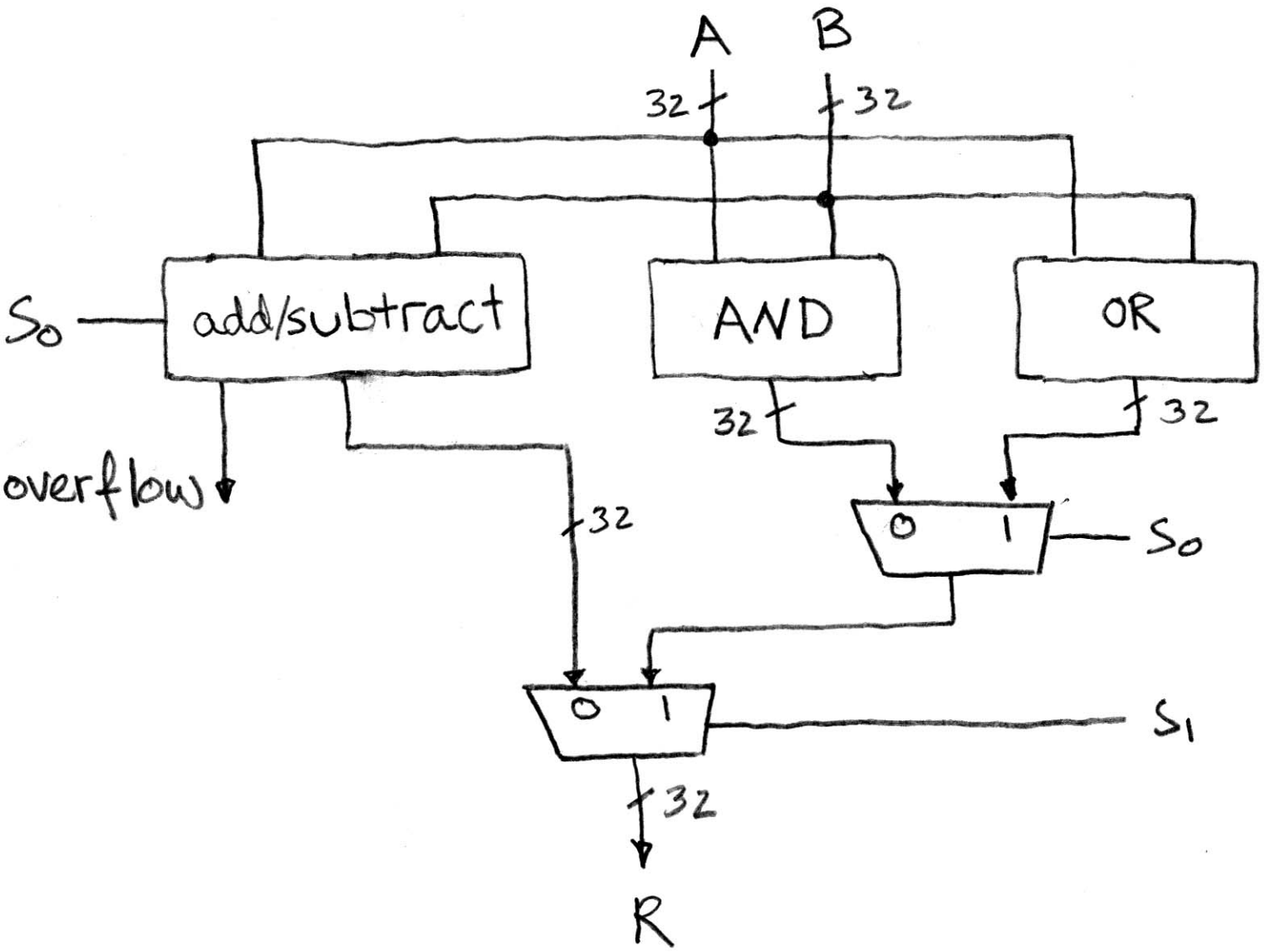
Arithmetic and Logic Unit

- Most processors contain a special logic block called the "Arithmetic and Logic Unit" (ALU)
- We'll show you an easy one that does ADD, SUB, bitwise AND, bitwise OR



when S=00, R=A+B
when S=01, R=A-B
when S=10, R=A AND B
when S=11, R=A OR B

Our simple ALU



How to design Adder/Subtractor?

- Truth-table, then determine canonical form, then minimize and implement as we've seen before
- Look at breaking the problem down into smaller pieces that we can cascade or hierarchically layer

Adder/Subtractor – One-bit adder LSB… (Half Adder)

$$
\begin{array}{cccc|c}
 & a_3 & a_2 & a_1 & a_0 \\
+ & b_3 & b_2 & b_1 & b_0 \\
\hline
 & s_3 & s_2 & s_1 & s_0
\end{array}
$$

a_0	b_0	s_0	c_1
0	0	0	0
0	1	1	0
1	0	1	0
1	1	0	1

$$s_0 =$$

$$c_1 =$$

Adder/Subtractor – One-bit full-adder (1/2)…

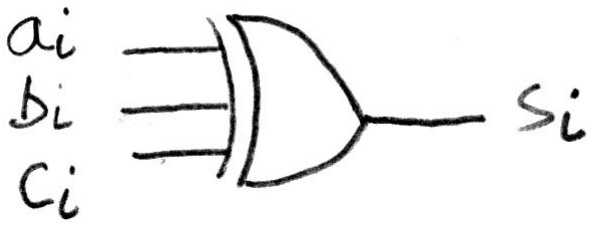
	a_3	a_2	a_1	a_0
+	b_3	b_2	b_1	b_0
	s_3	s_2	s_1	s_0

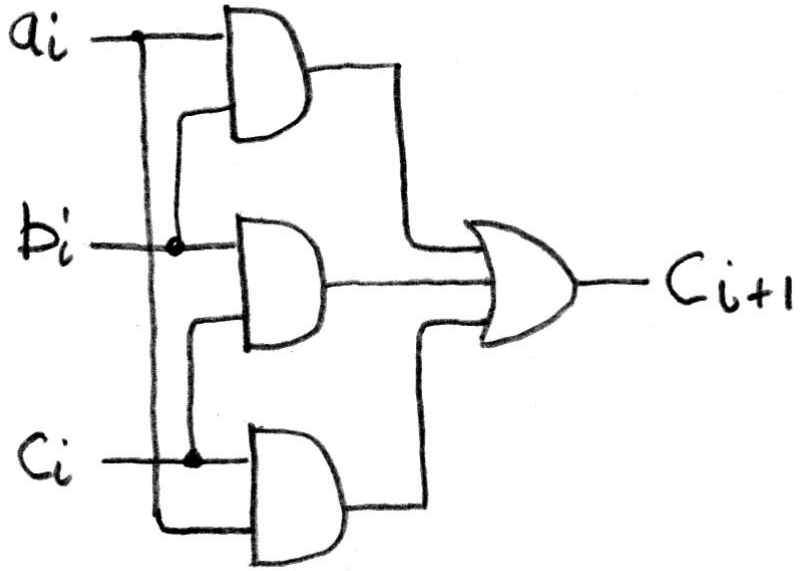
a_i	b_i	c_i	s_i	c_{i+1}
0	0	0	0	0
0	0	1	1	0
0	1	0	1	0
0	1	1	0	1
1	0	0	1	0
1	0	1	0	1
1	1	0	0	1
1	1	1	1	1

$$s_i =$$

$$c_{i+1} =$$

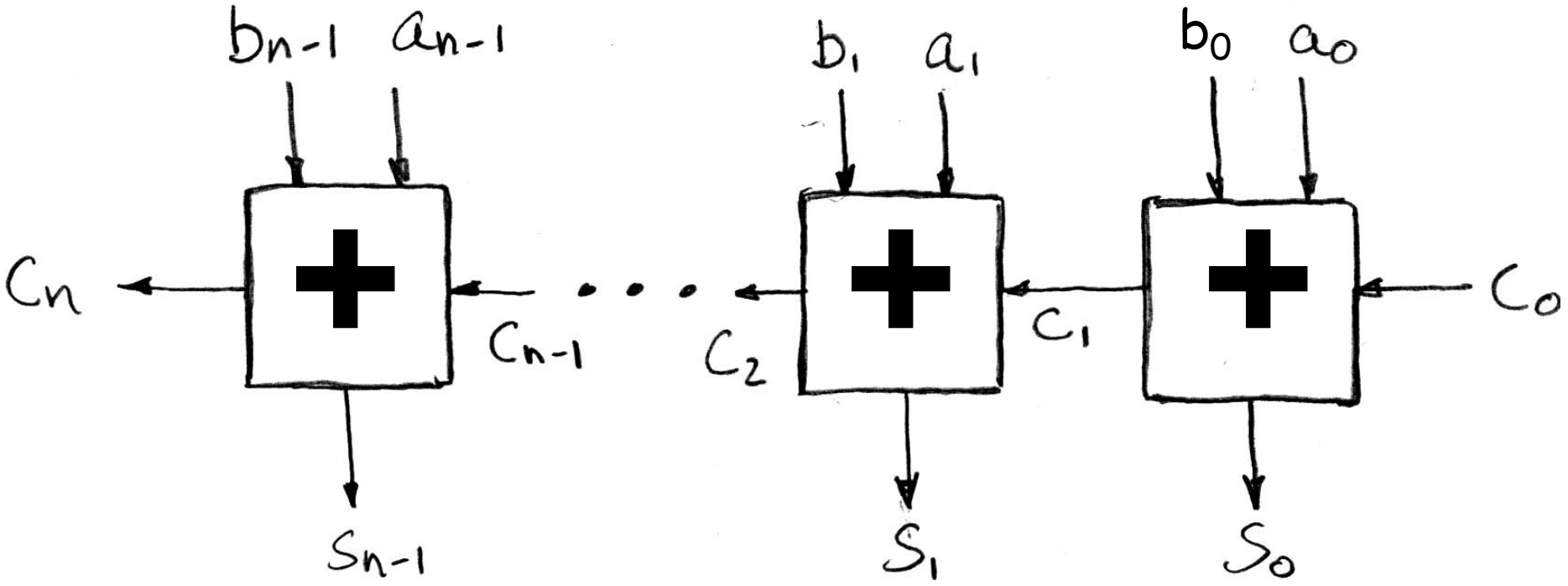
Adder/Subtractor – One-bit adder (2/2)





$$
\begin{aligned}
s_i &= \mathrm{XOR}(a_i, b_i, c_i) \\
c_{i+1} &= \mathrm{MAJ}(a_i, b_i, c_i) = a_i b_i + a_i c_i + b_i c_i
\end{aligned}
$$

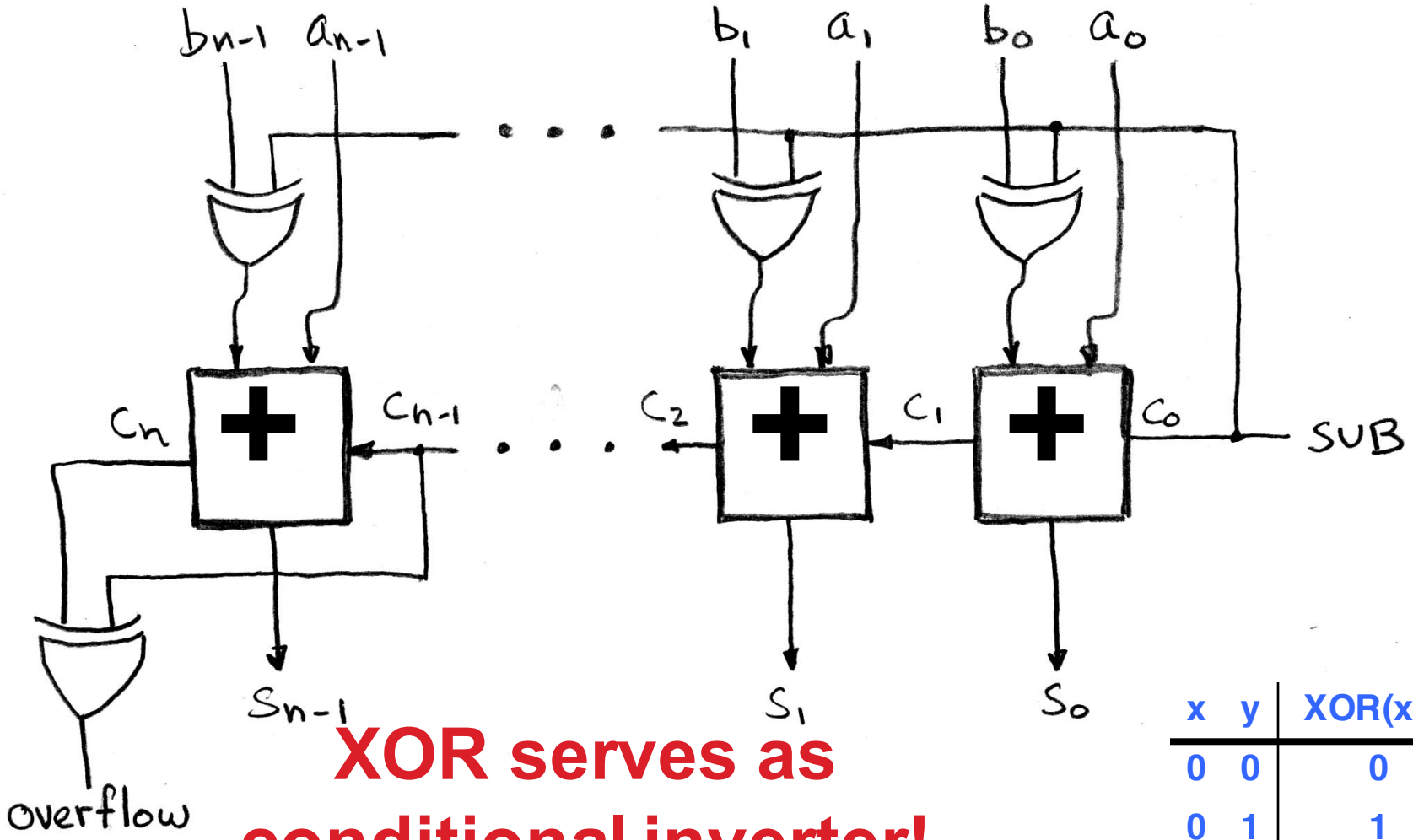
N 1-bit adders ⇒ 1 N-bit adder



What about overflow?

Overflow = c_n?

Extremely Clever Adder/Subtractor



XOR serves as conditional inverter!

Aka "Subtract is Invert and add 1"

x	y	XOR(x,y)
0	0	0
0	1	1
1	0	1
1	1	0

Clicker Question

Convert the truth table to a boolean expression (no need to simplify):

A: F = xy + x(~y)

B: F = xy + (~x)y + (~x)(~y)

C: F = (~x)y + x(~y)

D: F = xy + (~x)y

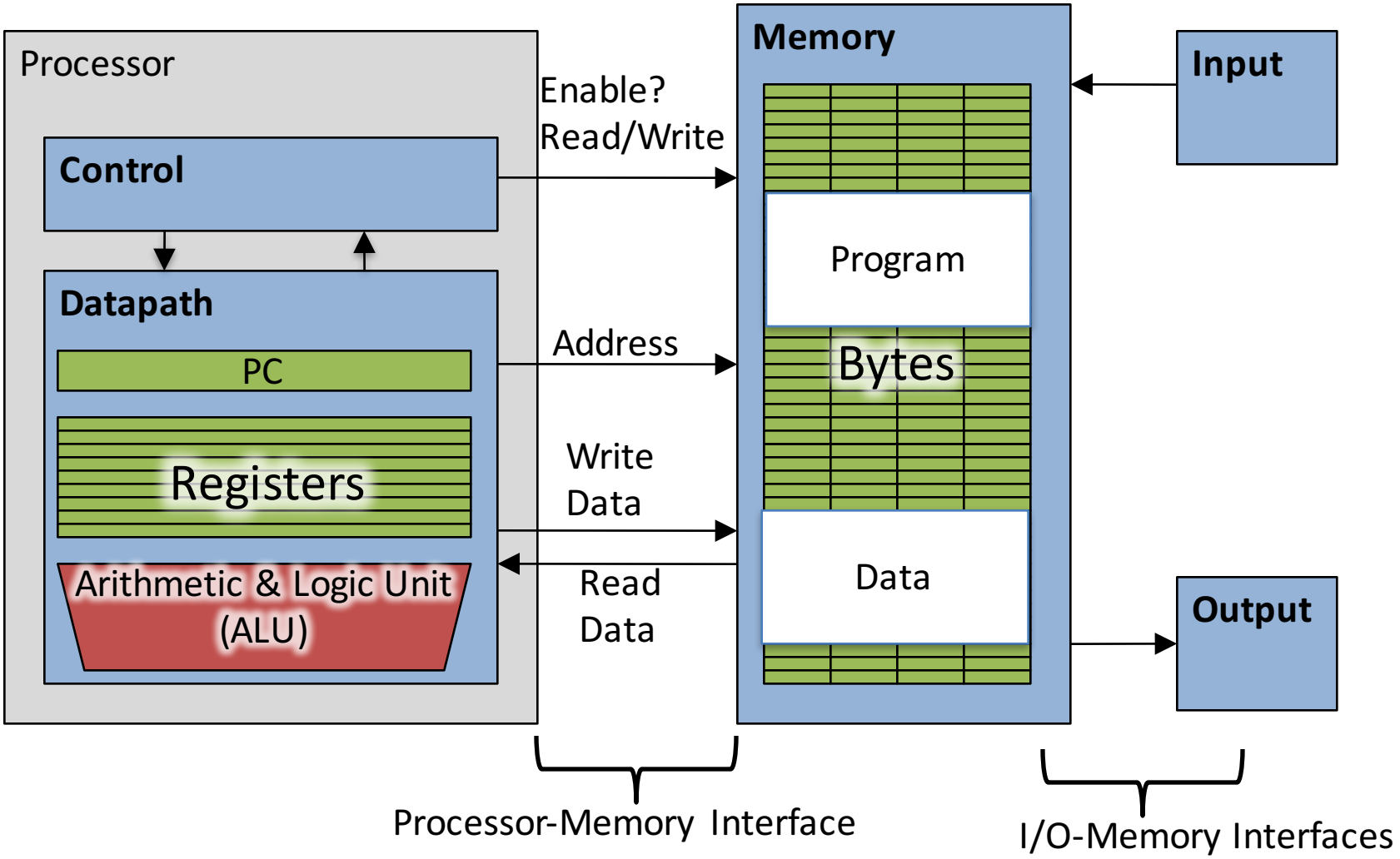
E: F = (x+y)(~x+~y)

x	y	F(x,y)
0	0	0
0	1	1
1	0	0
1	1	1

Administrivia

- Project 2-2 is out!

Components of a Computer

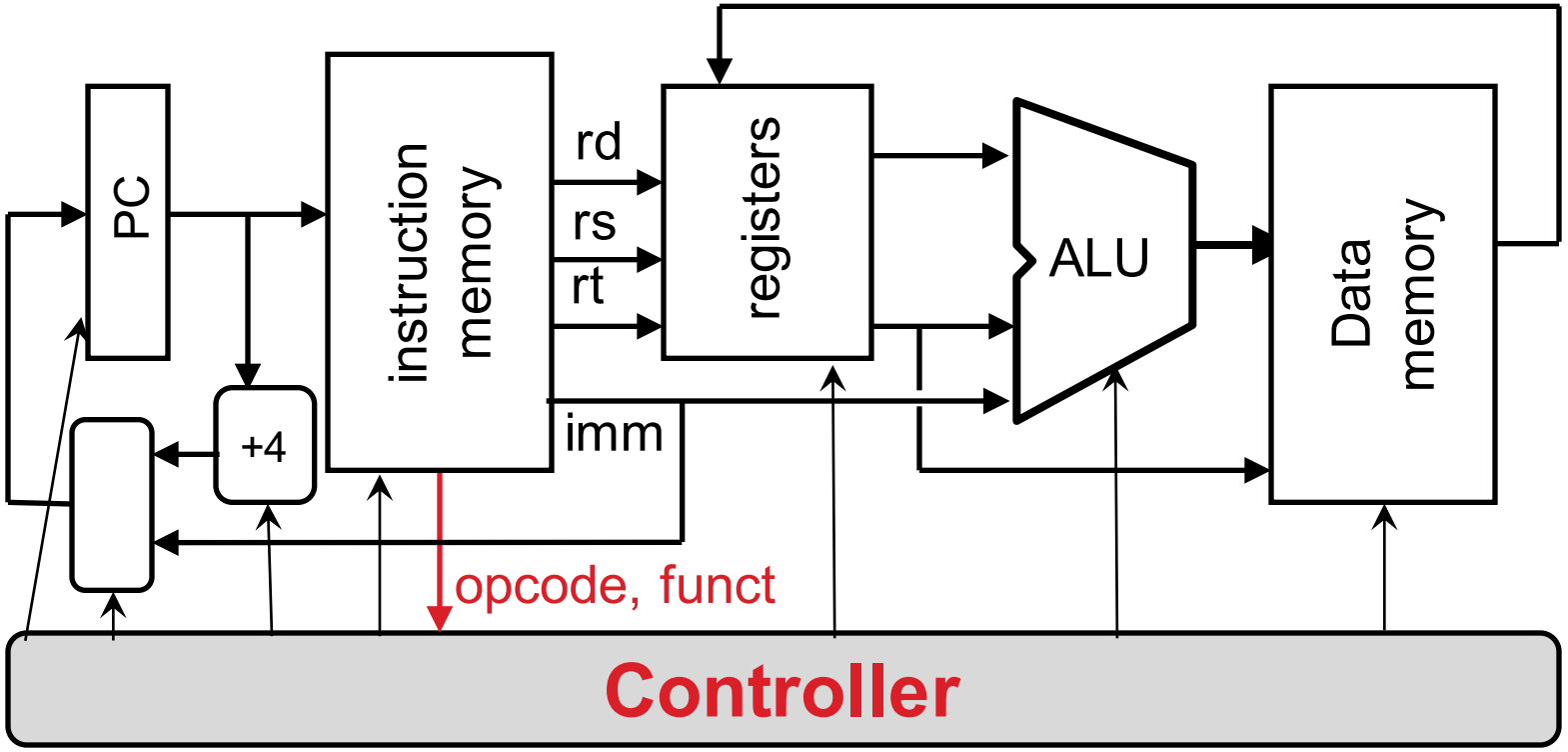


The CPU

- Processor (CPU): the active part of the computer that does all the work (data manipulation and decision-making)
- Datapath: portion of the processor that contains hardware necessary to perform operations required by the processor (the brawn)
- Control: portion of the processor (also in hardware) that tells the datapath what needs to be done (the brain)

Datapath and Control

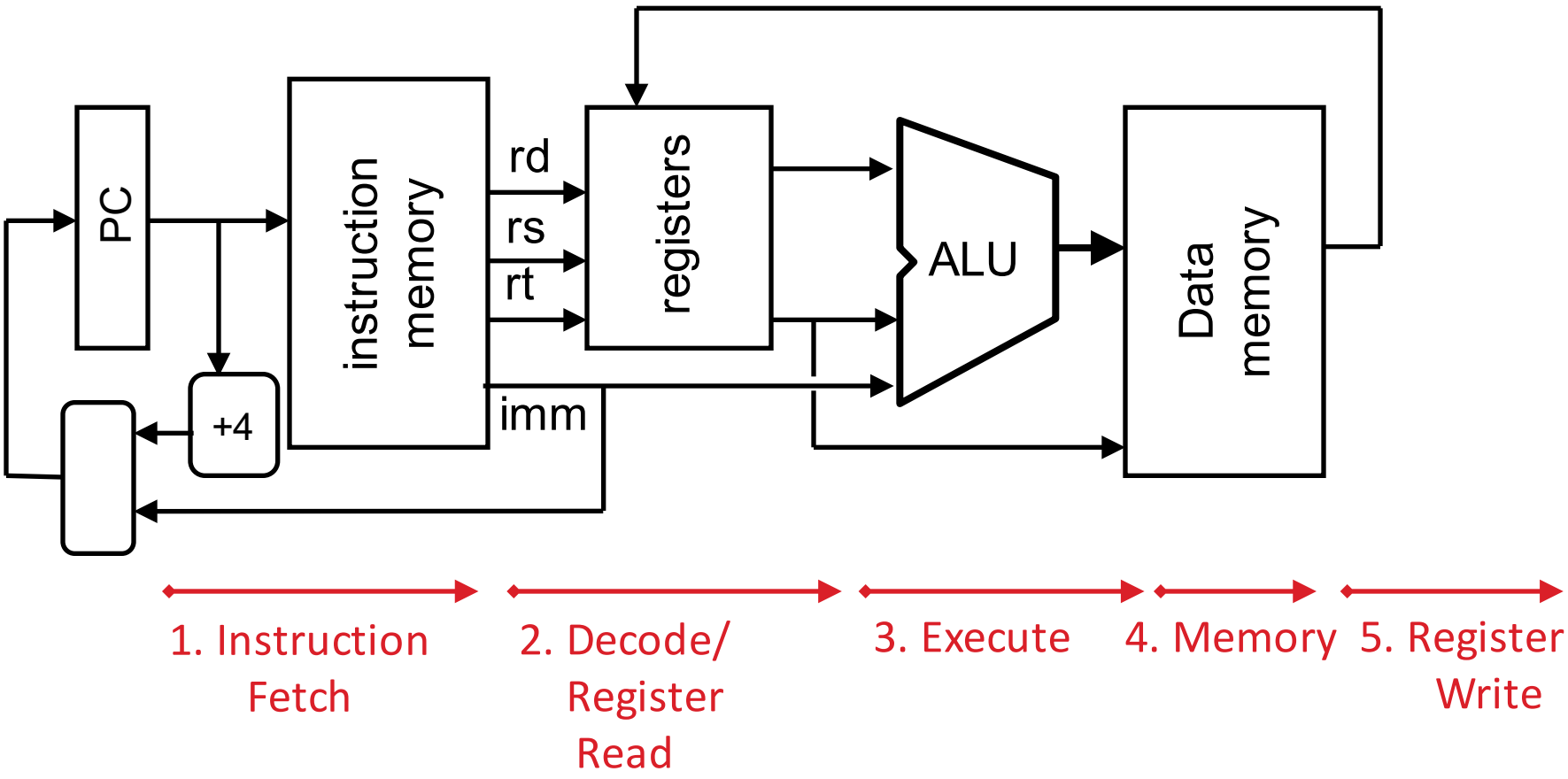
- Datapath designed to support data transfers required by instructions
- Controller causes correct transfers to happen



Five Stages of Instruction Execution

- Stage 1: Instruction Fetch
- Stage 2: Instruction Decode
- Stage 3: ALU (Arithmetic-Logic Unit)
- Stage 4: Memory Access
- Stage 5: Register Write

Stages of Execution on Datapath



Stages of Execution (1/5)

- There is a wide variety of MIPS instructions: so what general steps do they have in common?
- Stage 1: Instruction Fetch
  - no matter what the instruction, the 32-bit instruction word must first be fetched from memory (the cache-memory hierarchy)
  - also, this is where we Increment PC (that is, PC = PC + 4, to point to the next instruction: byte addressing so + 4)

Stages of Execution (2/5)

- Stage 2: Instruction Decode
  - upon fetching the instruction, we next gather data from the fields (decode all necessary instruction data)
  - first, read the opcode to determine instruction type and field lengths
  - second, read in data from all necessary registers
    - for add, read two registers
    - for addi, read one register
    - for jal, no reads necessary

Stages of Execution (3/5)

- Stage 3: ALU (Arithmetic-Logic Unit)
  - the real work of most instructions is done here: arithmetic (+, -, *, /), shifting, logic (&, |), comparisons (slt)
  - what about loads and stores?
    - lw $t0, 40($t1)
    - the address we are accessing in memory = the value in $t1 PLUS the value 40
    - so we do this addition in this stage

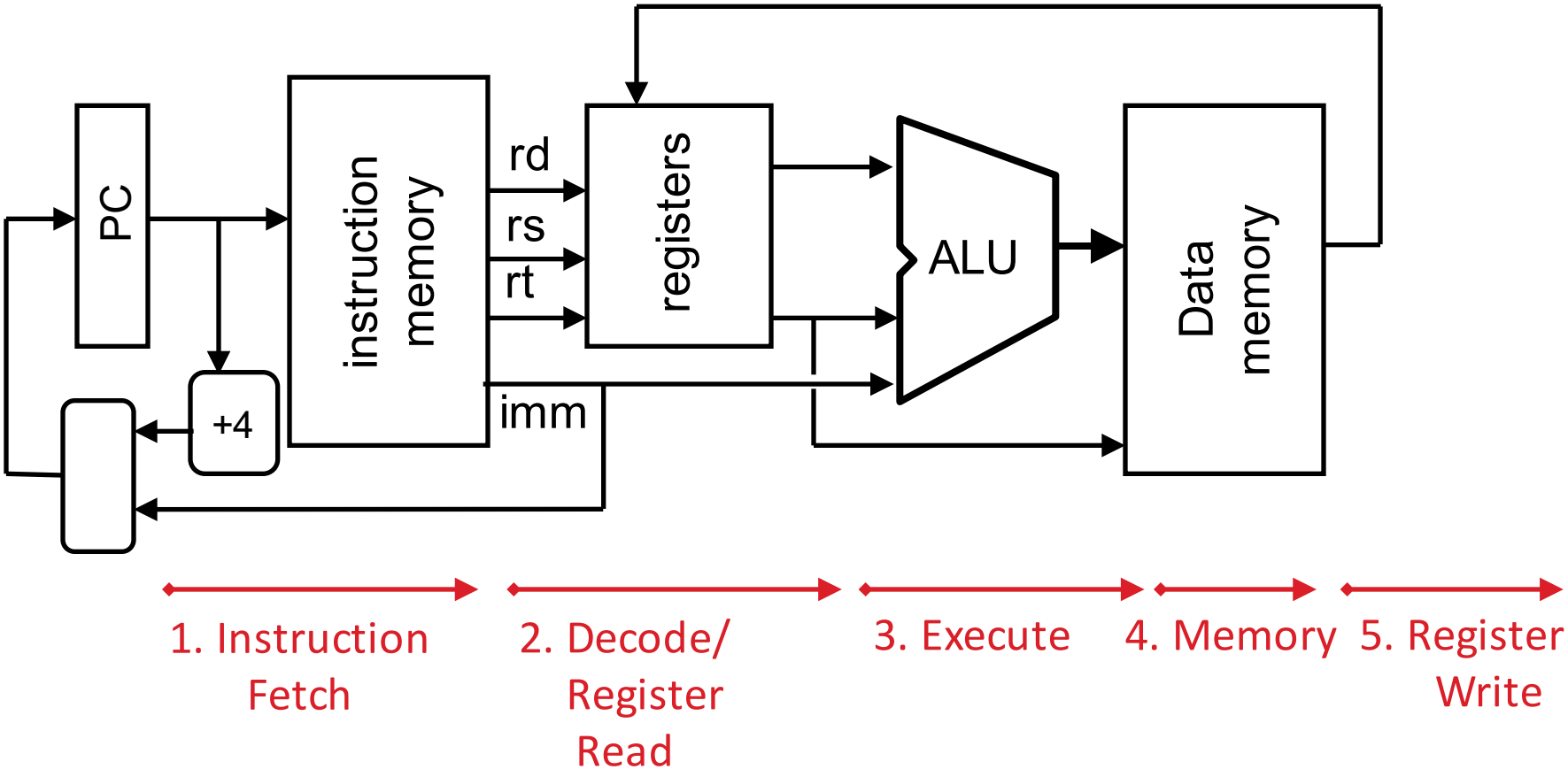
Stages of Execution (4/5)

- Stage 4: Memory Access
  - actually only the load and store instructions do anything during this stage; the others remain idle during this stage or skip it all together
  - since these instructions have a unique step, we need this extra stage to account for them
  - as a result of the cache system, this stage is expected to be fast

Stages of Execution (5/5)

- Stage 5: Register Write
  - most instructions write the result of some computation into a register
  - examples: arithmetic, logical, shifts, loads, slt
  - what about stores, branches, jumps?
    - don't write anything into a register at the end
    - these remain idle during this fifth stage or skip it all together

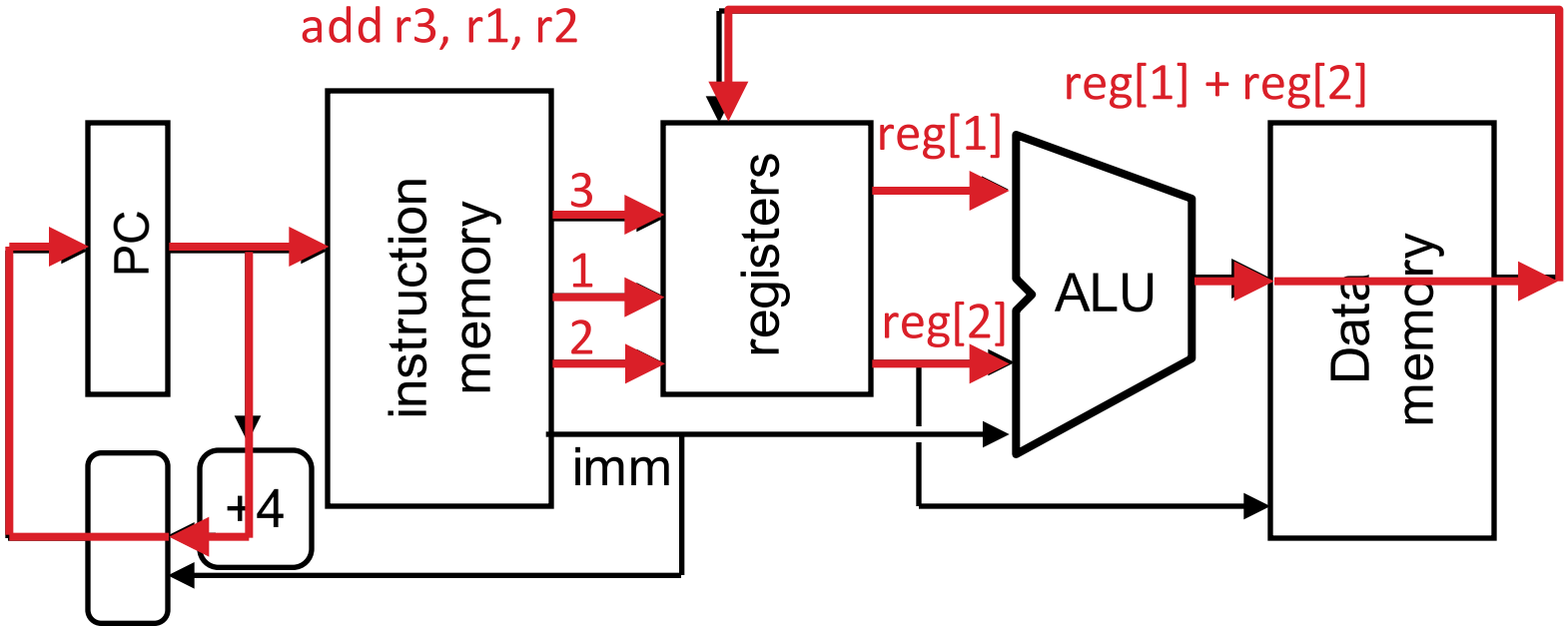
Stages of Execution on Datapath



Datapath Walkthroughs (1/3)

- add $r3,$r1,$r2 # r3 = r1+r2
  - Stage 1: fetch this instruction, increment PC
  - Stage 2: decode to determine it is an add, then read registers $r1 and $r2
  - Stage 3: add the two values retrieved in Stage 2
  - Stage 4: idle (nothing to write to memory)
  - Stage 5: write result of Stage 3 into register $r3

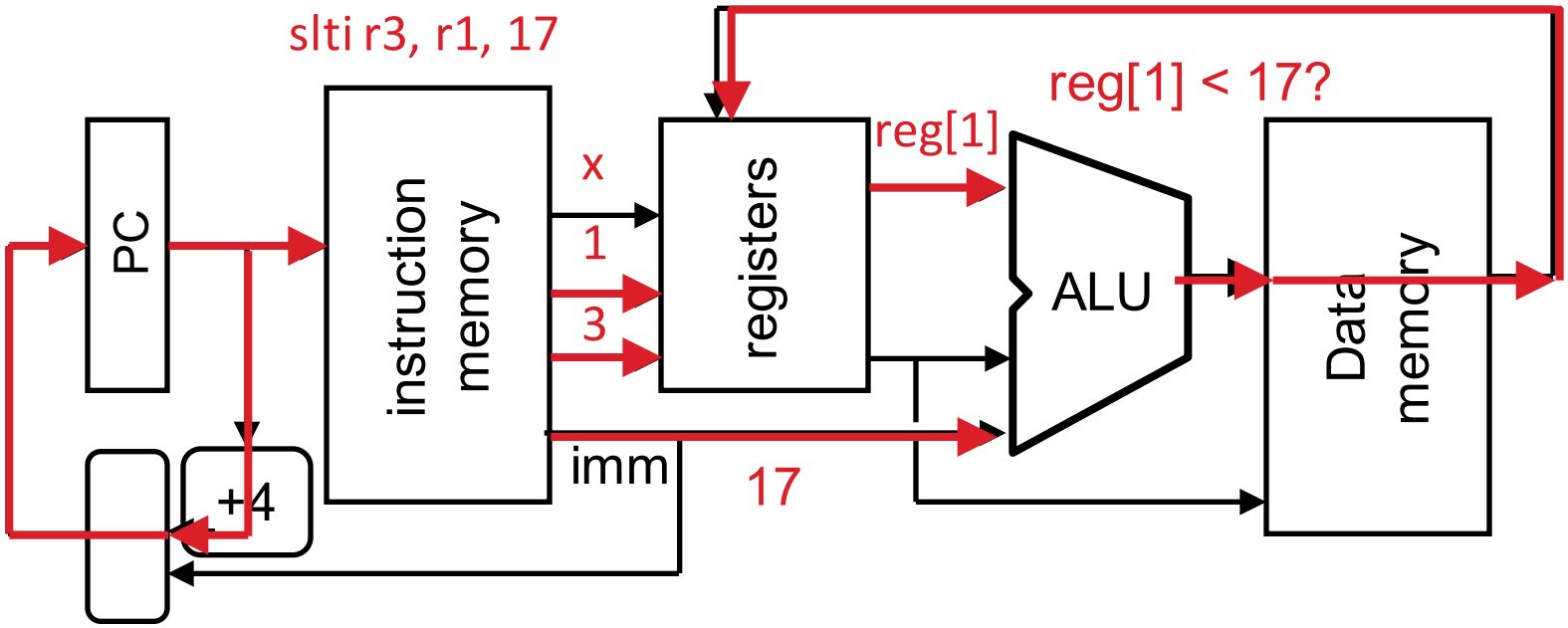
Example: add Instruction



Datapath Walkthroughs (2/3)

- slti $r3,$r1,17
  # if (r1 <17) r3 = 1 else r3 = 0
  - Stage 1: fetch this instruction, increment PC
  - Stage 2: decode to determine it is an slti, then read register $r1
  - Stage 3: compare value retrieved in Stage 2 with the integer 17
  - Stage 4: idle
  - Stage 5: write the result of Stage 3 (1 if reg source was less than signed immediate, 0 otherwise) into register $r3

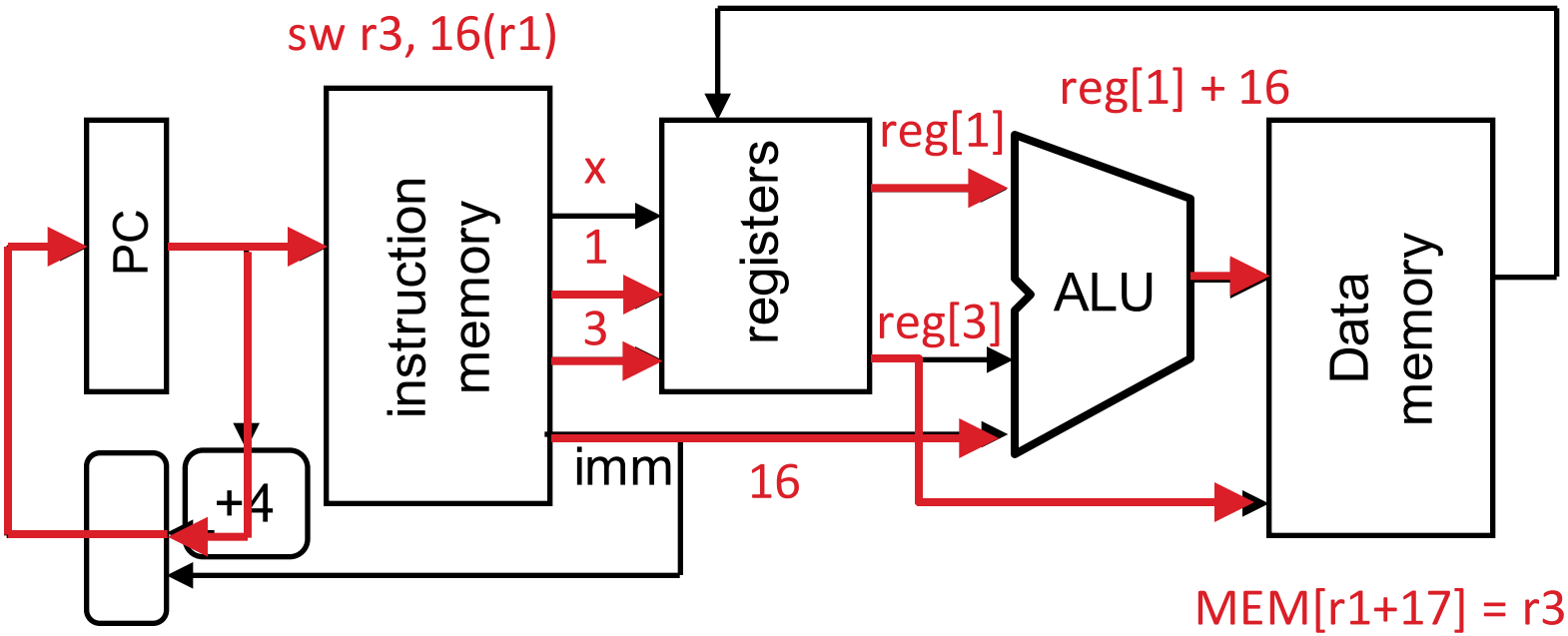
Example: slti Instruction



Datapath Walkthroughs (3/3)

- sw $r3,16($r1) # Mem[r1+16]=r3
  - Stage 1: fetch this instruction, increment PC
  - Stage 2: decode to determine it is a sw, then read registers $r1 and $r3
  - Stage 3: add 16 to value in register $r1 (retrieved in Stage 2) to compute address
  - Stage 4: write value in register $r3 (retrieved in Stage 2) into memory address computed in Stage 3
  - Stage 5: idle (nothing to write into a register)

Example: sw Instruction



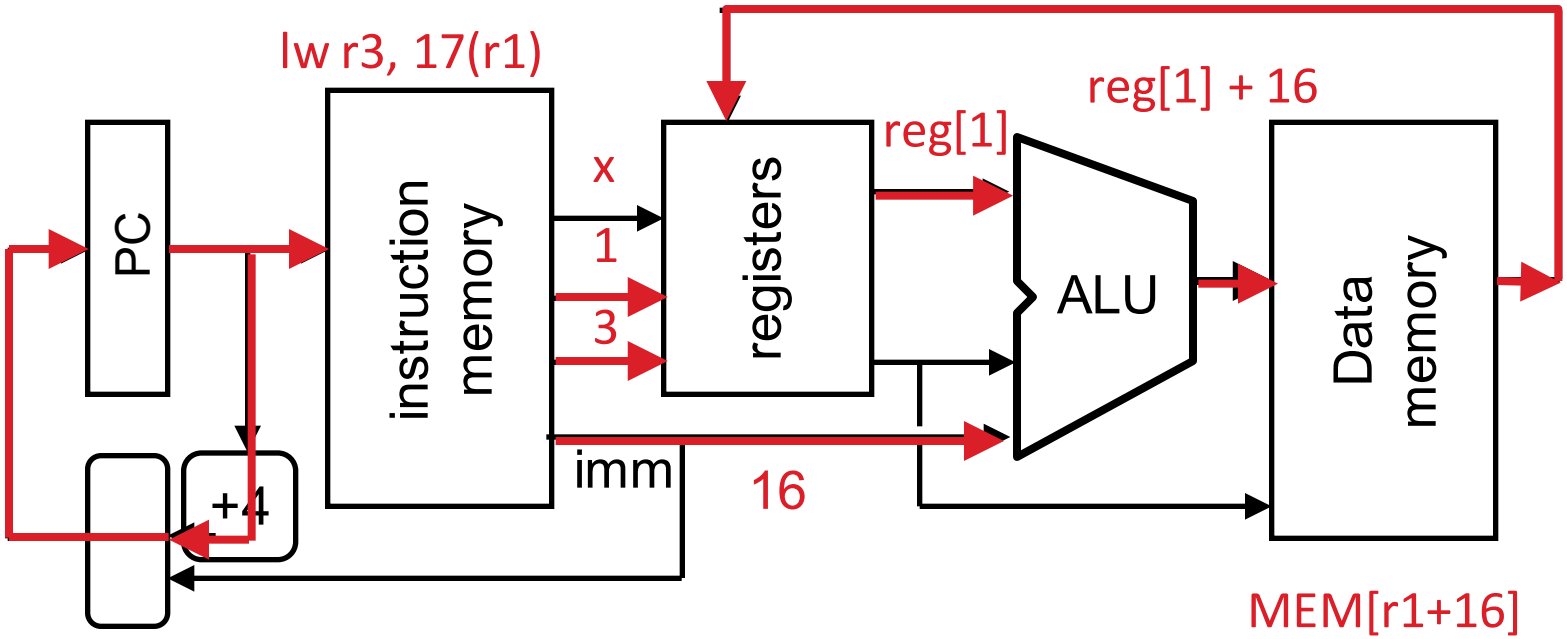
Why Five Stages? (1/2)

- Could we have a different number of stages?
  - Yes, other ISAs have different natural number of stages
    - And these days, pipelining can be much more aggressive than the "natural" 5 stages MIPS uses
- Why does MIPS have five if instructions tend to idle for at least one stage?
  - Five stages are the union of all the operations needed by all the instructions.
  - One instruction uses all five stages: the load

Why Five Stages? (2/2)

- lw $r3,16($r1) # r3=Mem[r1+16]
  - Stage 1: fetch this instruction, increment PC
  - Stage 2: decode to determine it is a lw, then read register $r1
  - Stage 3: add 16 to value in register $r1 (retrieved in Stage 2)
  - Stage 4: read value from memory address computed in Stage 3
  - Stage 5: write value read in Stage 4 into register $r3

Example: lw Instruction



Clickers/Peer Instruction

- Which type of MIPS instruction is active in the fewest stages?

A: LW

B: BEQ

C: J

D: JAL

E: ADDU

Processor Design: 5 steps

Step 1: Analyze instruction set to determine datapath requirements

- Meaning of each instruction is given by register transfers
- Datapath must include storage element for ISA registers
- Datapath must support each register transfer

Step 2: Select set of datapath components & establish clock methodology

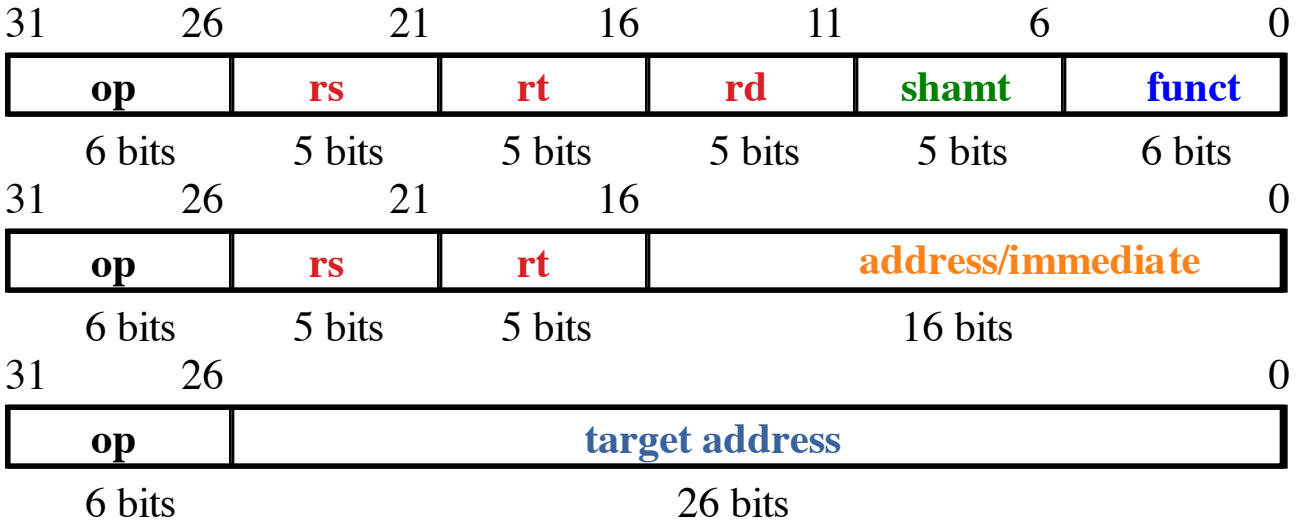
Step 3: Assemble datapath components that meet the requirements

Step 4: Analyze implementation of each instruction to determine setting of control points that realizes the register transfer

Step 5: Assemble the control logic

The MIPS Instruction Formats

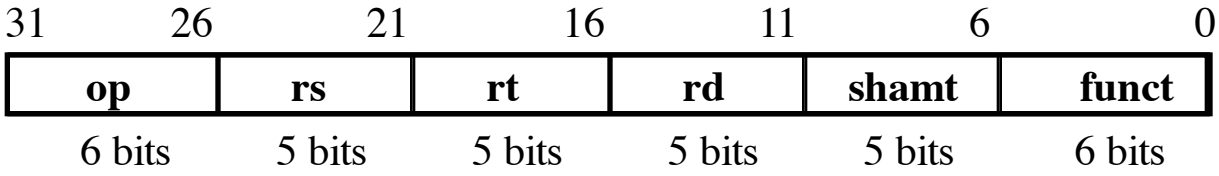
- All MIPS instructions are 32 bits long. 3 formats:
  - R-type
  - I-type
  - J-type



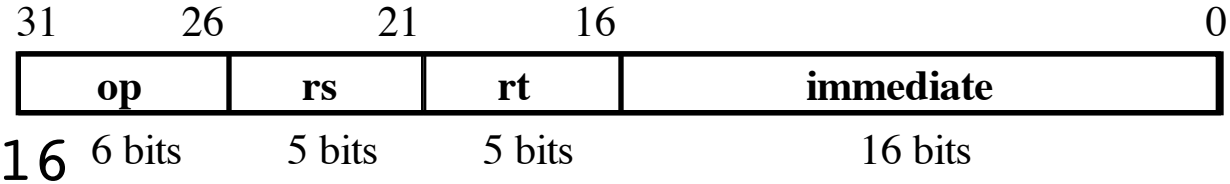
- The different fields are:
  - op: operation ("opcode") of the instruction
  - rs, rt, rd: the source and destination register specifiers
  - shamt: shift amount
  - funct: selects the variant of the operation in the "op" field
  - address / immediate: address offset or immediate value
  - target address: target address of jump instruction

The MIPS-lite Subset

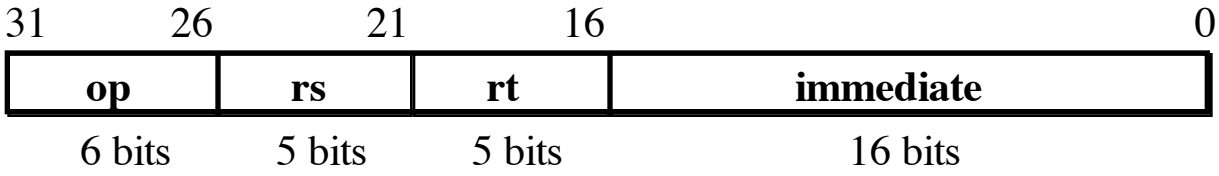
- ADDU and SUBU
  - `addu rd,rs,rt`
  - `subu rd,rs,rt`



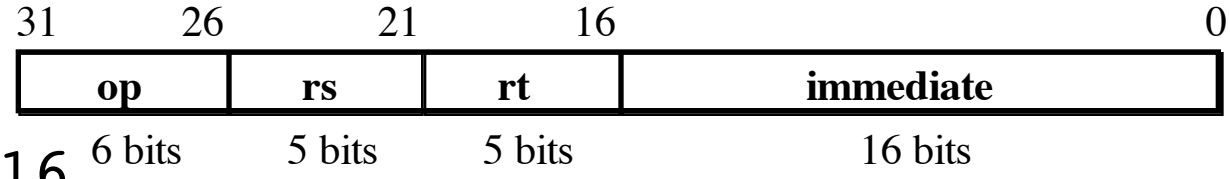
- OR Immediate:
  - `ori rt,rs,imm16`



- LOAD and STORE Word
  - `lw rt,rs,imm16`
  - `sw rt,rs,imm16`



- BRANCH:
  - `beq rs,rt,imm16`



Register Transfer Level (RTL)

- Colloquially called "Register Transfer Language"
- RTL gives the meaning of the instructions
- All start by fetching the instruction itself

```
{op , rs , rt , rd , shamt , funct} ← MEM[ PC ]

{op , rs , rt ,   Imm16} ← MEM[ PC ]
```

Inst	Register Transfers
ADDU	R[rd] ← R[rs] + R[rt]; PC ← PC + 4
SUBU	R[rd] ← R[rs] – R[rt]; PC ← PC + 4
ORI	R[rt] ← R[rs] | zero_ext(Imm16); PC ← PC + 4
LOAD	R[rt] ← MEM[R[rs] + sign_ext(Imm16)]; PC ← PC + 4
STORE	MEM[R[rs] + sign_ext(Imm16)] ← R[rt]; PC ← PC + 4
BEQ	if (R[rs] == R[rt]) PC ← PC + 4 + {sign_ext(Imm16), 2'b00} else PC ← PC + 4

In Conclusion

- “Divide and Conquer” to build complex logic blocks from smaller simpler pieces (adder)
- Five stages of MIPS instruction execution
- Mapping instructions to datapath components
- Single long clock cycle per instruction