

CS 61C:

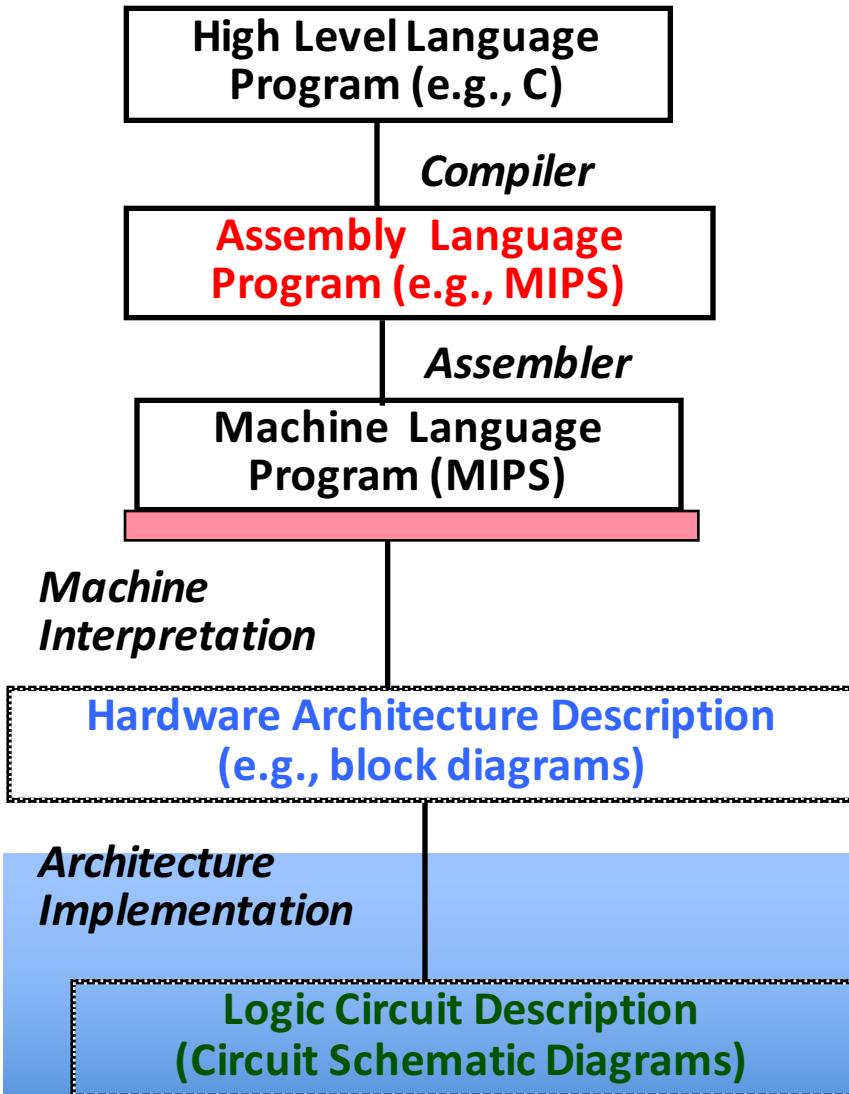
Great Ideas in Computer Architecture  
*Hardware intro, Digital Logic*

Instructors:

Nicholas Weaver & Vladimir Stojanovic

<http://inst.eecs.Berkeley.edu/~cs61c/sp16>

# Levels of Representation/Interpretation

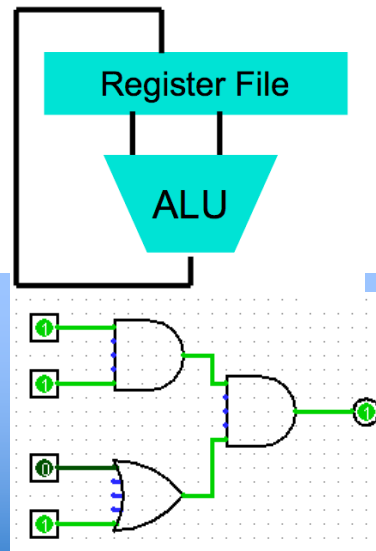


```
temp = v[k];
v[k] = v[k+1];
v[k+1] = temp;
```

```
lw $t0, 0($2)
lw $t1, 4($2)
sw $t1, 0($2)
sw $t0, 4($2)
```

Anything can be represented as a *number*, i.e., data or instructions

```
0000 1001 1100 0110 1010 1111 0101 1000
1010 1111 0101 1000 0000 1001 1100 0110
1100 0110 1010 1111 0101 1000 0000 1001
0101 1000 0000 1001 1100 0110 1010 1111
```



# Hardware Design

- Next several weeks: how a modern processor is built, starting with basic elements as building blocks
- Why study hardware design?
  - Understand capabilities and limitations of HW in general and processors in particular
  - What processors can do fast and what they can't do fast (avoid slow things if you want your code to run fast!)
  - Background for more in-depth HW courses (EECS 151, CS 152)
  - Hard to know what you'll need for next 30 years
  - There is only so much you can do with standard processors: you may need to design own custom HW for extra performance
    - Even some commercial processors today have customizable hardware!

# Synchronous Digital Systems

*Hardware of a processor, such as the MIPS, is an example of a Synchronous Digital System*

## *Synchronous:*

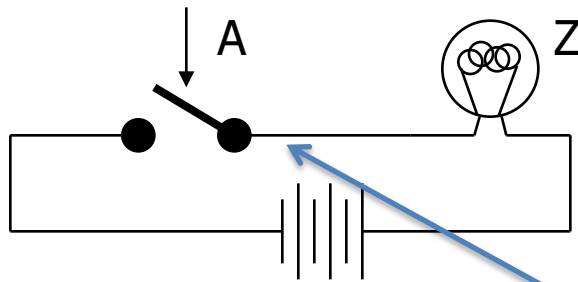
- All operations coordinated by a central clock
  - “Heartbeat” of the system!

## *Digital:*

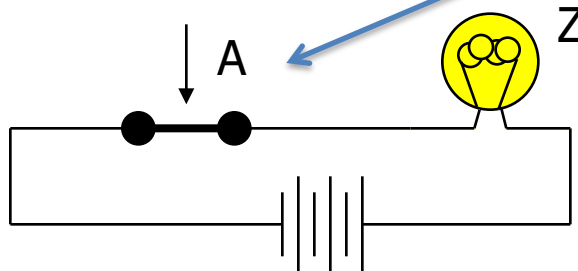
- Represent all values by discrete values
- Two binary digits: 1 and 0
- Electrical signals are treated as 1's and 0's
  - 1 and 0 are complements of each other
- High /low voltage for true / false, 1 / 0

# Switches: Basic Element of Physical Implementations

- Implementing a simple circuit (arrow shows action if wire changes to “1” or is *asserted*):



*On*-switch (if A is “1” or asserted) turns-on light bulb (Z)

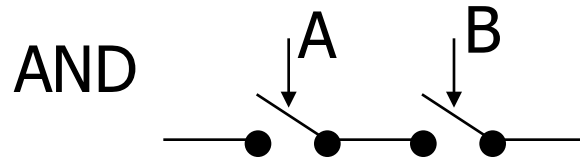


*Off*-switch (if A is “0” or unasserted) turns-off light bulb (Z)

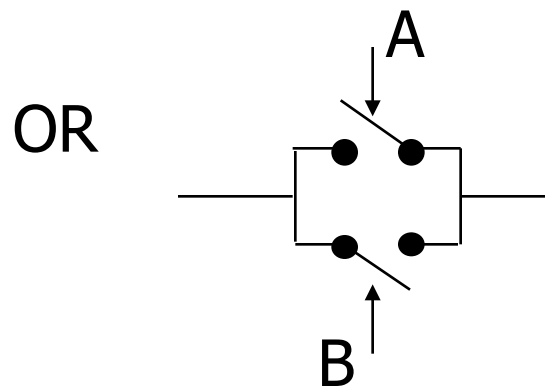
$$Z \equiv A$$

# Switches (cont'd)

- Compose switches into more complex ones (Boolean functions):



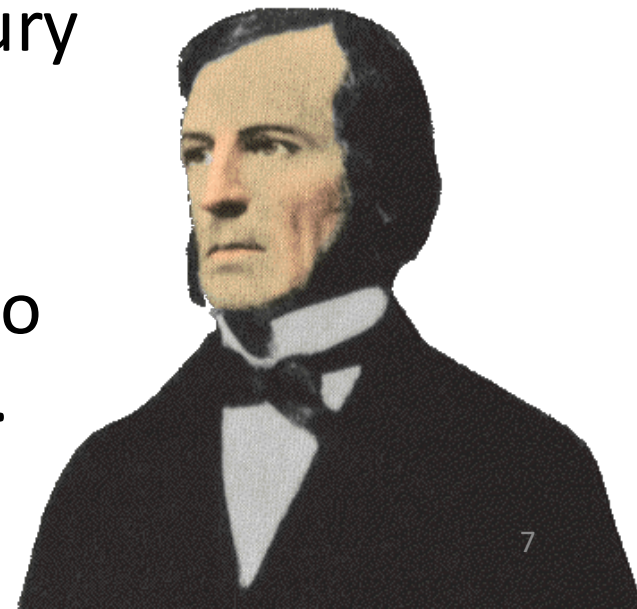
$$Z \equiv A \text{ and } B$$



$$Z \equiv A \text{ or } B$$

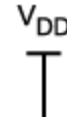
# Historical Note

- Early computer designers built ad hoc circuits from switches
- Began to notice common patterns in their work: ANDs, ORs, ...
- Master's thesis (by Claude Shannon, 1940) made link between work and 19<sup>th</sup> Century Mathematician George Boole
  - Called it “Boolean” in his honor
- Could apply math to give theory to hardware design, minimization, ...



# Transistors

- High voltage ( $V_{dd}$ ) represents 1, or true
  - In modern microprocessors,  $V_{dd} \sim 1.0$  Volt
- Low voltage (0 Volt or Ground) represents 0, or false
- Pick a midpoint voltage to decide if a 0 or a 1
  - Voltage greater than midpoint = 1
  - Voltage less than midpoint = 0
  - This removes noise as signals propagate – a big advantage of digital systems over analog systems
- If one switch can control another switch, we can build a computer!
- Our switches: CMOS transistors

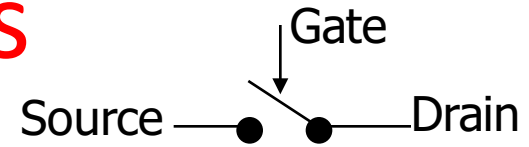




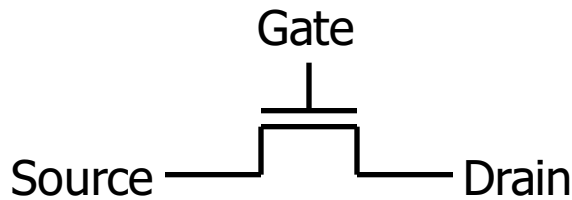
# CMOS Transistor Networks

- Modern digital systems designed in CMOS
  - MOS: Metal-Oxide on Semiconductor
  - C for complementary: use *pairs* of normally-*on* and normally-*off* switches
- CMOS transistors act as voltage-controlled switches
  - Similar, though easier to work with, than electro-mechanical relay switches from earlier era
  - Use energy primarily when switching

# CMOS Transistors



- Three terminals: source, gate, and drain
  - Switch action:  
if voltage on gate terminal is (some amount) higher/lower than source terminal then conducting path established between drain and source terminals (switch is closed)

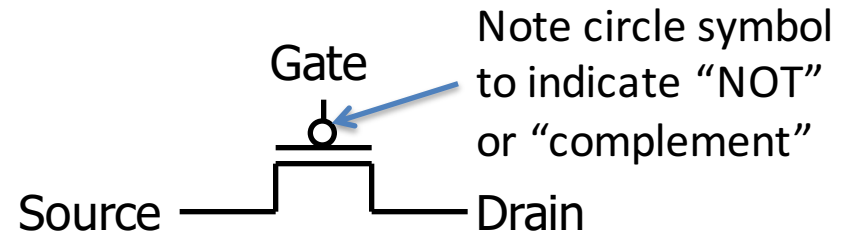


*n-channel transistor*

**off** when voltage at Gate is low

**on** when:

voltage(Gate) > voltage (Threshold)



*p-channel transistor*

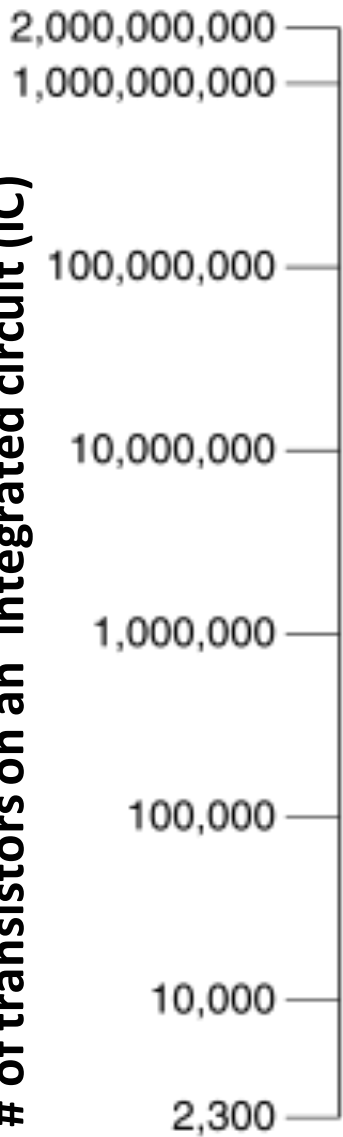
**on** when voltage at Gate is low

**off** when:

voltage(Gate) > voltage (Threshold)

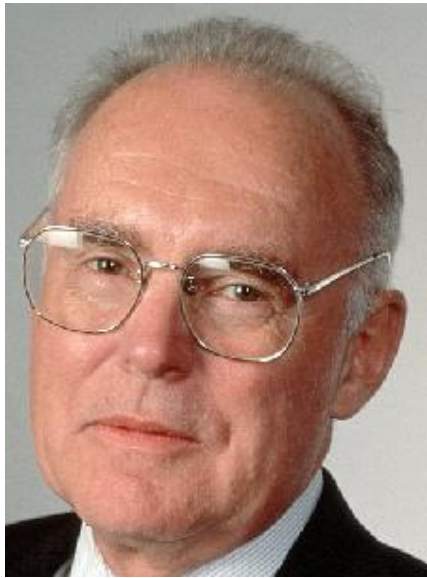
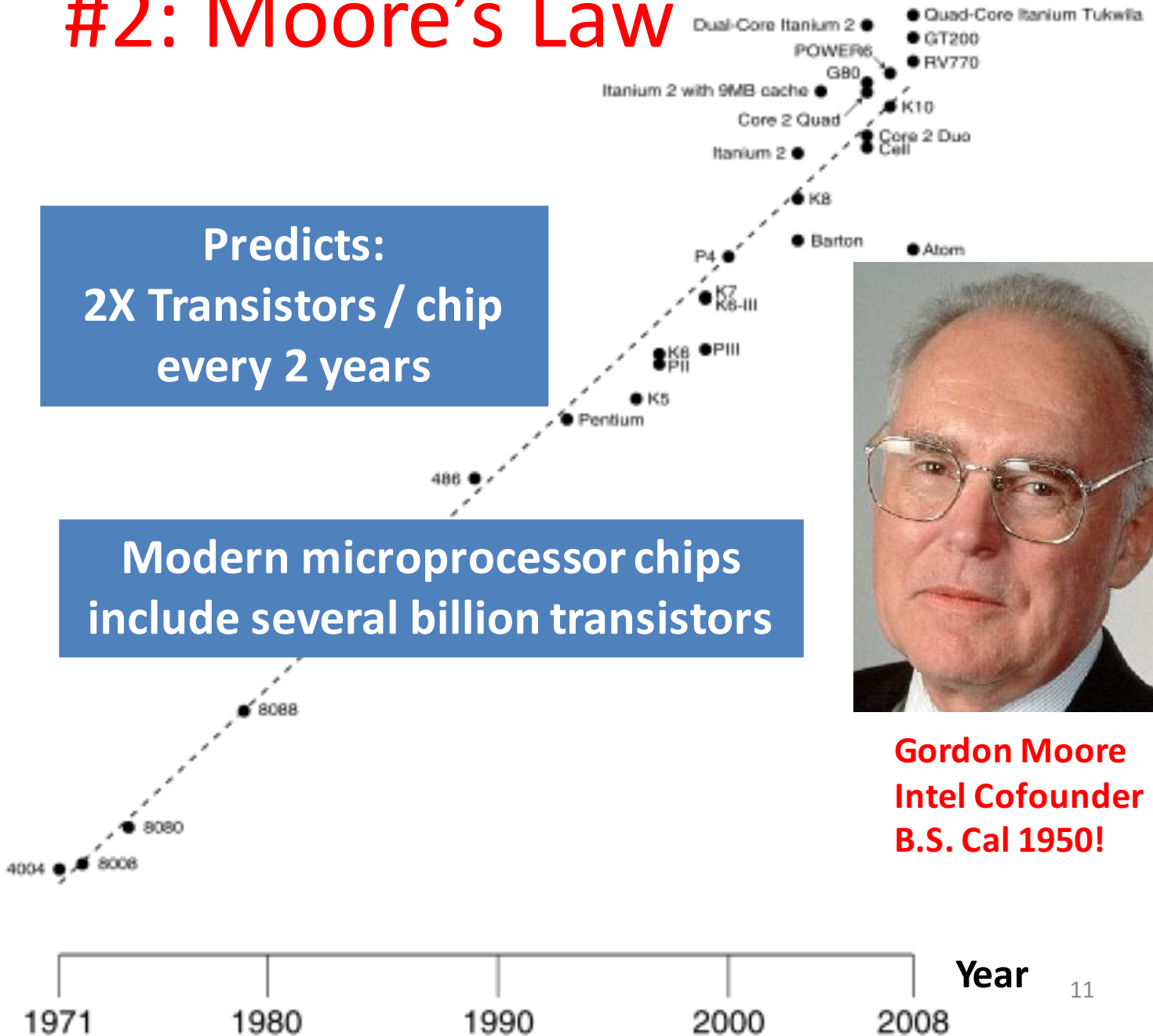
# #2: Moore's Law

# of transistors on an integrated circuit (IC)



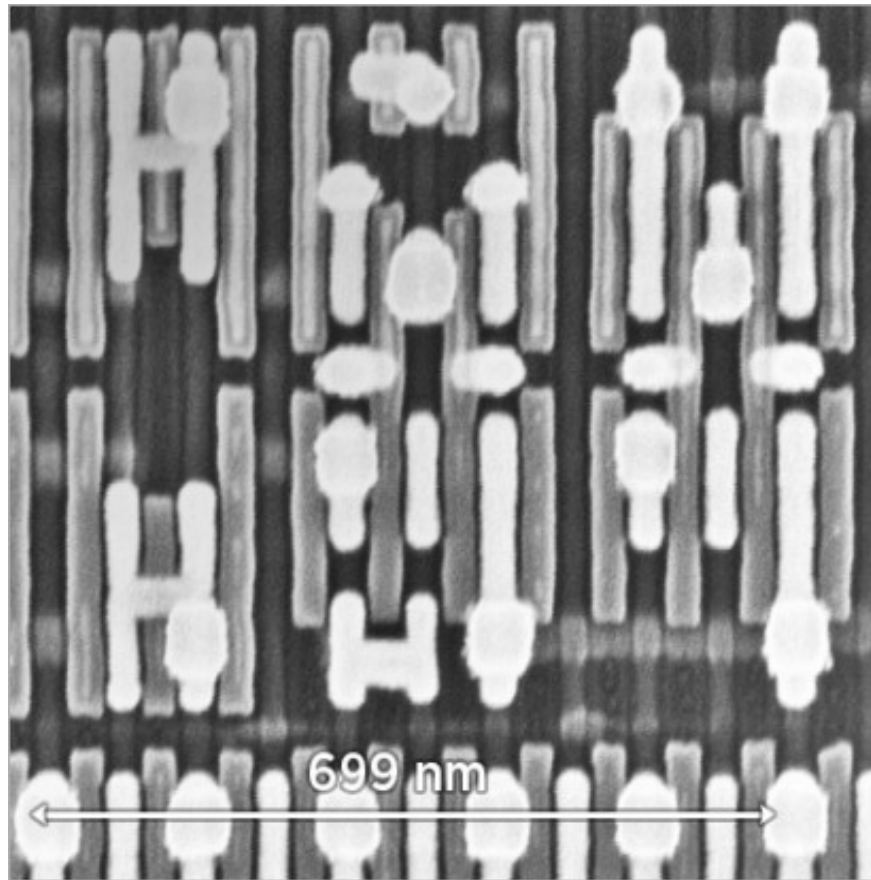
Predicts:  
2X Transistors / chip  
every 2 years

Modern microprocessor chips  
include several billion transistors

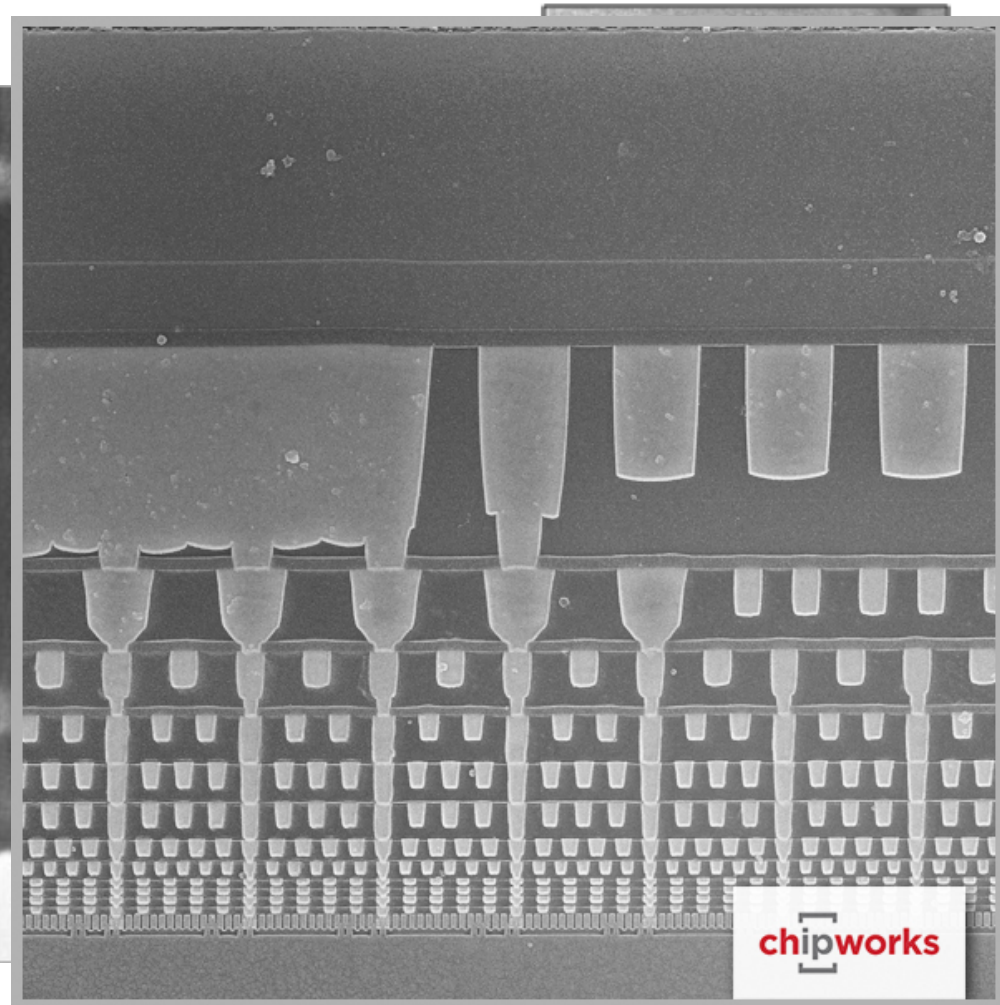


**Gordon Moore**  
**Intel Cofounder**  
**B.S. Cal 1950!**

# Intel 14nm Technology



Plan view of transistors



Side view of wiring layers

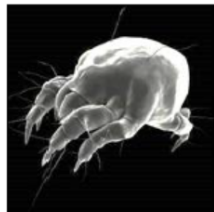
# Sense of Scale



Mark  
1.66 m



Fly  
7 mm



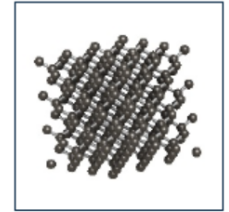
Mite  
300  $\mu\text{m}$



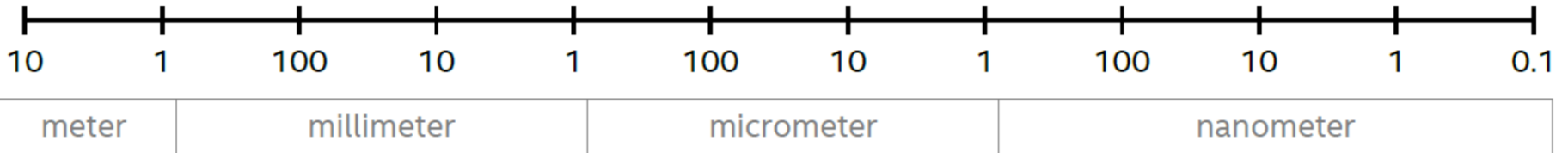
Blood Cell  
7  $\mu\text{m}$



Virus  
100 nm



Silicon Atom  
0.24 nm



Source: Mark Bohr, IDF14

# CMOS Circuit Rules

- Don't pass weak values => Use Complementary Pairs
  - N-type transistors pass weak 1's ( $V_{dd} - V_{th}$ )
  - N-type transistors pass strong 0's (ground)
  - Use N-type transistors only to pass 0's (N for negative)
  - Converse for P-type transistors: Pass weak 0s, strong 1s
    - Pass weak 0's ( $V_{th}$ ), strong 1's ( $V_{dd}$ )
    - Use P-type transistors only to pass 1's (P for positive)
  - Use pairs of N-type and P-type to get strong values
- Never leave a wire undriven
  - Make sure there's always a path to  $V_{dd}$  or GND
- Never create a path from  $V_{dd}$  to GND (ground)
  - This would short-circuit the power supply!

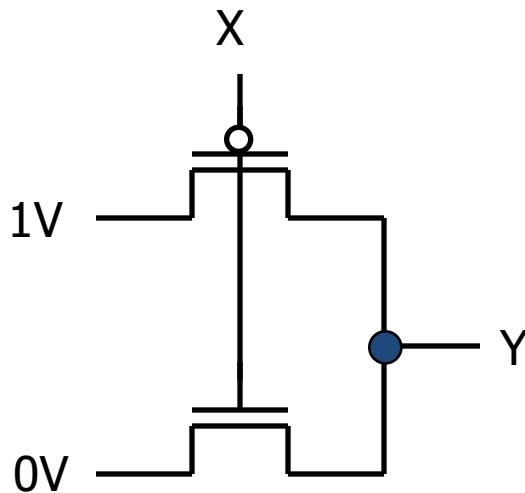
# CMOS Networks

*p-channel transistor*

on when voltage at Gate is low

off when:

voltage(Gate) > voltage (Threshold)



*n-channel transistor*

off when voltage at Gate is low

on when:

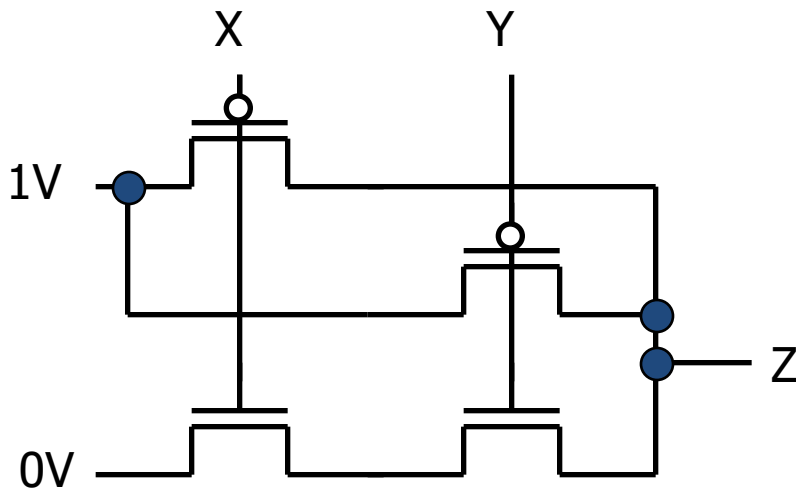
voltage(Gate) > voltage (Threshold)

what is the relationship between x and y?

x	y
0 Volt (GND)	1 Volt (Vdd)
1 Volt (Vdd)	0 Volt (GND)

Called an *inverter* or *not gate*

# Two-Input Networks



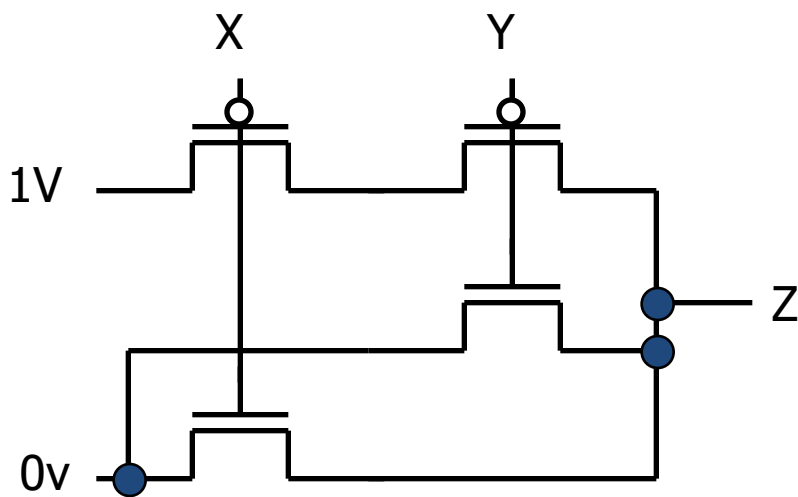
what is the relationship between x, y and z?

x	y	z
0 Volt	0 Volt	1 Volt
0 Volt	1 Volt	1 Volt
1 Volt	0 Volt	1 Volt
1 Volt	1 Volt	0 Volt

Called a *NAND gate*  
(*NOT AND*)



# Clickers/Peer Instruction



x	y	z				
		A	B	C	D	
0 Volt	0 Volt	0	0	1	1	Volts
0 Volt	1 Volt	0	1	0	1	Volts
1 Volt	0 Volt	0	1	0	1	Volts
1 Volt	1 Volt	1	1	0	0	Volts

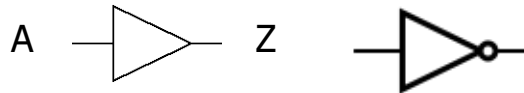
# Administrivia

- Proj2-1 due Sunday 2/21!
- MT1 next **Thursday** night
  - If you are in DSP or have an exam conflict, you should have received an email from Fred. If not, email Fred and William.
  - EE16B students will take it at the normal time
  - We will post room assignments on Piazza over the weekend
- Proj2-2 will be released late next week.

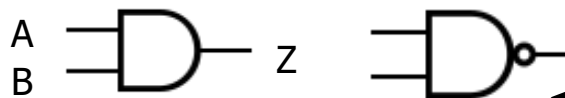
# Combinational Logic Symbols

- Common combinational logic systems have standard symbols called logic gates

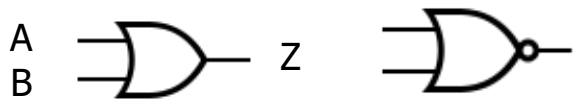
- Buffer, NOT



- AND, NAND



- OR, NOR



Inverting versions (NOT, NAND, NOR) easiest to implement with CMOS transistors (the switches we have available and use most)

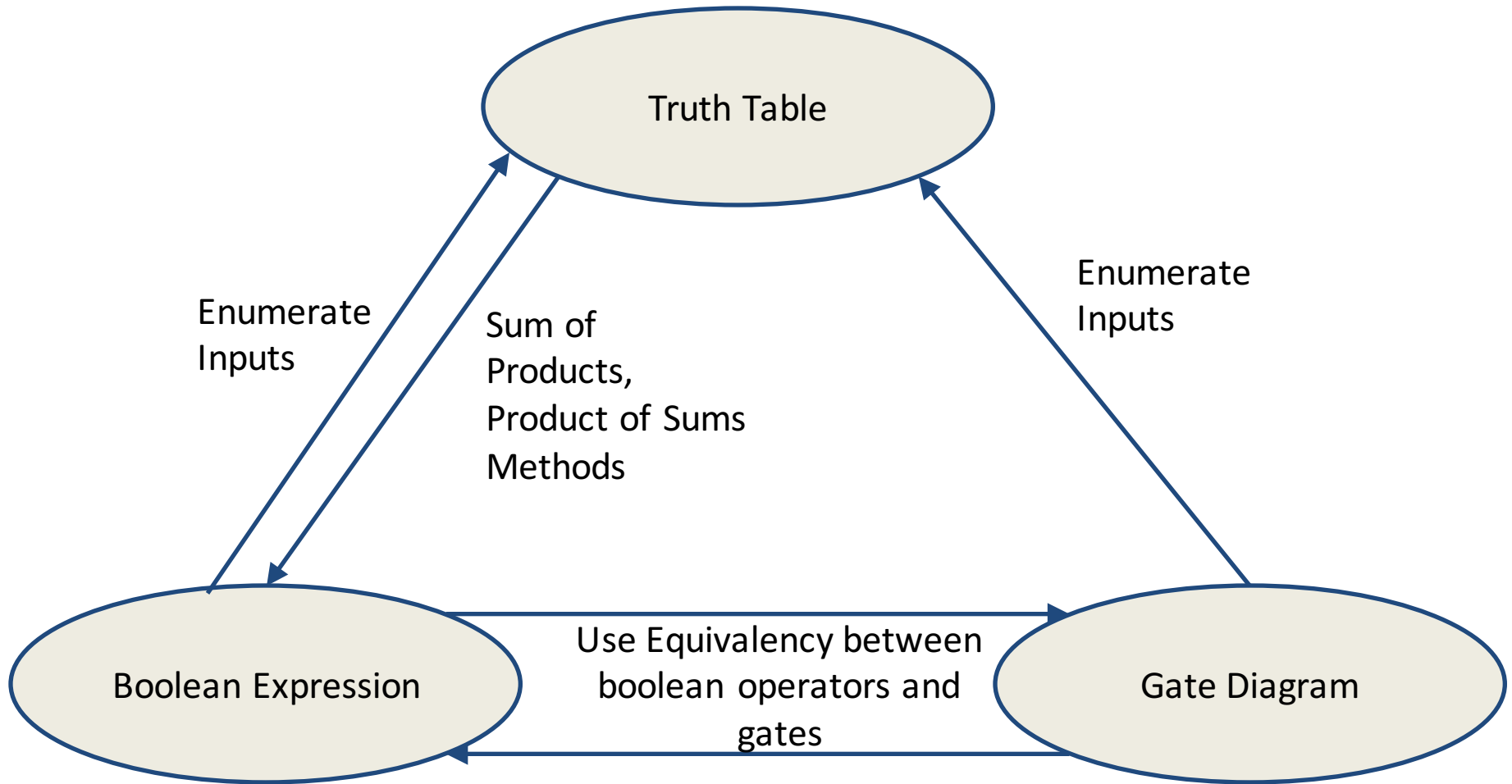
# Boolean Algebra

- Use plus “+” for OR
  - “logical sum”
- Use product for AND ( $a \bullet b$  or implied via  $ab$ )
  - “logical product”
- “Hat” to mean complement (NOT)
- Thus

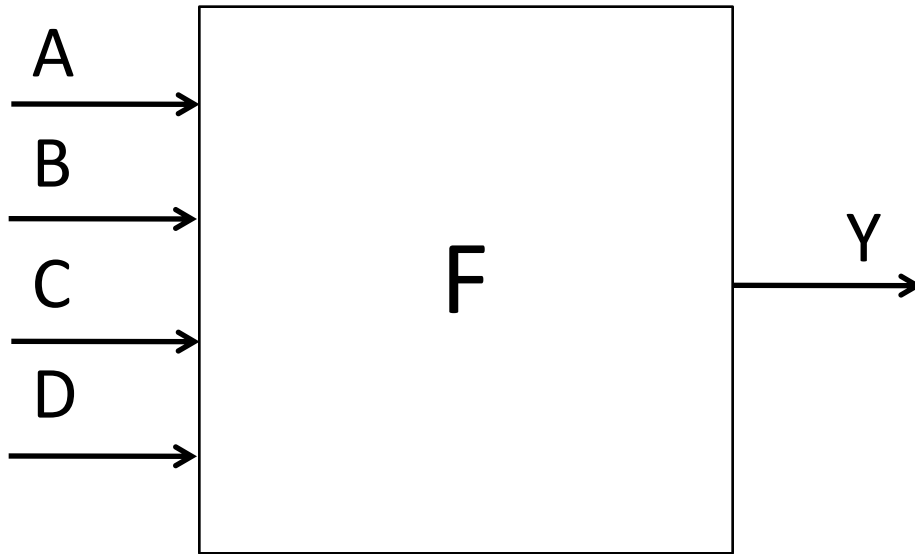
$$\begin{aligned} & ab + a + \bar{c} \\ = & a \bullet b + a + \bar{c} \\ = & (a \text{ AND } b) \text{ OR } a \text{ OR } (\text{NOT } c) \end{aligned}$$



# Representations of Combinational Logic (groups of logic gates)



# Truth Tables for Combinational Logic



Exhaustive list of the output value  
generated for each combination of inputs

How many logic functions can be defined  
with N inputs?

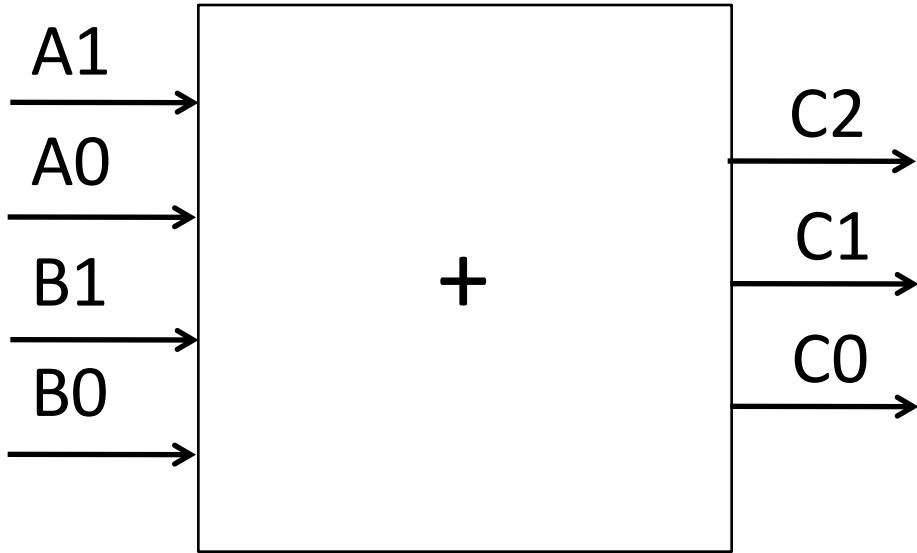
a	b	c	d	y
0	0	0	0	F(0,0,0,0)
0	0	0	1	F(0,0,0,1)
0	0	1	0	F(0,0,1,0)
0	0	1	1	F(0,0,1,1)
0	1	0	0	F(0,1,0,0)
0	1	0	1	F(0,1,0,1)
0	1	1	0	F(0,1,1,0)
0	1	1	1	F(0,1,1,1)
1	0	0	0	F(1,0,0,0)
1	0	0	1	F(1,0,0,1)
1	0	1	0	F(1,0,1,0)
1	0	1	1	F(1,0,1,1)
1	1	0	0	F(1,1,0,0)
1	1	0	1	F(1,1,0,1)
1	1	1	0	F(1,1,1,0)
1	1	1	1	F(1,1,1,1)

# Truth Table Example #1:

$y = F(a,b)$ : 1 iff  $a \neq b$

<b>a</b>	<b>b</b>	<b>y</b>
<b>0</b>	<b>0</b>	<b>0</b>
<b>0</b>	<b>1</b>	<b>1</b>
<b>1</b>	<b>0</b>	<b>1</b>
<b>1</b>	<b>1</b>	<b>0</b>

# Truth Table Example #2: 2-bit Adder



How  
Many  
Rows?

A	B	C
$a_1a_0$	$b_1b_0$	$c_2c_1c_0$



# Truth Table Example #3: 32-bit Unsigned Adder

A	B	C
000 ... 0	000 ... 0	000 ... 00
000 ... 0	000 ... 1	000 ... 01
.	.	.
.	.	.
.	.	.
111 ... 1	111 ... 1	111 ... 10

How  
Many  
Rows?

# Truth Table Example #4: 3-input Majority Circuit

$Y =$

This is called *Sum of Products* form;  
Just another way to represent the TT  
as a logical expression

More simplified forms  
(fewer gates and wires)

a	b	c	y
0	0	0	0
0	0	1	0
0	1	0	0
0	1	1	1
1	0	0	0
1	0	1	1
1	1	0	1
1	1	1	1

# And in Conclusion, ...

- Multiple Hardware Representations
  - Analog voltages quantized to represent logic 0 and logic 1
  - Transistor switches form gates: AND, OR, NOT, NAND, NOR
  - Truth table mapped to gates for combinational logic design
  - Boolean algebra for gate minimization