“The application for Introduction to Mathematical Thinking, a 2-unit DeCal that aims to develop mathematical maturity and prepare students for CS 70, is now live! Go to http://apply.imt-decal.org. Applications are due on Friday, August 31st.

In order to help make CS 70 more accessible, we’re starting Introduction to Mathematical Thinking, a 2-unit DeCal meant to expose students to some ideas and concepts in discrete mathematics before they’re tested on them in CS 70. The course will cover topics such as proof techniques, set theory, number theory and combinatorics. We’ve worked with professors that have taught CS 70 to pick these specific topics.

Check out the full list of topics, along with the FAQs, at the course website: http://imt-decal.org.”
Public-Service Announcement II

“ASUC Senator Chow is looking for applicants to intern in her office this year. Interns could choose from a variety of committees (Publications/Media, UC Berkeley Club Recruitment Portal Development, Christian Committee, etc.), adding resume experience and becoming ingratiated in a positive community driving change on campus.

Applications can be found here: tinyurl.com/SenatorChowApp

For students interested in CS opportunities specifically, Senator Chow’s office is working to develop a platform similar to a LinkedIn on campus for club recruitment and extracurricular communication. As such, we need front-end coders and designers as well as back end coders.”
Labs: We are forgiving during the first week or so, but try to get your lab1 submitted by Thursday night. DBC: Let us know if you can’t get something to work!

In particular, there are almost 60 people who have accounts but do not have Git repositories. You cannot hand anything in without the latter, so do get this part of the lab done!

Likewise, there are about 950 students with accounts, which is substantially less than the enrollment + waitlist. You must have an account to have a repo, which you need to turn things in!

This class is crowded, so I may very well start dropping people who appear not to be doing the labs and homework.

We do not encourage signing up for classes with conflicting lectures, although there is a way to seek an exception. You will have a final conflict if you have a lecture conflict; we do not consider such conflicts as valid grounds to take an alternative final.
More Iteration: Sort an Array

Problem. Print out the command-line arguments in lexicographic order:

% java sort the quick brown fox jumped over the lazy dog
brown dog fox jumped lazy over quick the the

Plan.

public class Sort {
    /** Sort and print WORDS lexicographically. */
    public static void main(String[] words) {
        sort(words, 0, words.length-1);
        print(words);
    }

    /** Sort items A[L..U], with all others unchanged. */
    static void sort(String[] A, int L, int U) { /* "TOMORROW" */ }

    /** Print A on one line, separated by blanks. */
    static void print(String[] A) { /* "TOMORROW" */ }
}
How do We Know If It Works?

• **Unit testing** refers to the testing of individual units (methods, classes) within a program, rather than the whole program.

• In this class, we mainly use the JUnit tool for unit testing.

• Example: AGTestYear.java in lab #1.

• **Integration testing** refers to the testing of entire (integrated) set of modules—the whole program.

• In this course, we’ll look at various ways to run the program against prepared inputs and checking the output.

• **Regression testing** refers to testing with the specific goal of checking that fixes, enhancements, or other changes have not introduced faults (regressions).
Test-Driven Development

- Idea: write tests first.
- Implement unit at a time, run tests, fix and refactor until it works.
- We’re not really going to push it in this course, but it is useful and has quite a following.
Testing sort

• This is pretty easy: just give a bunch of arrays to sort and then make sure they each get sorted properly.

• Have to make sure we cover the necessary cases:
  - *Corner cases.* E.g., empty array, one-element, all elements the same.
  - *Representative “middle” cases.* E.g., elements reversed, elements in order, one pair of elements reversed, . . . .
Simple JUnit

- The JUnit package provides some handy tools for unit testing.
- The Java annotation `@Test` on a method tells the JUnit machinery to call that method.
- (An **annotation** in Java provides information about a method, class, etc., that can be examined within Java itself.)
- A collection of methods with names beginning with `assert` then allow your test cases to check conditions and report failures.
- [See example.]
Selection Sort

/** Sort items A[L..U], with all others unchanged. */
static void sort(String[] A, int L, int U) {
    if (L < U) {
        int k = /*( Index s.t. A[k] is largest in A[L],...,A[U] )*/;
        /*{ Sort items L to U-1 of A. }*/;
    }
}

And we're done! Well, OK, not quite.
Selection Sort

/** Sort items A[L..U], with all others unchanged. */
static void sort(String[] A, int L, int U) {
    if (L < U) {
        int k = indexOfLargest(A, L, U);
        /* { Sort items L to U-1 of A. }*/;
    }
}

/** Index k, I0<=k<=I1, such that V[k] is largest element among
 * V[I0], ... V[I1]. Requires I0<=I1. */
static int indexOfLargest(String[] V, int i0, int i1) {
    ...
}
Selection Sort

/** Sort items A[L..U], with all others unchanged. */
static void sort(String[] A, int L, int U) {
    if (L < U) {
        int k = indexOfLargest(A, L, U);
        sort(A, L, U-1);  // Sort items L to U-1 of A
    }
}

/** Index k, IO<=k<=I1, such that V[k] is largest element among 
 * V[I0], ... V[I1]. Requires I0<=I1. */
static int indexOfLargest(String[] V, int i0, int i1) {
    ...
}
Selection Sort

/** Sort items A[L..U], with all others unchanged. */
static void sort(String[] A, int L, int U) {
    if (L < U) {
        int k = indexOfLargest(A, L, U);
        sort(A, L, U-1); // Sort items L to U-1 of A
    }
}

/** Index k, I0<=k<=I1, such that V[k] is largest element among */
/** V[I0], ... V[I1]. Requires I0<=I1. */
static int indexOfLargest(String[] V, int i0, int i1) {
    ...
}
Selection Sort

/** Sort items A[L..U], with all others unchanged. */
static void sort(String[] A, int L, int U) {
    if (L < U) {
        int k = indexOfLargest(A, L, U);
        sort(A, L, U-1); // Sort items L to U-1 of A
    }
}

What would an iterative version look like?

    while (?) {
        ?
    }
Selection Sort

/** Sort items A[L..U], with all others unchanged. */
static void sort(String[] A, int L, int U) {
    if (L < U) {
        int k = indexOfLargest(A, L, U);
        sort(A, L, U-1);  // Sort items L to U-1 of A
    }
}

Iterative version:

while (L < U) {
    int k = indexOfLargest(A, L, U);
    U -= 1;
}
Find Largest

/** Index k, I0<=k<=I1, such that V[k] is largest element among V[I0], ... V[I1]. Requires I0<=I1. */
static int indexOfLargest(String[] V, int i0, int i1) {
    if (?) return i1;
    else {
        return i1;
    }
}
Find Largest

/** Index k, i0<=k<=i1, such that V[k] is largest element among
 * V[i0], ... V[i1]. Requires i0<=i1. */
static int indexOfLargest(String[] V, int i0, int i1) {
    if (i0 >= i1)
        return i1;
    else /* if (i0 < i1) */ {
        // Code block
    }
}
/** Index k, I0<=k<=I1, such that V[k] is largest element among * V[I0], ... V[I1]. Requires I0<=I1. */
static int indexOfLargest(String[] V, int i0, int i1) {
    if (i0 >= i1)
        return i1;
    else /* if (i0 < i1) */ {
        int k = /*( index of largest value in V[i0 + 1..i1] )*/;
        return /*( whichever of i0 and k has larger value )*/;
    }
}
/** Index \( k, I_0 \leq k \leq I_1 \), such that \( V[k] \) is largest element among
* \( V[I_0], \ldots, V[I_1] \). Requires \( I_0 \leq I_1 \). */

```java
static int indexOfLargest(String[] V, int i0, int i1) {
    if (i0 >= i1)
        return i1;
    else /* if (i0 < i1) */ {
        int k = indexOfLargest(V, i0 + 1, i1);
        return /*( whichever of \( i_0 \) and \( k \) has larger value )*/;
    }
}
```
Find Largest

/** Index k, I0<=k<=I1, such that V[k] is largest element among * V[I0], ... V[I1]. Requires I0<=I1. */
static int indexOfLargest(String[] V, int i0, int i1) {
  if (i0 >= i1)
    return i1;
  else /* if (i0 < i1) */ {
    int k = indexOfLargest(V, i0 + 1, i1);
    return (V[i0].compareTo(V[k]) > 0) ? i0 : k;
    // if (V[i0].compareTo(V[k]) > 0) return i0; else return k;
  }
}

• Turning this into an iterative version is tricky: not tail recursive.
• What are the arguments to compareTo the first time it’s called?
Iteratively Find Largest

/** Value k, I0<=k<=I1, such that V[k] is largest element among * V[I0], ... V[I1]. Requires I0<=I1. */
static int indexOfLargest(String[] V, int i0, int i1) {
    if (i0 >= i1)
        return i1;
    else /* if (i0 < i1) */ {
        int k = indexOfLargest(V, i0 + 1, i1);
        return (V[i0].compareTo(V[k]) > 0) ? i0 : k;
        // if (V[i0].compareTo(V[k]) > 0) return i0; else return k;
    }
}

Iterative:

int i, k;
    k = ?;  // Deepest iteration
for (i = ?; ...?; i ...) { 
    k = ?;
return k;
Iteratively Find Largest

/** Value k, I0<=k<=I1, such that V[k] is largest element among * V[I0], ... V[I1]. Requires I0<=I1. */
static int indexOfLargest(String[] V, int i0, int i1) {
    if (i0 >= i1)
        return i1;
    else /* if (i0 < i1) */ {
        int k = indexOfLargest(V, i0 + 1, i1);
        return (V[i0].compareTo(V[k]) > 0) ? i0 : k;
        // if (V[i0].compareTo(V[k]) > 0) return i0; else return k;
    }
}

Iterative:

int i, k;
    k = i1;       // Deepest iteration
    for (i = ?; ...?; i ...?)
        k = ?;
    return k;
Iteratively Find Largest

/** Value k, I0<=k<=I1, such that V[k] is largest element among * V[I0], ... V[I1]. Requires I0<=I1. */
static int indexOfLargest(String[] V, int i0, int i1) {
    if (i0 >= i1)
        return i1;
    else /* if (i0 < i1) */ {
        int k = indexOfLargest(V, i0 + 1, i1);
        return (V[i0].compareTo(V[k]) > 0) ? i0 : k;
    }
}

Iterative:

int i, k;

k = i1;  // Deepest iteration
for (i = i1 - 1; i >= i0; i -= 1)
    k = ?;
return k;
Iteratively Find Largest

/** Value k, I0<=k<=I1, such that V[k] is largest element among * V[I0], ... V[I1]. Requires I0<=I1. */
static int indexOfLargest(String[] V, int i0, int i1) {
    if (i0 >= i1)
        return i1;
    else /* if (i0 < i1) */ {
        int k = indexOfLargest(V, i0 + 1, i1);
        return (V[i0].compareTo(V[k]) > 0) ? i0 : k;
    }
}

Iterative:

int i, k;

k = i1; // Deepest iteration
for (i = i1 - 1; i >= i0; i -= 1)
    k = (V[i].compareTo(V[k]) > 0) ? i : k;
return k;
Finally, Printing

/** Print A on one line, separated by blanks. */
static void print(String[] A) {
    for (int i = 0; i < A.length; i += 1)
        System.out.print(A[i] + " ");
    System.out.println();
}

/* J2SE 5 introduced a new syntax for the for loop here: */
for (String s : A)
    System.out.print(s + " ");
/* Use it if you like, but let’s not stress over it yet! */
Another Problem

Given an array of integers, A, of length \( N > 0 \), find the smallest index, \( k \), such that all elements at indices \( \geq k \) and \( < N - 1 \) are greater than \( A[N - 1] \). Then rotate elements \( k \) to \( N - 1 \) right by one. For example, if \( A \) starts out as

\[
\{ 1, 9, 4, 3, 0, 12, 11, 9, 15, 22, 12 \}
\]

then it ends up as

\[
\{ 1, 9, 4, 3, 0, 12, 11, 9, 12, 15, 22 \}
\]

As another example,

\[
\{ 1, 9, 4, 3, 0, 12, 11, 9, 15, 22, -2 \}
\]

would become

\[
\{ -2, 1, 9, 4, 3, 0, 12, 11, 9, 15, 22 \}
\]
public class Shove {

    /** Rotate elements A[k] to A[A.length-1] one element to the right, where k is the smallest index such that elements k through A.length-2 are all larger than A[A.length-1]. */
    static void moveOver(int[] A) {
        // FILL IN
    }
}
