CS61B Lecture #34

Administrivia:

• Project due Tuesday night.

• Autograder running with preliminary test sets.

Today's Readings: Graph Structures: DSIJ, Chapter 12

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• Examples:

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Some Terminology

- A graph consists of
 - A set of nodes (aka vertices)
 - A set of edges: pairs of nodes.
 - Nodes with an edge between are adjacent.
 - Depending on problem, nodes or edges may have labels (or weights)
- ullet Typically call node set $V = \{v_0, \ldots\}$, and edge set E.
- If the edges have an order (first, second), they are directed edges, and we have a directed graph (digraph), otherwise an undirected graph.
- Edges are incident to their nodes.
- Directed edges exit one node and enter the next.
- A cycle is a path without repeated edges leading from a node back to itself (following arrows if directed).
- A graph is cyclic if it has a cycle, else acyclic. Abbreviation: Directed Acyclic Graph—DAG.

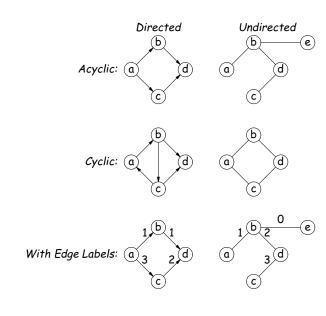
Some Pictures

Why Graphs?

• For expressing non-hierarchically related items

Networks: pipelines, roads, assignment problemsRepresenting processes: flow charts, Markov models

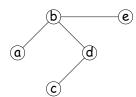
- Representing partial orderings: PERT charts, makefiles

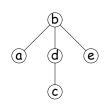


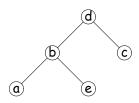
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Trees are Graphs

- A graph is connected if there is a (possibly directed) path between every pair of nodes.
- That is, if one node of the pair is reachable from the other.
- A DAG is a (rooted) tree iff connected, and every node but the root has exactly one parent.
- A connected, acyclic, undirected graph is also called a *free tree*. Free: we're free to pick the root; e.g.,







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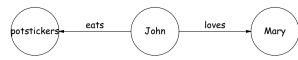
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• Edge = Begat

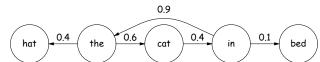
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More Examples

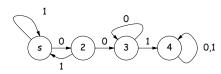
• Edge = some relationship



• Edge = next state might be (with probability)



• Edge = next state in state machine, label is triggering input. (Start at s. Being in state 4 means "there is a substring '001' somewhere in the input".)



Representation

Examples of Use

200

• Edge = Must be completed before; Node label = time to complete.

Chicago

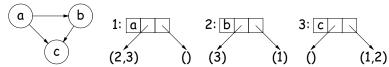
Sleep

8 hrs

George

• Edge = Connecting road, with length.

- Often useful to number the nodes, and use the numbers in edges.
- Edge list representation: each node contains some kind of list (e.g., linked list or array) of its successors (and possibly predecessors).



• Edge sets: Collection of all edges. For graph above:

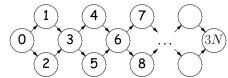
Martin

$$\{(1,2),(1,3),(2,3)\}$$

• Adjacency matrix: Represent connection with matrix entry:

Traversing a Graph

- Many algorithms on graphs depend on traversing all or some nodes.
- Can't quite use recursion because of cycles.
- Even in acyclic graphs, can get combinatorial explosions:



Treat 0 as the root and do recursive traversal down the two edges out of each node: $\Theta(2^N)$ operations!

• So typically try to visit each node constant # of times (e.g., once).

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