CS61B Lecture #24

Today:

• Priority queues (Data Structures §6.4, §6.5)

• Range queries (§6.2)

• Java utilities: SortedSet, Map, etc.

Next topic: Hashing (Data Structures Chapter 7).

Heaps

- A max-heap is a binary tree that enforces the
 Heap Property: Both labels in both children of each node are
 less than node's label.
- So node at top has largest label.
- Looser than binary search property, which allows us to keep tree "bushy".
- That is, it's always valid to put the smallest nodes anywhere at the bottom of the tree.
- Thus, heaps can be made *nearly complete*: all but possibly the last row have as many keys as possible.
- ullet As a result, insertion of new value and deletion of largest value always take time proportional to $\lg N$ in worst case.
- A min-heap is basically the same, but with the minimum value at the root and children having larger values than their parents.

Priority Queues, Heaps

- Priority queue: defined by operations "add," "find largest," "remove largest."
- Examples: scheduling long streams of actions to occur at various future times.
- Also useful for sorting (keep removing largest).
- Common implementation is the heap, a kind of tree.
- (Confusingly, this same term is used to described the pool of storage that the **new** operator uses. Sorry about that.)

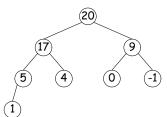
Last modified: Fri Oct 24 12:53:07 2014 C561B: Lecture #24 2

Example: Inserting into a simple heap

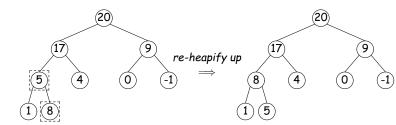
Data:

1 17 4 5 9 0 -1 20

Initial Heap:

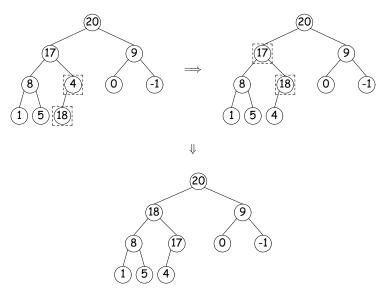


Add 8: Dashed boxes show where heap property violated



Heap insertion continued

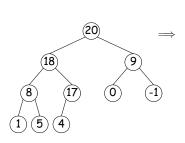
Now insert 18:



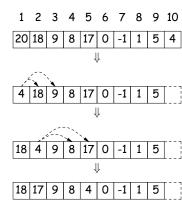
Last modified: Fri Oct 24 12:53:07 2014 CS61B: Lecture #24 5

Heaps in Arrays

- Since heaps are nearly complete (missing items only at bottom level), can use arrays for compact representation.
- Example of removal from last slide (dashed arrows show children):

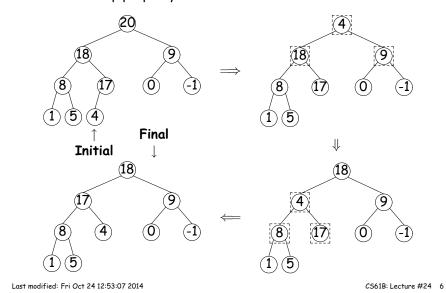


Nodes stored in level order. Children of node at index #K are in 2K and 2K+1



Removing Largest from Heap

To remove largest: Move bottommost, rightmost node to top, then re-heapify down as needed (swap offending node with larger child) to re-establish heap property.

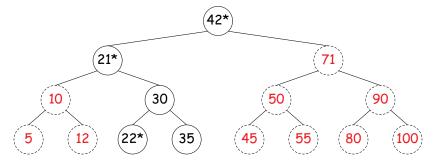


Ranges

- So far, have looked for specific items
- But for BSTs, need an ordering anyway, and can also support looking for ranges of values.
- Example: perform some action on all values in a BST that are within some range (in natural order):

Time for Range Queries

- Time for range query $\in O(h+M)$, where h is height of tree, and M is number of data items that turn out to be in the range.
- \bullet Consider searching the tree below for all values, x , such that $25 \leq x < 40.$
- ullet In this example, the h comes from the starred nodes; the M comes from other non-dashed nodes. Dashed nodes are never looked at.



Last modified: Fri Oct 24 12:53:07 2014 CS61B: Lecture #24 9

Example of Representation: BSTSet

- Use binary search tree to represent set. Can use same representation for both BSTSet and its subsets.
- Each set has pointer to BST, plus bounds (if any).
- In this representation, size is rather expensive!

Ordered Sets and Range Queries in Java

- Class SortedSet supports range queries with views of set:
 - S.headSet(U): subset of S that is < U.
 - S.tailSet(L): subset that is $\geq L$.
 - S. subSet (L, U): subset that is \geq L, < U.
- Changes to views modify S.
- Attempts to, e.g., add to a headSet beyond U are disallowed.
- Can iterate through a view to process a range:

 Java library type TreeSet<T> requires either that T be Comparable, or that you provide a Comparator:

SortedSet<String> rev_fauna = new TreeSet<String> (Collections.reverseOrder());

Last modified: Fri Oct 24 12:53:07 2014 CS61B: Lecture #24 10