CS61B Lecture #22

Today: Backtracking searches, game trees (DSIJ, Section 6.5)

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Searching by "Generate and Test"

- We've been considering the problem of searching a set of data stored in some kind of data structure: "Is $x \in S$?"
- \bullet But suppose we don't have a set S, but know how to recognize what we're after if we find it: "Is there an x such that P(x)?"
- If we know how to enumerate all possible candidates, can use approach of Generate and Test: test all possibilities in turn.
- Can sometimes be more clever: avoid trying things that won't work, for example.
- What happens if the set of possible candidates is infinite?

Backtracking Search

- Backtracking search is one way to enumerate all possibilities.
- Example: Knight's Tour. Find all paths a knight can travel on a chessboard such that it touches every square exactly once and ends up one knight move from where it started.
- In the example below, the numbers indicate position numbers (knight starts at 0).
- Here, knight (N) is stuck; how to handle this?

6						
		5				
4	7					
	10		2			
8	3	0				
N		9		1		

General Recursive Algorithm

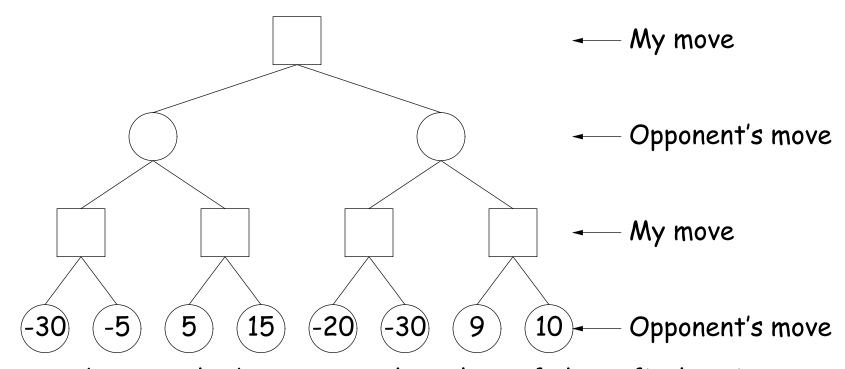
```
/** Append to PATH a sequence of knight moves starting at ROW, COL
  that avoids all squares that have been hit already and
   that ends up one square away from ENDROW, ENDCOL. B[i][j] is
  true iff row i and column j have been hit on PATH so far.
 * Returns true if it succeeds, else false (with no change to PATH).
 * Call initially with PATH containing the starting square, and
   the starting square (only) marked in B. */
boolean findPath (boolean[][] b, int row, int col,
                  int endRow, int endCol, List path) {
  if (path.size () == 64) return isKnightMove (row, col, endRow, endCol);
  for (r, c = all possible moves from (row, col)) {
    if (! b[r][c]) {
     b[r][c] = true; // Mark the square
     path.add (new Move (r, c));
      if (findPath (b, r, c, endRow, endCol, path)) return true;
     b[r][c] = false; // Backtrack out of the move.
     path.remove (path.size ()-1);
  return false;
}
```

Another Kind of Search: Best Move

- Consider the problem of finding the best move in a two-person game.
- One way: assign a value to each possible move and pick highest.
 - Example: number of our pieces number of opponent's pieces.
- But this is misleading. A move might give us more pieces, but set up a devastating response from the opponent.
- So, for each move, look at opponent's possible moves, assume he picks the best one for him, and use that as the value.
- But what if you have a great response to his response?
- How do we organize this sensibly?

Game Trees

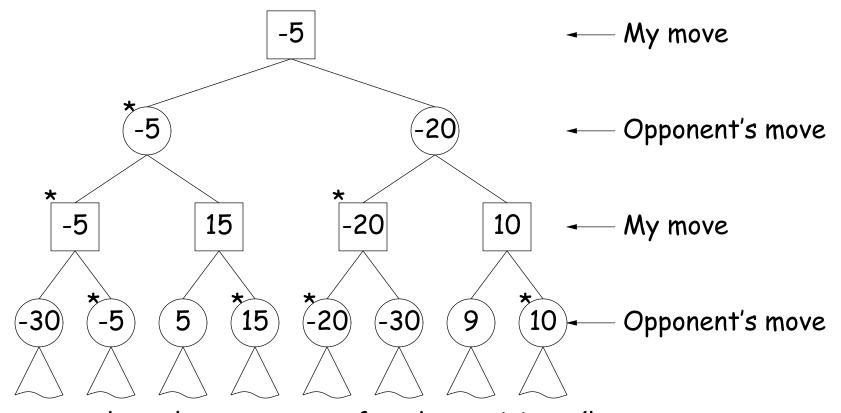
- Think of the space of possible continuations of the game as a tree.
- Each node is a position, each edge a move.



- Suppose numbers at the bottom are the values of those final positions to me. Smaller numbers are of more value to my opponent.
- What should I move? What value can I get if my opponent plays as well as possible?

Game Trees, Minimax

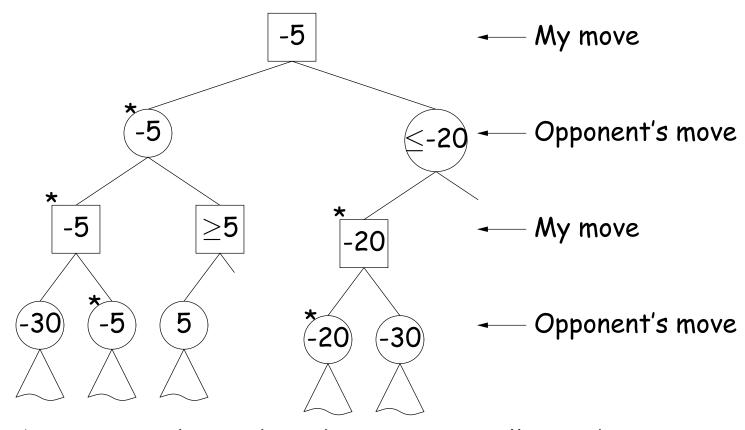
- Think of the space of possible continuations of the game as a tree.
- Each node is a position, each edge a move.



- Numbers are the values we guess for the positions (larger means better for me). Starred nodes would be chosen.
- I always choose child (next position) with maximum value; opponent chooses minimum value ("Minimax algorithm")

Alpha-Beta Pruning

We can prune this tree as we search it.



- ullet At the ' ≥ 5 ' position, I know that the opponent will not choose to move here (since he already has a -5 move).
- \bullet At the ' ≤ -20 ' position, my opponent knows that I will never choose to move here (since I already have a -5 move).

Cutting off the Search

- If you could traverse game tree to the bottom, you'd be able to force a win (if it's possible).
- Sometimes possible near the end of a game.
- Unfortunately, game trees tend to be either infinite or impossibly large.
- So, we choose a maximum depth, and use a heuristic value computed on the position alone (called a static valuation) as the value at that depth.
- Or we might use iterative deepening (kind of breadth-first search), and repeat the search at increasing depths until time is up.
- Much more sophisticated searches are possible, however (take CS188).

Some Pseudocode for Searching

```
/** A legal move for WHO that either has an estimated value >= CUTOFF
   or that has the best estimated value for player WHO, starting from
   position START, and looking up to DEPTH moves ahead.
Move findBestMove (Player who, Position start, int depth, double cutoff)
  if (start is a won position for who) return WON_GAME; /* Value \infty */
  else if (start is a lost position for who) return LOST_GAME; /* Value -\infty */
  else if (depth == 0) return guessBestMove (who, start, cutoff);
  Move bestSoFar = REALLY_BAD_MOVE;
  for (each legal move, M, for who from position start) {
    Position next = start.makeMove (M):
    Move response = findBestMove (who.opponent (), next,
                                    depth-1, -bestSoFar.value ());
    if (-response.value () > bestSoFar.value ()) {
      Set M's value to -response.value (); // Value for who = - Value for opponent
      bestSoFar = M;
      if (M.value () >= cutoff) break;
  return bestSoFar;
```

Static Evaluation

 This leaves static evaluation, which looks just at the next possible move:

```
Move guessBestMove (Player who, Position start, double cutoff)
  Move bestSoFar;
  bestSoFar = Move.REALLY_BAD_MOVE;
  for (each legal move, M, for who from position start) {
    Position next = start.makeMove (M);
    Set M's value to heuristic guess of value to who of next;
    if (M.value () > bestSoFar.value ()) {
      bestSoFar = M;
      if (M.value () >= cutoff)
        break;
    }
  return bestSoFar;
}
```