CS61B Lecture #26	Back to Simple Search: Hashing			
Test #2: Wednesday, 7 November in class.	 Linear search is OK for small data sets, bad for large. 			
Today: Hashing (Data Structures Chapter 7).	 So linear search would be OK if we could rapidly narrow the search to a few items. 			
Next topic: Sorting (Data Structures Chapter 8).	 Suppose that in constant time could put any item in our data set into a numbered bucket, where # buckets stays within a constant factor of # keys. 			
	 Suppose also that buckets contain roughly equal numbers of keys. 			
	• Then search would be constant time.			
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Hash functions	External chaining			
 To do this, must have way to convert key to bucket number: a hash function. Example: N = 200 data items. keys are longs, evenly spread over the range 02⁶³ - 1. Want to keep maximum search to L = 2 items. Use hash function h(K) = K%M, where M = N/L = 100 is the 	 Array of M buckets. Each bucket is a list of data items. 			
number of buckets: $0 \le h(K) < M$. - So 100232, 433, and 10002332482 go into different buckets, but 10, 400210, and 210 all go into the same bucket.	• Not all buckets have same length, but average is $N/M = L$, the load factor.			

• To work well, hash function must avoid *collisions*: keys that "hash" to equal values.

Open Addressing Filling the Table • To get (likely to be) constant-time lookup, need to keep #buckets • Idea: Put one data item in each bucket. within constant factor of #items. • When there is a collision, and bucket is full, just use another. • So resize table when load factor gets higher than some limit. • Various ways to do this: • In general, must re-hash all table items. - Linear probes: If there is a collision at h(K), try h(K)+m, h(K)+m2m, etc. (wrap around at end). Still, this operation constant time per item, - Quadratic probes: h(K) + m, $h(K) + m^2$, ... • So by doubling table size each time, get constant amortized time - Double hashing: h(K) + h'(K), h(K) + 2h'(K), etc. for insertion and lookup • Example: $h(K) = K \ M$, with M = 10, linear probes with m = 1. • (Assuming, that is, that our hash function is good). - Add 1, 2, 11, 3, 102, 9, 18, 108, 309 to empty table. 108 1 2 11 3 102 309 18 9 • Things can get slow, even when table is far from full. • Lots of literature on this technique, but Personally, I just settle for external chaining. CS61B: Lecture #26 5 CS61B: Lecture #26 6 Last modified: Wed Oct 24 15:03:36 2012 Last modified: Wed Oct 24 15:03:36 2012 Hash Functions: Other Data Structures I Hash Functions: Strings • Lists (ArrayList, LinkedList, etc.) are analogous to strings: e.g., • For String, " $s_0s_1\cdots s_{n-1}$ " want function that takes all characters and their positions into account. Java uses • What's wrong with $s_0 + s_1 + \ldots + s_{n-1}$? hashCode = 1; Iterator i = list.iterator(); while (i.hasNext()) { • For strings, Java uses Object obj = i.next(); $h(s) = s_0 \cdot 31^{n-1} + s_1 \cdot 31^{n-2} + \ldots + s_{n-1}$ hashCode =31*hashCode computed modulo 2^{32} as in Java int arithmetic. + (obj==null ? 0 : obj.hashCode()); • To convert to a table index in 0..N - 1, compute h(s)%N (but don't } use table size that is multiple of 31!) • Can limit time spent computing hash function by not looking at entire • Not as hard to compute as you might think; don't even need multiplilist. For example: look only at first few items (if dealing with a List cation! or SortedSet). int r; r = 0; • Causes more collisions, but does not cause equal things to go to diffor (int i = 0; i < s.length (); i += 1) ferent buckets. r = (r << 5) - r + s.charAt (i);

Hash Functions: Other Data S [.]	tructures II	What Java Provides			
 Recursively defined data structures ⇒ refunctions. For example, on a binary tree, one can use so hash(T): 		 In class Object, is function hashCode(). By default, returns address of this, or something similar. Can override it for your particular type. For reasons given on last slide, is overridden for type String, as well as many types in the Java library, like all kinds of List. 			
<pre>if (T == null) return 0;</pre>					
else return someHashFunction (T. + 255 * hash(T.left	())	 The types Hashtable, HashSet, and HashMap use hashCode to give you fast look-up of objects. 			
+ 255*255 * hash(T.r	ight ());	HashMap <keytype,valuetype> map =</keytype,valuetype>			
 Can use address of object ("hash on identi- jects are never considered equal. 	ry") if distinct (!=) ob-	<pre>new HashMap<keytype,valuetype> (approximate size, load fac- tor);</keytype,valuetype></pre>			
 But careful! Won't work for Strings, becaus be in different buckets: 	e .equal Strings could	<pre>map.put (key, value); // Map KEY -> VALUE. // VALUE last mapped to by SOMEKEY.</pre>			
<pre>String H = "Hello", S1 = H + ", world!", S2 = "Hello, world!";</pre>		<pre> map.get (someKey)</pre>			
• Here S1.equals(S2), but S1 != S2.		// Is SOMEKEY mapped?			
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Characteristics

- \bullet Assuming good hash function, add, lookup, deletion take $\Theta(1)$ time, amortized.
- Good for cases where one looks up equal keys.
- Usually bad for *range queries:* "Give me every name between Martin and Napoli." [Why?]
- But sometimes OK, if hash function is monotonic (i.e., when key $k_1 > k_2$, then $h(k_1) \ge h(k_2)$. For example,
 - Items are time-stamped records; key is the time.
 - Hashing function is to have one bucket for every hour.
- Hashing is probably not a good idea for small sets that you rapidly create and discard [why?]

Comparing Search Structures

Here, N is #items, k is #answers to query.

	Unordered	Sorted	Bushy Search	"Good" Hash	
Function	List	Array	Tree	Table	Heap
find	$\Theta(N)$	$\Theta(\lg N)$	$\Theta(\lg N)$	$\Theta(1)$	$\Theta(N)$
add	$\Theta(1)$	$\Theta(N)$	$\Theta(\lg N)$	$\Theta(1)$	$\Theta(\lg N)$
range query	$\Theta(N)$	$\Theta(k + \lg N)$	$\Theta(k+\lg N)$	$\Theta(N)$	$\Theta(N)$
find largest	$\Theta(N)$	$\Theta(1)$	$\Theta(\lg N)$	$\Theta(N)$	$\Theta(1)$
remove largest	$\Theta(N)$	$\Theta(1)$	$\Theta(\lg N)$	$\Theta(N)$	$\Theta(\lg N)$