CS61B Lecture #26		Back to Simple Search: Hashing			
<b>Today:</b> Hashing (Data Structures Chapter 7).		<ul> <li>Linear search is OK for small data sets, bad for large.</li> </ul>			
Next topic: Sorting (Data Structures Chapter 8).		<ul> <li>So linear search would be OK if we could rapidly narrow the search to a few items.</li> </ul>			
		<ul> <li>Suppose that in constant time could p a numbered bucket, where # buckets of # keys.</li> </ul>			
		• Suppose also that buckets contain roughly equal numbers of keys.			
		• Then search would be constant time.	<ul> <li>Then search would be constant time.</li> </ul>		
Last modified: Thu Oct 25 19:09:55 2007	CS61B: Lecture #26 1	Last modified: Thu Oct 25 19:09:55 2007	C561B: Lecture #26 2		
Hash functions		External cha	aining		
• To do this, must have way to convert key to bucket number: a <i>hash function</i> .		<ul> <li>Array of M buckets.</li> <li>Each bucket is a list of data items.</li> </ul>			
• Example:					
<ul> <li>N = 200 data items.</li> <li>keys are longs, evenly spread over the r</li> <li>Want to keep maximum search to L = 2</li> <li>Use hash function h(K) = K%M, when number of buckets: 0 ≤ h(K) &lt; M.</li> <li>So 100232, 433, and 10002332482 go but 10, 400210, and 210 all go into the s</li> </ul>	items. e $M = N/L = 100$ is the into different buckets,	• Not all buckets have same length, but	t average is $N/M = L$ , the load		

• To work well, hash function must avoid *collisions*: keys that "hash" to equal values.

factor.

## **Open Addressing** Filling the Table • To get (likely to be) constant-time lookup, need to keep #buckets • Idea: Put one data item in each bucket. within constant factor of #items. • When there is a collision, and bucket is full, just use another. • So resize table when load factor gets higher than some limit. • Various ways to do this: • In general, must re-hash all table items. - Linear probes: If there is a collision at h(K), try h(K)+m, h(K)+m2m, etc. (wrap around at end). Still, this operation constant time per item, - Quadratic probes: h(K) + m, $h(K) + m^2$ , ... • So by doubling table size each time, get constant amortized time - Double hashing: h(K) + h'(K), h(K) + 2h'(K), etc. for insertion and lookup • Example: $h(K) = K \ M$ , with M = 10, linear probes with m = 1. • (Assuming, that is, that our hash function is good). - Add 1, 2, 11, 3, 102, 9, 18, 108, 309 to empty table. 108 1 2 11 3 102 309 18 9 • Things can get slow, even when table is far from full. • Lots of literature on this technique, but Personally, I just settle for external chaining. CS61B: Lecture #26 5 CS61B: Lecture #26 6 Last modified: Thu Oct 25 19:09:55 2007 Last modified: Thu Oct 25 19:09:55 2007 Hash Functions: Other Data Structures I Hash Functions: Strings • Lists (ArrayList, LinkedList, etc.) are analogous to strings: e.g., • For String, " $s_0s_1\cdots s_{n-1}$ " want function that takes all characters and their positions into account. Java uses • What's wrong with $s_0 + s_1 + \ldots + s_{n-1}$ ? hashCode = 1; Iterator i = list.iterator(); while (i.hasNext()) { • For strings, Java uses Object obj = i.next(); $h(s) = s_0 \cdot 31^{n-1} + s_1 \cdot 31^{n-2} + \ldots + s_{n-1}$ hashCode =31\*hashCode computed modulo $2^{32}$ as in Java int arithmetic. + (obj==null ? 0 : obj.hashCode()); • To convert to a table index in 0..N - 1, compute h(s)%N (but don't } use table size that is multiple of 31!) • Can limit time spent computing hash function by not looking at entire • Not as hard to compute as you might think; don't even need multiplilist. For example: look only at first few items (if dealing with a List cation! or SortedSet). int r; r = 0; • Causes more collisions, but does not cause equal things to go to diffor (int i = 0; i < s.length (); i += 1) ferent buckets. r = (r << 5) - r + s.charAt (i);

Hash Functions: Other Data Structures II	What Java Provides			
<ul> <li>Recursively defined data structures ⇒ recursively defined hash functions.</li> <li>For example, on a binary tree, one can use something like hash(T): if (T == null) </li> </ul>	<ul> <li>In class Object, is function hashCode().</li> <li>By default, returns address of this, or something similar.</li> <li>Can override it for your particular type.</li> <li>For reasons given on last slide, is overridden for type String, as well as many types in the Java library, like all kinds of List.</li> </ul>			
return 0; else return someHashFunction (T.label ()) + 255 * hash(T.left ()) + 255*255 * hash(T.right ());	<ul> <li>The types Hashtable, HashSet, and HashMap use hashCode to give you fast look-up of objects.</li> <li>HashMap<keytype,valuetype> map = new HashMap<keytype,valuetype> (approximate size, load fac-</keytype,valuetype></keytype,valuetype></li> </ul>			
<ul> <li>Can use address of object ("hash on identity") if distinct (!=) objects are never considered equal.</li> </ul>	tor);			
<ul> <li>But careful! Won't work for Strings, because .equal Strings could be in different buckets:</li> <li>String H = "Hello", S1 = H + ", world!",</li> </ul>	<pre>map.put (key, value); // Map KEY -&gt; VALUE. // VALUE last mapped to by SOMEKEY.  map.get (someKey) // VALUE last mapped to by SOMEKEY.</pre>			
S2 = "Hello, world!"; • Here S1.equals(S2), but S1 != S2. Last modified: Thu Oct 25 19:09:55 2007 C561B: Lecture #26 9	<pre> map.containsKey (someKey)</pre>			

## Characteristics

- $\bullet$  Assuming good hash function, add, lookup, deletion take  $\Theta(1)$  time, amortized.
- Good for cases where one looks up equal keys.
- Usually bad for *range queries:* "Give me every name between Martin and Napoli." [Why?]
- But sometimes OK, if hash function is monotonic (i.e., when key  $k_1 > k_2$ , then  $h(k_1) \ge h(k_2)$ . For example,
  - Items are time-stamped records; key is the time.
  - Hashing function is to have one bucket for every hour.
- Hashing is probably not a good idea for small sets that you rapidly create and discard [why?]

## **Comparing Search Structures**

Here, N is #items, k is #answers to query.

	Unordered	Sorted	Bushy Search	"Good" Hash	
Function	List	Array	Tree	Table	Heap
find	$\Theta(N)$	$\Theta(\lg N)$	$\Theta(\lg N)$	$\Theta(1)$	$\Theta(N)$
add	$\Theta(1)$	$\Theta(N)$	$\Theta(\lg N)$	$\Theta(1)$	$\Theta(\lg N)$
range query	$\Theta(N)$	$\Theta(k + \lg N)$	$\Theta(k+\lg N)$	$\Theta(N)$	$\Theta(N)$
find largest	$\Theta(N)$	$\Theta(1)$	$\Theta(\lg N)$	$\Theta(N)$	$\Theta(1)$
remove largest	$\Theta(N)$	$\Theta(1)$	$\Theta(\lg N)$	$\Theta(N)$	$\Theta(\lg N)$