

61A Lecture 14

Friday, October 4

Mutable Functions

Announcements

- Homework 4 due Tuesday 10/8 @ 11:59pm.
- Project 2 due Thursday 10/10 @ 11:59pm.
- Guerrilla Section 2 this Saturday 10/5 & Sunday 10/6 10am-1pm in Soda.
 - Topics: Data abstraction, sequences, and non-local assignment.
 - Please RSVP on Piazza!
- Guest lecture on Wednesday 10/9, Peter Norvig on Natural Language Processing in Python.
 - No video (except a screencast)! Come to Wheeler.

A Function with Behavior That Varies Over Time

Let's model a bank account that has a balance of \$100

```

>>> withdraw(25)
75
>>> withdraw(25)
50
>>> withdraw(60)
'Insufficient funds'
>>> withdraw(15)
35
    
```

Return value: remaining balance

Argument: amount to withdraw

Different return value!

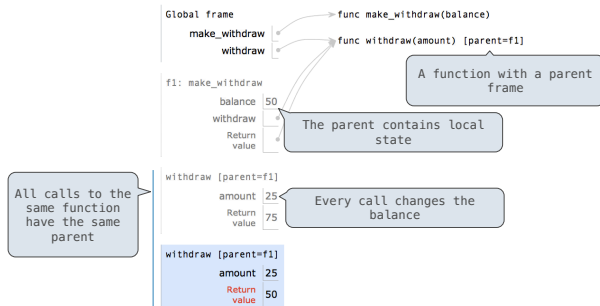
Second withdrawal of the same amount

Where's this balance stored?

Within the parent frame of the function!

A function has a body and a parent environment

Persistent Local State Using Environments



Example: <http://goo.gl/2d009a>

Reminder: Local Assignment

```

def percent_difference(x, y):
    difference = abs(x-y)
    return 100 * difference / x
diff = percent_difference(40, 50)
    
```

Assignment binds name(s) to value(s) in the first frame of the current environment

Global frame

- percent_difference

percent_difference

- x: 40
- y: 50
- difference: 10

Execution rule for assignment statements:

1. Evaluate all expressions right of =, from left to right.
2. Bind the names on the left the resulting values in the **first** frame of the current environment.

Example: <http://goo.gl/2kqg52>

Non-Local Assignment & Persistent Local State

```
def make_withdraw(balance):
    """Return a withdraw function with a starting balance."""
    def withdraw(amount):
        nonlocal balance
        if amount > balance:
            return 'Insufficient funds'
        balance = balance - amount
        return balance
    return withdraw
```

Declare the name "balance" nonlocal at the top of the body of the function in which it is re-assigned

Re-bind balance in the first non-local frame in which it was bound previously

(Demo)

Non-Local Assignment

The Effect of Nonlocal Statements

```
nonlocal <name>, <name>, ...
```

Effect: Future assignments to that name change its pre-existing binding in the **first non-local frame** of the current environment in which that name is bound.

Python Docs: an "enclosing scope"

From the Python 3 language reference:

Names listed in a nonlocal statement must refer to pre-existing bindings in an enclosing scope.

Names listed in a nonlocal statement must not collide with pre-existing bindings in the local scope.

http://docs.python.org/release/3.1.3/reference/simple_stmts.html#the-nonlocal-statement

<http://www.python.org/dev/peps/pep-3184/>

The Many Meanings of Assignment Statements

Status	Effect
<ul style="list-style-type: none"> No nonlocal statement "x" is not bound locally 	<div style="border: 1px solid black; padding: 2px; width: fit-content; margin: 0 auto;">x = 2</div> Create a new binding from name "x" to object 2 in the first frame of the current environment.
<ul style="list-style-type: none"> No nonlocal statement "x" is bound locally 	Re-bind name "x" to object 2 in the first frame of the current env.
<ul style="list-style-type: none"> nonlocal x "x" is bound in a non-local frame 	Re-bind "x" to 2 in the first non-local frame of the current environment in which it is bound.
<ul style="list-style-type: none"> nonlocal x "x" is not bound in a non-local frame 	SyntaxError: no binding for nonlocal 'x' found
<ul style="list-style-type: none"> nonlocal x "x" is bound in a non-local frame "x" also bound locally 	SyntaxError: name 'x' is parameter and nonlocal

Python Particulars

Python pre-computes which frame contains each name before executing the body of a function.

Therefore, within the body of a function, all instances of a name must refer to the same frame.

```
def make_withdraw(balance):
    def withdraw(amount):
        if amount > balance:
            return 'Insufficient funds'
        balance = balance - amount
        return balance
    return withdraw

wd = make_withdraw(20)
wd(5)
```

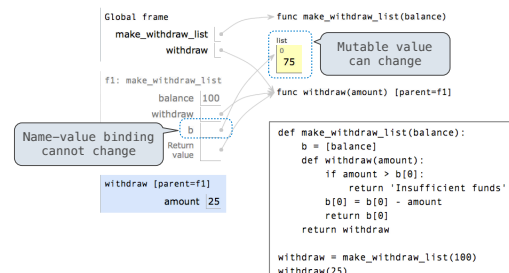
Local assignment

UnboundLocalError: local variable 'balance' referenced before assignment

Example: <http://goo.gl/B0YzC6>

Mutable Values & Persistent Local State

Mutable values can be changed *without* a nonlocal statement.



Example: <http://goo.gl/y41pZ2>

Multiple Mutable Functions

(Demo)

Sameness and Change

- As long as we **never modify** objects, we can regard a compound object to be precisely the **totality of its pieces**.
- A **rational number** is just its numerator and denominator.
- This view is no longer valid **in the presence of change**.
- Now, a compound data **object has an "identity"** that is something more than the pieces of which it is composed.
- A bank account is **still "the same" bank account even if we change the balance** by making a withdrawal.
- Conversely, we could have two bank accounts that happen to have the **same balance, but are different objects**.

John's Account
\$10

Steven's Account
\$10

Referential Transparency, Lost

•Expressions are **referentially transparent** if substituting an expression with its value does not change the meaning of a program.



```
mul(add(2, mul(4, 6)), add(3, 5))
```

```
mul(add(2, 24), add(3, 5))
```

```
mul(26, add(3, 5))
```



•Mutation operations violate the condition of referential transparency because they do more than just return a value; **they change the environment**.

(Demo)