

External Sorting

R & G Chapter 13

One of the advantages of being disorderly is that one is constantly making exciting discoveries.

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Why Sort?

- A classic problem in computer science!
- Data requested in sorted order
 - e.g., find students in increasing gpa order
- Sorting is first step in bulk loading B+ tree index.
- Sorting useful for eliminating duplicate copies in a collection of records (Why?)
- Sorting is useful for summarizing related groups of tuples
- Sort-merge join algorithm involves sorting.
- Problem: sort 1TB of data with 1GB of RAM.
 - why not virtual memory?



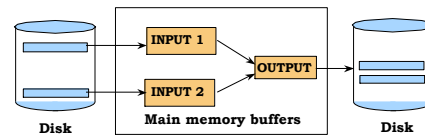
Streaming Data Through RAM

- An important detail for sorting & other DB operations
- Simple case:
 - Compute $f(x)$ for each record, write out the result
 - Read a page from INPUT to Input Buffer
 - Write $f(x)$ for each item to Output Buffer
 - When Input Buffer is consumed, read another page
 - When Output Buffer fills, write it to OUTPUT
- Reads and Writes are not coordinated
 - E.g., if $f()$ is Compress(), you read many pages per write.
 - E.g., if $f()$ is DeCompress(), you write many pages per read.



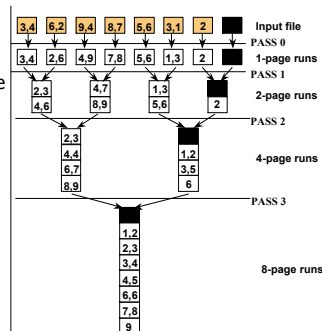
2-Way Sort

- Pass 0: Read a page, sort it, write it.
 - only one buffer page is used (as in previous slide)
- Pass 1, 2, ..., etc.:
 - requires 3 buffers
 - merge pairs of runs into runs twice as long



Two-Way External Merge Sort

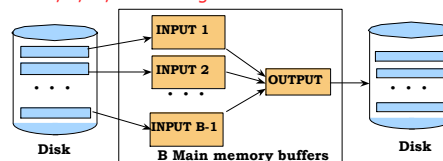
- Each pass we read + write each page in file.
- N pages in the file \Rightarrow the number of passes $= \lceil \log_2 N \rceil + 1$
- So total cost is: $2N(\lceil \log_2 N \rceil + 1)$
- **Idea: Divide and conquer:** sort subfiles and merge



General External Merge Sort

➤ *More than 3 buffer pages. How can we utilize them?*

- To sort a file with N pages using B buffer pages:
 - Pass 0: use B buffer pages. Produce $\lceil N/B \rceil$ sorted runs of B pages each.
 - Pass 1, 2, ..., etc.: merge $B-1$ runs.





Cost of External Merge Sort

- Number of passes: $1 + \lceil \log_{B-1} \lceil N/B \rceil \rceil$
- Cost = $2N * (\text{\# of passes})$
- E.g., with 5 buffer pages, to sort 108 page file:
 - Pass 0: $\lceil 108/5 \rceil = 22$ sorted runs of 5 pages each (last run is only 3 pages)
- Now, do four-way (B-1) merges
 - Pass 1: $\lceil 22/4 \rceil = 6$ sorted runs of 20 pages each (last run is only 8 pages)
 - Pass 2: 2 sorted runs, 80 pages and 28 pages
 - Pass 3: Sorted file of 108 pages



Number of Passes of External Sort

(I/O cost is $2N$ times number of passes)

N	B=3	B=5	B=9	B=17	B=129	B=257
100	7	4	3	2	1	1
1,000	10	5	4	3	2	2
10,000	13	7	5	4	2	2
100,000	17	9	6	5	3	3
1,000,000	20	10	7	5	3	3
10,000,000	23	12	8	6	4	3
100,000,000	26	14	9	7	4	4
1,000,000,000	30	15	10	8	5	4



Internal Sort Algorithm

- Quicksort is a fast way to sort in memory.
- Alternative: "tournament sort" (a.k.a. "heapsort", "replacement selection")
- Keep two heaps in memory, **H1** and **H2**

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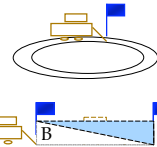
read B-2 pages of records, inserting into H1;
while (records left) {
    m = H1.removeMin(); put m in output buffer;
    if (H1 is empty)
        H1 = H2; H2.reset(); start new output run;
    else
        read in a new record r (use 1 buffer for input pages);
        if (r < m) H2.insert(r);
        else H1.insert(r);
}
H1.output(); start new run; H2.output();

```



More on Heapsort

- Fact: average length of a run is $2(B-2)$
 - The "snowplow" analogy
- Worst-Case:
 - What is min length of a run?
 - How does this arise?
- Best-Case:
 - What is max length of a run?
 - How does this arise?
- Quicksort is faster, but ... longer runs often means fewer passes!



I/O for External Merge Sort

- Actually, doing I/O a page at a time
 - Not an I/O per record
- In fact, read a *block (chunk)* of pages sequentially!
- Suggests we should make each buffer (input/output) be a *chunk* of pages.
 - But this will reduce fan-out during merge passes!
 - In practice, most files still sorted in **2-3 passes**.



Number of Passes of Optimized Sort

N	B=1,000	B=5,000	B=10,000
100	1	1	1
1,000	1	1	1
10,000	2	2	1
100,000	3	2	2
1,000,000	3	2	2
10,000,000	4	3	3
100,000,000	5	3	3
1,000,000,000	5	4	3

Block size = 32, initial pass produces runs of size $2B$.



Sorting Records!

- Sorting has become a blood sport!
 - Parallel sorting is the name of the game ...
- Minute Sort: how many 100-byte records can you sort in a minute?
 - Typical DBMS: in the MBs?
 - Current World record: 116 **GB**
 - 40 Dual-Processor Itanium2-based PCs, 2,520-disk RAID array
 - Estimated cost > \$9M
- Penny Sort: how many can you sort for a penny?
 - Current world record: 40GB
 - 1541 seconds on a \$614 Linux/AMD system (2003)
 - \$614 spread over 3 years worth of seconds = 1541 seconds/penny
- See <http://research.microsoft.com/barc/SortBenchmark/>



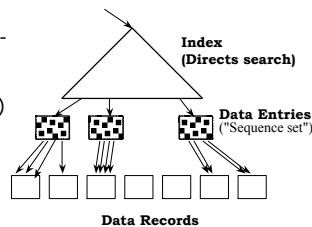
Using B+ Trees for Sorting

- Scenario: Table to be sorted has B+ tree index on sorting column(s).
- Idea: Can retrieve records in order by traversing leaf pages.
- Is this a good idea?
- Cases to consider:
 - B+ tree is clustered **Good idea!**
 - B+ tree is not clustered **Could be a very bad idea!**



Clustered B+ Tree Used for Sorting

- Cost: root to the left-most leaf, then retrieve all leaf pages (Alternative 1)
- If Alternative 2 is used? Additional cost of retrieving data records: each page fetched just once.

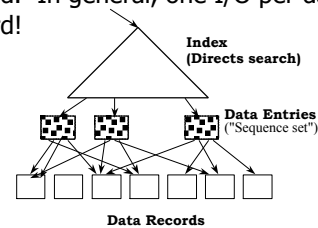


➡ **Better than external sorting!**



Unclustered B+ Tree Used for Sorting

- Alternative (2) for data entries; each data entry contains rid of a data record. In general, one I/O per data record!



External Sorting vs. Unclustered Index

N	Sorting	p=1	p=10	p=100
100	200	100	1,000	10,000
1,000	2,000	1,000	10,000	100,000
10,000	40,000	10,000	100,000	1,000,000
100,000	600,000	100,000	1,000,000	10,000,000
1,000,000	8,000,000	1,000,000	10,000,000	100,000,000
10,000,000	80,000,000	10,000,000	100,000,000	1,000,000,000

- ➡ p : # of records per page
- ➡ $B=1,000$ and block size=32 for sorting
- ➡ $p=100$ is the more realistic value.



Summary

- External sorting is important; some DBMSs may dedicate part of buffer pool for sorting!
- External merge sort minimizes disk I/O cost:
 - Pass 0: Produces sorted runs of size B (# buffer pages). Later passes: merge runs.
 - # of runs merged at a time depends on B, and block size.
 - Larger block size means less I/O cost per page.
 - Larger block size means smaller # runs merged.
 - In practice, # of passes rarely more than 2 or 3.



Summary, cont.

- Choice of internal sort algorithm may matter:
 - Quicksort: Quick!
 - Heap/tournament sort: slower (2x), longer runs
- The best sorts are wildly fast:
 - Despite 40+ years of research, we're still improving!
- Clustered B+ tree is good for sorting; unclustered tree is usually very bad.