



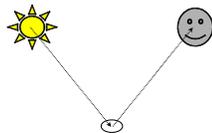
# Today

- Local Illumination & Shading
  - The BRDF
  - Simple diffuse and specular approximations
  - Shading interpolation: flat, Gouraud, Phong
  - Some miscellaneous tricks

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# Local Shading

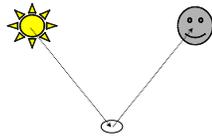
- Local: consider in isolation
  - 1 light
  - 1 surface
  - The viewer
- Recall: lighting is linear
  - Almost always...



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# Local Shading

- Local: consider in isolation
  - 1 light
  - 1 surface
  - The viewer
- Recall: lighting is linear
  - Almost always...



Counter example: photochromatic materials

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# Local Shading

- Examples of non-local phenomena
  - Shadows
  - Reflections
  - Refraction
  - Indirect lighting

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# The BRDF

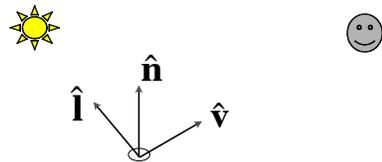
- The **B**i-directional **R**eflectance **D**istribution **F**unction
- Given
  - Surface material
  - Incoming light direction
  - Direction of viewer
  - Orientation of surface
- Return:
  - fraction of light that reaches the viewer
- We'll worry about physical units later...

$$\begin{aligned}\rho &= \rho(\theta_V, \theta_L) \\ &= \rho(\mathbf{v}, \mathbf{l}, \mathbf{n})\end{aligned}$$

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# The BRDF

$\rho(\mathbf{v}, \mathbf{l}, \mathbf{n})$



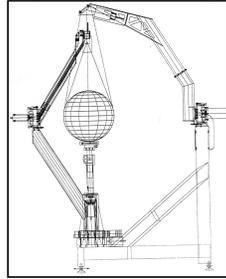
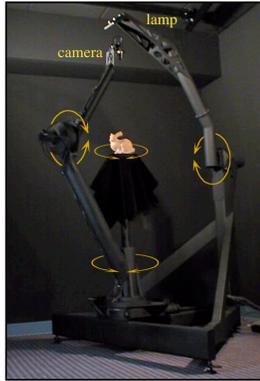
- Spatial variation capture by “the material”
- Frequency dependent
  - Typically use separate RGB functions
  - Does not work perfectly
  - Better:

$$\rho = \rho(\theta_V, \theta_L, \lambda_{in}, \lambda_{out})$$

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## Obtaining BRDFs

- Measure from real materials



Images from Marc Levoy 8

## Obtaining BRDFs

- Measure from real materials
- Computer simulation
  - Simple model + complex geometry
- Derive model by analysis
- Make something up

## Beyond BRDFs

- The BRDF model does not capture everything
  - e.g. Subsurface scattering (BSSRDF)

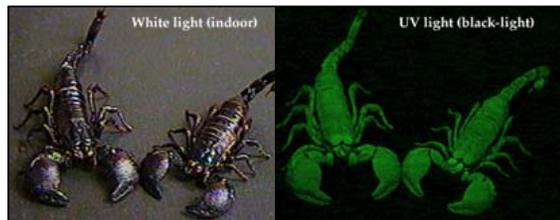


Images from Jensen *et. al*, SIGGRAPH 2001

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## Beyond BRDFs

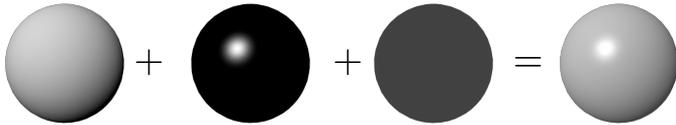
- The BRDF model does not capture everything
  - e.g. Inter-frequency interactions



$\rho = \rho(\theta_V, \theta_L, \lambda_{in}, \lambda_{out})$  This version would work... ..

## A Simple Model

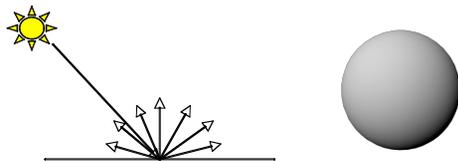
- Approximate BRDF as sum of
  - A diffuse component
  - A specular component
  - A "ambient" term



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## Diffuse Component

- Lambert's Law
  - Intensity of reflected light proportional to cosine of angle between surface and incoming light direction
  - Applies to "diffuse," "Lambertian," or "matte" surfaces
  - Independent of viewing angle
- Use as a component of non-Lambertian surfaces



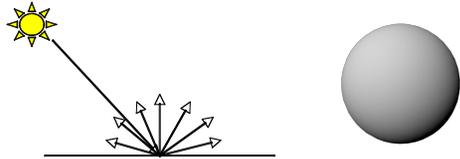
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# Diffuse Component

Comment about two-side lighting in text is wrong..

$$k_d I (\hat{\mathbf{l}} \cdot \hat{\mathbf{n}})$$

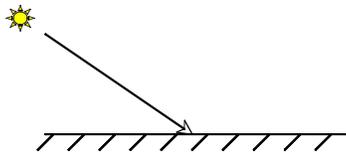
$$\max(k_d I (\hat{\mathbf{l}} \cdot \hat{\mathbf{n}}), 0)$$



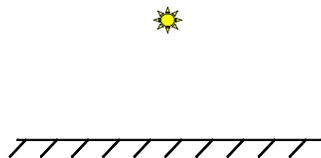
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# Diffuse Component

- Plot light leaving in a given direction:



- Plot light leaving from each point on surface



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# Specular Component

- Specular component is a mirror-like reflection
- Phong Illumination Model
  - A reasonable approximation for some surfaces
  - Fairly cheap to compute
- Depends on view direction

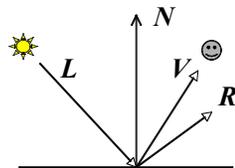


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# Specular Component

$$k_s I (\hat{\mathbf{r}} \cdot \hat{\mathbf{v}})^p$$

$$k_s I \max(\hat{\mathbf{r}} \cdot \hat{\mathbf{v}}, 0)^p$$

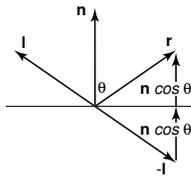


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## Specular Component

- Computing the reflected direction

$$\hat{\mathbf{r}} = -\hat{\mathbf{l}} + 2(\hat{\mathbf{l}} \cdot \hat{\mathbf{n}})\hat{\mathbf{n}}$$

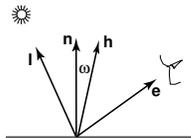


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## Specular Component

- “Half-angle” approximation for specular

$$\hat{\mathbf{h}} = \frac{\hat{\mathbf{l}} + \hat{\mathbf{v}}}{\|\hat{\mathbf{l}} + \hat{\mathbf{v}}\|}$$



different specular term  $k_s I (\hat{\mathbf{h}} \cdot \hat{\mathbf{n}})^p$

*\*Don't use half-angle approximation  
in your assignment!*

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Wednesday, August 31, 11





## Ambient Term

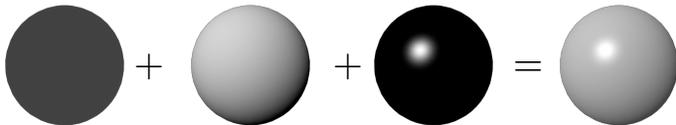
- Really, its a cheap hack
- Accounts for “ambient, omnidirectional light”
- Without it everything looks like it's in space



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## Summing the Parts

$$R = k_a I + k_d I \max(\hat{\mathbf{l}} \cdot \hat{\mathbf{n}}, 0) + k_s I \max(\hat{\mathbf{r}} \cdot \hat{\mathbf{v}}, 0)^p$$



- Recall that the  $k_i$  are by wavelength
  - RGB in practice
- Sum over all lights

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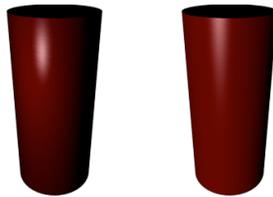






## Direction -vs- Point Lights

- For a point light, the light direction changes over the surface
- For "distant" light, the direction is constant
- Similar for orthographic/perspective viewer



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## Falloff

- Physically correct:  $1/r^2$  light intensity falloff
  - Tends to look bad (why?)
  - Not used in practice
- Sometimes compromise of  $1/r$  used

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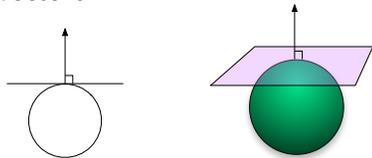
Ugly....



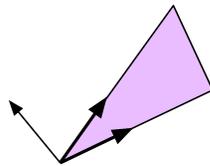
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## Surface Normals

- The normal vector at a point on a surface is perpendicular to all surface tangent vectors



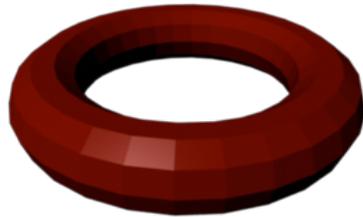
- For triangles normal given by right-handed cross product



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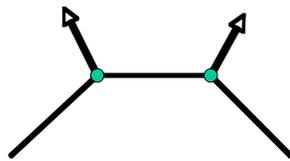
## Flat Shading

- Use constant normal for each triangle (polygon)
  - Polygon objects don't look smooth
  - Faceted appearance very noticeable, especially at specular highlights
  - Recall mach bands...



## Smooth Shading

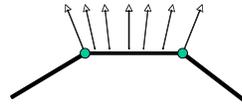
- Compute "average" normal at vertices
- Interpolate across polygons
- Use threshold for "sharp" edges
  - Vertex may have different normals for each face





# Phong Shading

- Compute shading at each pixel
  - Interpolate *normals* from vertices
  - Pros: looks smooth, better speculars
  - Cons: expensive



Gouraud



Phong

Note: Gouraud was hardware rendered...