| Lecture #17: Typing Examples for ChocoPy | Variable Access |
|---|---|
| Today, we'll adapt the notation from Friday to ChocoPy. | The type environment tells us about variables' types. |
| In order to cover all constructs, we will need to augment the type environment with some other information. | $\frac{O(id) = T, \text{where } T \text{ is not a function type.}}{O, M, C, R \vdash id : T} [\text{var-read}]$ |
| Our type assertions will have one of the forms | We only apply this rule when an identifier appears as an expression or the left side of an assignment. |
| $O, M, C, R \vdash e : T$ or $O, M, C, R \vdash s$ | |
| depending on whether we are typing expressions or statements, where | The provision that T not be a function type reflects the fact that in ChocoPy, functions are not first-class values. Their identifiers are handled elsewhere. |
| O is a type environment as in the last lecture. M is the member environment: M(C, I) returns the type of the attribute or method named I in class C. C is the enclosing class. R is the type to be returned by the enclosing function or method. | |
| Hence the type assertions above means | |
| The expression e type checks and has type T , or the construct s is correctly typed, given that O, M, C, R are the type environment, member environment, enclosing class, and expected return type. | |
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Variable Assignment

• Variable assignment is closely related:

 $\begin{array}{l} O, M, C, R \vdash e_0 : T_0 \\ O, M, C, R \vdash e_1 : T_1 \\ \hline T_1 \leq_a T_0 \\ O, M, C, R \vdash e_0 = e_1 \end{array} \ \begin{bmatrix} \text{ASSIGN-STMT} \end{bmatrix} \end{array}$

- The final line lacks a ': T' annotation because an assignment, being a statement, does not produce a value and therefore does not have a type.
- We are making use of the \leq_a relation between types: assignment compatibility.
- This is a slight tweak on the ChocoPy type hierarchy: $T_1 \leq_a T_2$ iff
 - $T_1 \leq T_2$ (i.e., ordinary subtyping).
 - T_1 is <None> and T_2 is not int, bool, or str.
 - T_2 is a list type \circ{T} and T_1 is <Empty>.
 - T_2 is the list type [T] and T_1 is [<None>], where <None> $\leq_a T$.
- Here, <Empty> is the type of the empty list, and <None> is the type of None.

Variable Initialization

• This is obviously closely related to assignment.

$$\begin{split} O(id) &= T\\ O, M, C, R \vdash e_1: T_1\\ \frac{T_1 \leq_a T}{O, M, C, R \vdash id: T = e_1} \quad \text{[VAR-INIT]} \end{split}$$

• This is declaration and, like a statement, does not produce a value. The ':' here is part of ChocoPy syntax, and not part of a type rule.



Return

 \bullet The return statement is where the 'R' part of type rules comes in:

$$\begin{array}{l} O, M, C, R \vdash e : T \\ \hline T \leq_a R \\ O, M, C, R \vdash \texttt{return} \ e \end{array} \quad \begin{bmatrix} \texttt{RETURN-E} \end{bmatrix}$$

$$\frac{<\texttt{None}> \leq_a R}{O, M, C, R \vdash \texttt{return}} \quad \begin{bmatrix} \texttt{RETURN} \end{bmatrix}$$

• The second rule forbids programs like this:

def f() -> int:
 return

Since None may not be assigned to an int value.

• We don't deal here with an *implicit* return of None from a function returning int, as happens when there is no **return** statement along some path. Instead, we can deal with that by inserting a **return** at the end of any function with a path that does not contain a **return**.

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Function Calls

$$\begin{array}{c} O, M, C, R \vdash e_{1} : T_{1}^{\prime \prime} \\ \vdots \\ O, M, C, R \vdash e_{n} : T_{n}^{\prime \prime} \\ n \geq 0 \\ O(f) = \{T_{1} \times \ldots \times T_{n} \rightarrow T_{0}; x_{1}, x_{2}, \ldots, x_{n}; v_{1} : T_{1}^{\prime}, \ldots, v_{m} : T_{m}^{\prime}\} \\ \frac{\forall 1 \leq i \leq n : T_{i}^{\prime \prime} \leq_{a} T_{i}}{O, M, C, R \vdash f(e_{1}, e_{2}, \ldots, e_{n}) : T_{0}} \quad \text{[Invoke]} \end{array}$$

 \bullet Dispatching calls on class members are the same, except that we get the type from M rather than O:

$$O, M, C, R \vdash e_1 : T''_1$$

$$: O, M, C, R \vdash e_n : T''_n$$

$$n \ge 1$$

$$M(T''_1, f) = \{T_1 \times \ldots \times T_n \to T_0; x_1, x_2, \ldots, x_n; v_1 : T_1', \ldots, v_m : T_m'\}$$

$$T''_1 \le_a T_1$$

$$\forall 1 \le 2 \le n : T''_i \le_a T_i$$

$$O, M, C, R \vdash e_1.f(e_2, \ldots, e_n) : T_0$$
[DISPATCH]

Function Types

- The ChocoPy reference uses a somewhat nonstandard notation for function types in order to carry around a bit more information that's useful elsewhere.
- Here, I'll revise it a bit to make the traditional function type signature itself clear:

 $\{T_1 \times T_2 \times \ldots \times T_n \to T_0; x_1, x_2, \ldots, x_n; v_1 : T_1', v_2 : T_2', \ldots, v_m : T_m'\}$

will denote a function whose

- type is $T_1 \times T_2 \times \ldots \times T_n \rightarrow T_0$,
- formal parameters names are x_i , and
- local names (local variables and nested functions) are v_j with types T_j '.

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Function Definition

$$T = \begin{cases} T_0, & \text{if } -> \text{ is present,} \\ <\text{None>}, & otherwise. \end{cases}$$

$$O(f) = \{T_1 \times \ldots \times T_n \to T_0; x_1, x_2, \ldots, x_n; v_1 : T_1', \ldots, v_m : T_m'\}$$

$$n \ge 0 \qquad m \ge 0$$

$$O[T_1/x_1] \ldots [T_n/x_n][T_1'/v_1] \ldots [T_m'/v_m], M, C, T \vdash b$$

$$O(M, C, R \vdash \det f(x_1:T_1, \ldots, x_n:T_n) \text{ [-> } T_0 \text{]}^?:b \qquad \text{[FUNC-DEF]}$$

- So the definition as a whole type checks if it gives the right types for parameters and locals, and...
- the body type checks after substituting the indicated types for the formal parameter and local variable and function names.
- Here, we finally do something other than passing the R parameter in. When type-checking the body, R becomes the return type, allowing us to type-check **return** statements correctly (see the last hypothesis).

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Getting Things Started

- \bullet Before applying these rules, we gather up definitions of variables, functions, and classes in order to get the initial O and C.
- Also, the global definitions are part of this initial O and M:

• And the whole program is then

 $\frac{O, M, \bot, \bot \vdash program}{\vdash program} \quad [PROGRAM]$

where \perp ("bottom") means something undefined.

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