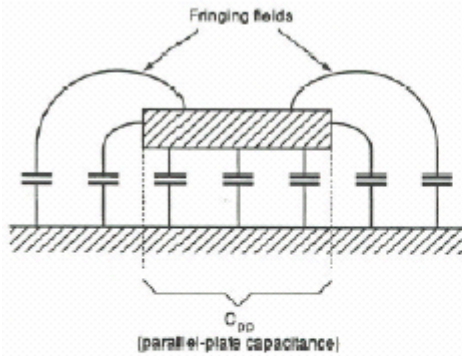


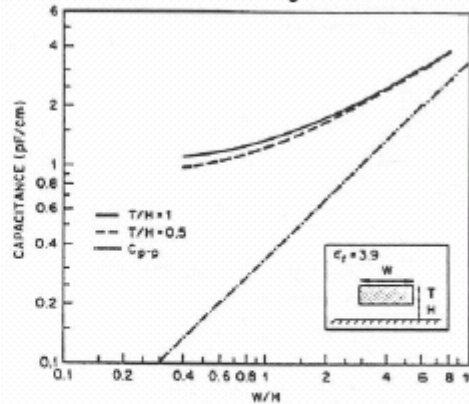
Homework #12 Solutions

Problem 1

Model for determining interconnect capacitance:



For $W / t_{di} < 1.5$, C_{fringe} is dominant



Wire capacitance per unit length:

$$C_{wire} \cong C_{pp} + C_{fringe} = \frac{W \epsilon_{di}}{t_{di}} + \frac{2\pi \epsilon_{di}}{\log(t_{di} / H)} \quad w = W - \frac{H}{2}$$

First calculate the resistance and capacitance of the wire:

$$R_{wire} = (\rho L) / (HW) = (2.7 \mu\Omega\text{-cm} \times L) / (0.5 \times 10^{-4} \text{cm} \times 1 \times 10^{-4} \text{cm}) = 540L \text{ } [\Omega/\text{cm}]$$

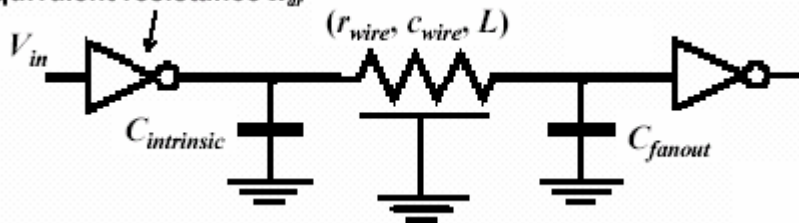
$$w = W - H/2 = 1 \times 10^{-4} \text{cm} - 0.5 \times 10^{-4} \text{cm} / 2 = 0.75 \times 10^{-4} \text{cm}$$

$$C_{wire_per_unit_length} = [(0.75 \times 10^{-4} \text{cm} \times 3.45 \times 10^{-13} \text{ F/cm}) / 1 \times 10^{-4} \text{cm}] + [(2 \times 3.14 \times 3.45 \times 10^{-13} \text{ F/cm}) / \log(1/0.5)] = 7.46 \times 10^{-12} \text{ F/cm}$$

$$C_{wire} = 7.4597 \times 10^{-12} \times L \text{ } [\text{F/cm}]$$

Model for determining propagation delay:

Equivalent resistance R_{dr}



$$t_p = 0.69 R_{dr} C_{intrinsic} + 0.69 (R_{dr} + R_{wire}) C_{fanout} + (0.69 R_{dr} + 0.38 R_{wire}) C_{wire}$$

Substituting in the values for all the components in the above equation we get:

The propagation delay of Inverter A is given by the equation above.
Substituting in the values for all the components in the above equation we get:

$$t_p = 0.69(10k\Omega)(3 \times 10^{-15}F) + 0.69(10k\Omega + 540L)(3 \times 10^{-15}F) + [0.69(10k\Omega) + 0.38(540L)] 7.4597 \times 10^{-12} \times L$$

$$t_p = 4.14 \times 10^{-11} + 5.1473 \times 10^{-8} \times L + 1.5307 \times 10^{-9} \times L^2$$

We must solve for L using the following constraint:

$$\text{interconnect delay} = 0.5(t_p)$$

$$5.1472 \times 10^{-8} \times L + 1.5307 \times 10^{-9} \times L^2 = 0.5(4.14 \times 10^{-11} + 5.1475 \times 10^{-8} \times L + 1.53 \times 10^{-9} \times L^2)$$

$$-2.07 \times 10^{-11} + 2.5735 \times 10^{-8} \times L + 7.6537 \times 10^{-10} \times L^2 = 0$$

Solving for L yields: $L = 8.035 \times 10^{-3} \text{ cm} = 80.35 \mu\text{m}$.

Problem 2

For this problem we assume the simple parallel-plate model as we are told that fringing-field capacitance is negligible. The equation we use to calculate the wire capacitance is given on slide 6, lecture 37:

$$C_{pp} = \frac{\epsilon_{di}}{t_{di}} WL$$

$$a) R_{\text{wire1}} = (\rho L)/(HW) = (2.7 \mu\Omega\text{-cm} \times 500 \times 10^{-4} \text{ cm}) / (0.5 \times 10^{-4} \text{ cm} \times 2 \times 10^{-4} \text{ cm}) = 13.5 \Omega$$

R_{wire1} is much smaller than R_{dr} of Inverter A: $13.5 \Omega \ll 10 \text{ k}\Omega$

Hence $(R_{\text{wire1}} + R_{\text{dr}}) \approx R_{\text{dr}} = 10 \text{ k}\Omega$.

$$C_{\text{wire1}} = C_{\text{wire2}} = C_{pp} = [(2 \times 10^{-4} \text{ cm} \times 500 \times 10^{-4} \text{ cm} \times 3.45 \times 10^{-13} \text{ F/cm}) / 1 \times 10^{-4} \text{ cm}] = 34.5 \text{ fF}$$

$$C_C = \epsilon_{di} \times H \times L / \text{spacing}$$

$$C_C = 3.45 \times 10^{-13} \text{ F/cm} \times 0.5 \times 10^{-4} \text{ cm} \times 500 \times 10^{-4} \text{ cm} / 0.5 \times 10^{-4} \text{ cm}$$

$$C_C = 17.25 \text{ fF}$$

$$C_{\text{in2}} = 3 \text{ fF from Problem 1.}$$

$$C_{\text{out1}} = 3 \text{ fF from Problem 1.}$$

$$\tau_D = (C_{\text{out1}} R_{\text{dr}}) + (R_{\text{wire1}} + R_{\text{dr}}) [C_{\text{wire1}} + (C_{\text{wire2}} C_C) / (C_{\text{wire2}} + C_C) + C_{\text{in2}}]$$

$$\tau_D \approx 3 \text{ fF} \times 10 \text{ k}\Omega + 10 \text{ k}\Omega [34.5 \text{ fF} + 34.5 \text{ fF} (17.25 \text{ fF}) / (34.5 \text{ fF} + 17.25 \text{ fF}) + 3 \text{ fF}]$$

$$\tau_D \approx 0.52 \text{ ns}$$

$$c) \tau_D = (C_{\text{out1}} R_{\text{dr}}) + (R_{\text{wire1}} + R_{\text{dr}}) [C_{\text{wire1}} + C_C + C_{\text{in2}}]$$

$$\tau_D \approx 3 \text{ fF} \times 10 \text{ k}\Omega + 10 \text{ k}\Omega (34.5 \text{ fF} + 17.25 \text{ fF} + 3 \text{ fF})$$

$$\tau_D \approx 0.58 \text{ ns}$$