

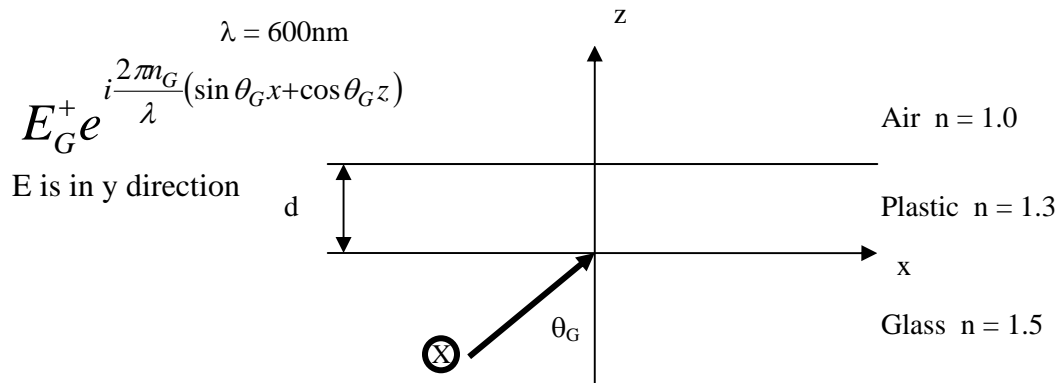
**EECS 210**  
 Fall 2006  
 Tu, Th 12:30-2  
 400 Cory

**Applied Electromagnetic Theory**  
 Office Hours  
 M, (W), 11AM  
 Tu, Th, (F) 10AM

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**Homework # 6: Due Start of Class Thursday, Oct 19<sup>th</sup>**  
**Midterm In Class Tuesday, Oct 24**  
**See Exam Midterm Specification Sheet**



**6.1) Kinetic Boundary Conditions and k-vectors:**

- Start a k-vector plot by drawing the  $k_x$  and  $k_z$  axes and concentric circles of radius 1, 1.3 and 1.5. (The 1 here indicates that the k-vectors are normalized to the k for a plane wave in free space.)
- Sketch the 5 k-vectors for the plane waves that will arise for an incidence angle of  $30^\circ$  in glass.
- Compute the angles in plastic and air and show that the k-vector x-component is the same for all 5 k-vectors.
- Find the period of the variation parallel to the surface. (It is larger than 600 nm and this allows radiation in air).
- Find the k-vectors for an incidence angle of  $60^\circ$  in glass find the period of variation along the surface. (It is smaller than 600nm and no radiation occurs.)

**6.2) Dynamic Boundary Conditions:**

- Write out phasor expressions for the plane wave fields as a function of x and z for each of the 5 k-vectors in terms of a complex constant in each region using the example notation above.
- Write sufficient boundary conditions at  $z = 0$ , plug in the fields and evaluate derivatives.
- Write sufficient boundary conditions at  $z = d$ , plug in the field and evaluate derivatives.
- Show that the kinematic condition can be factored out of these boundary conditions.

**6.3) Physical Effects:**

- Find the time-average and instantaneous Poynting vector in air for  $30^\circ$  incidence in glass.
- Find the time-average and instantaneous Poynting vector in air for  $50^\circ$  incidence in glass.
- Show that for  $50^\circ$  incidence in glass that the z-component of the Poynting vector is zero for time average and imaginary for time-varying.
- Define the transverse impedance as  $E_y/H_x$  and show that this impedance is real for  $30^\circ$  incidence in glass and becomes a capacitive reactance for  $50^\circ$  incidence in glass.
- Show that the ratio of the incident and reflected waves in plastic at d is independent of d itself and hence the standing wave ratio in plastic does not depend on thickness.