inst.eecs.berkeley.edu/~cs61c UC Berkeley CS61C : Machine Structures Lecture 26 – Combinational Logic Blocks



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Robot rides bike! \Rightarrow

The PRIMER-V2 robot is capable of starting from a stopped position, start riding, follows a path specified by a controller, and can stop without falling! Very very cool...

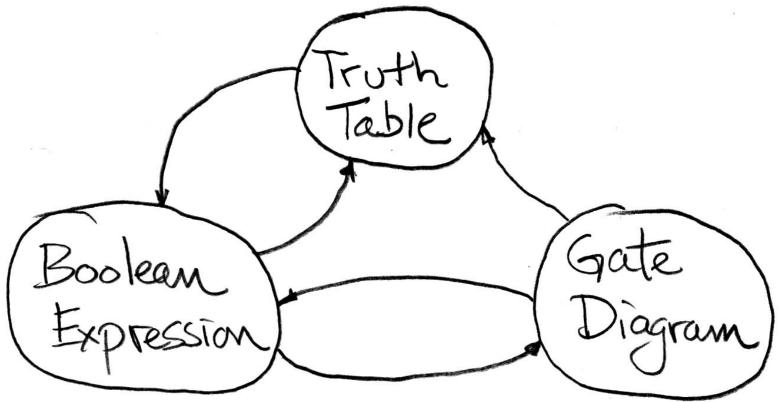




robosavvy.com/forum/viewtopic.php?p=32542 CS61C L26 Combinational Logic Blocks (1) Garcia, Fall 2011 © UCB

Review

• Use this table and techniques we learned to transform from 1 to another





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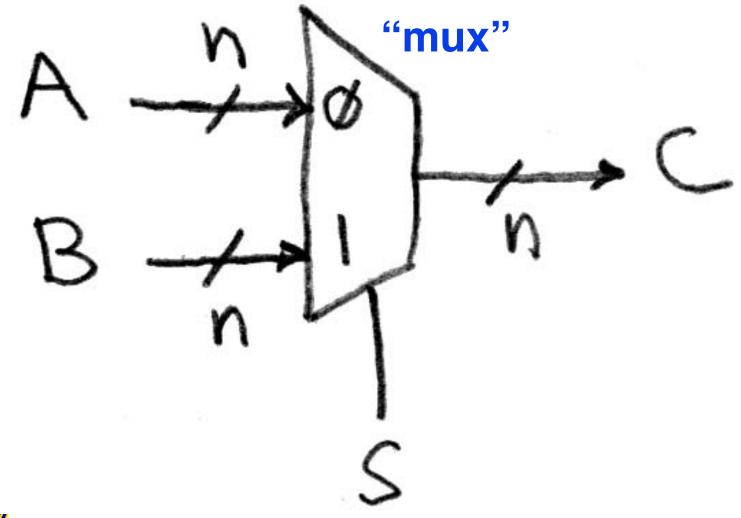
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Today

- Data Multiplexors
- Arithmetic and Logic Unit
- Adder/Subtractor

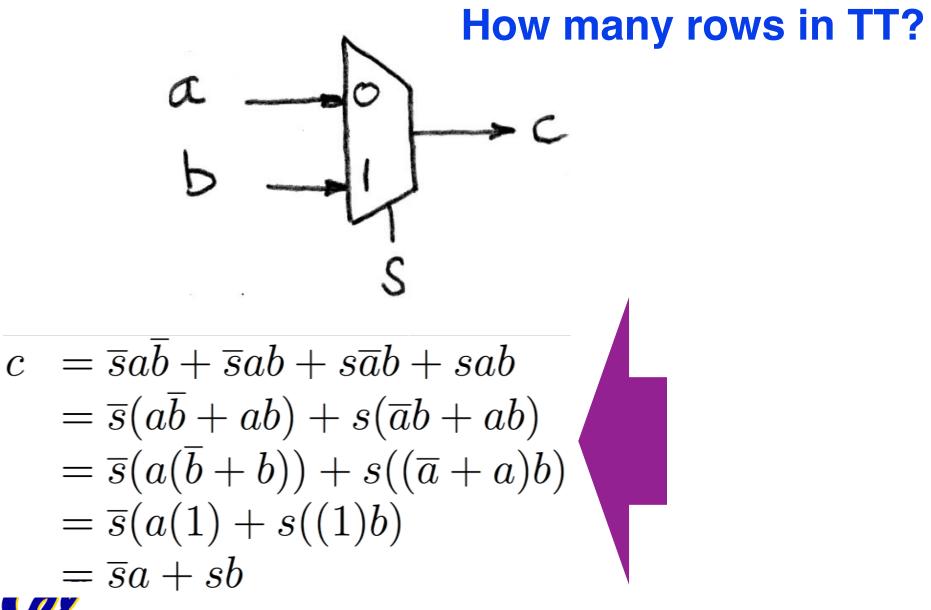


Data Multiplexor (here 2-to-1, n-bit-wide)



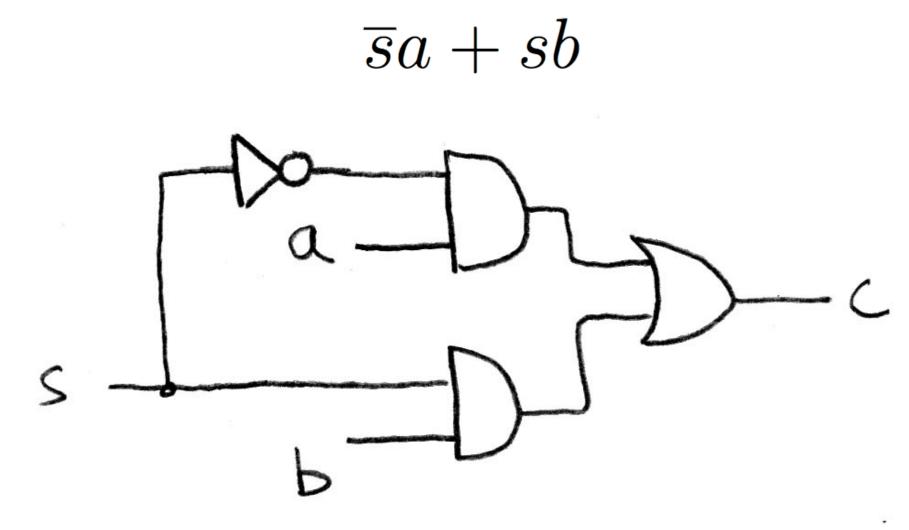


N instances of 1-bit-wide mux

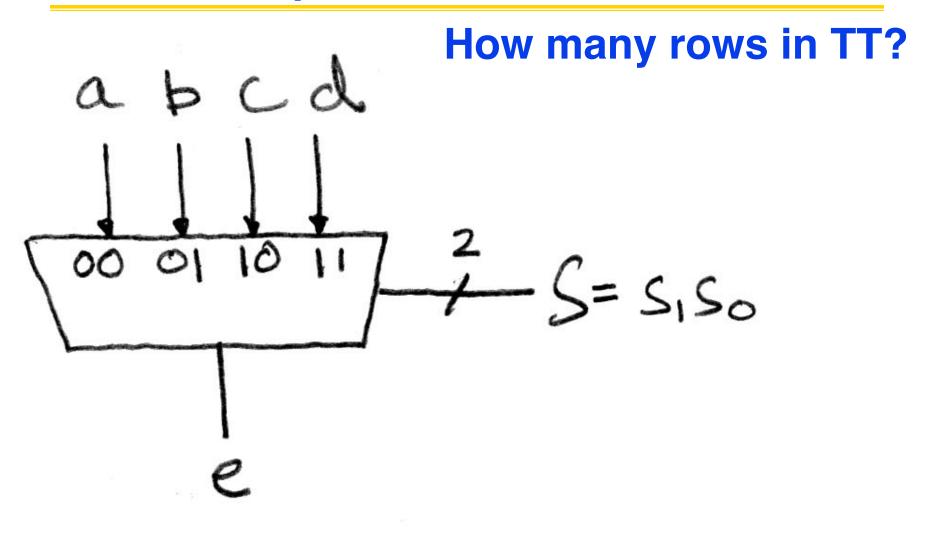




How do we build a 1-bit-wide mux?



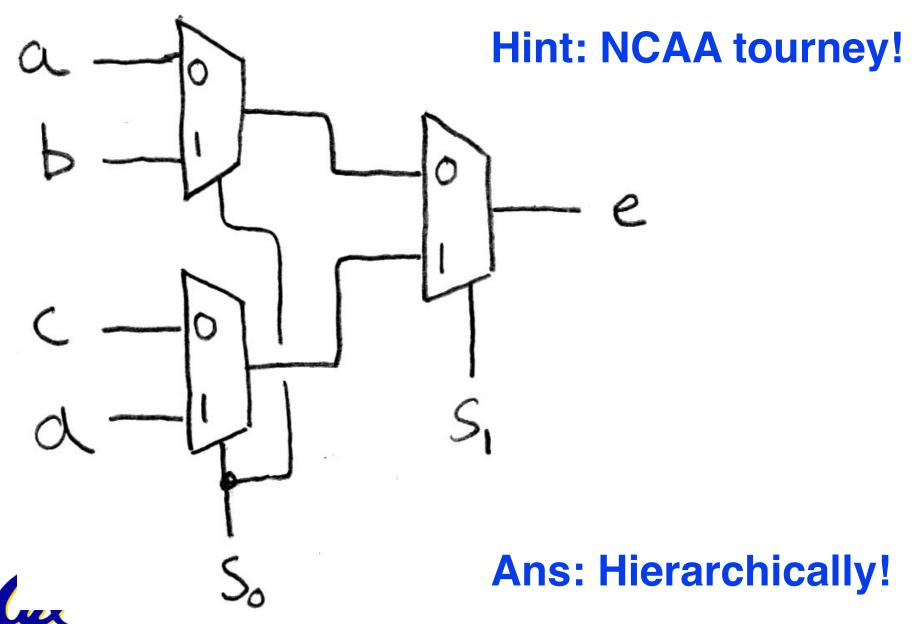
4-to-1 Multiplexor?



 $e = \overline{s_1}\overline{s_0}a + \overline{s_1}s_0b + s_1\overline{s_0}c + s_1s_0d$



Is there any other way to do it?

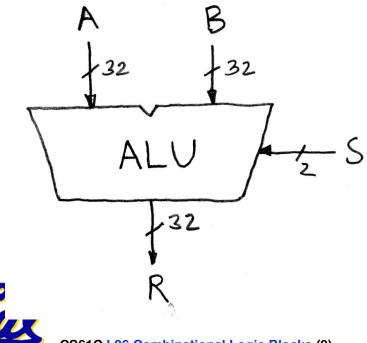


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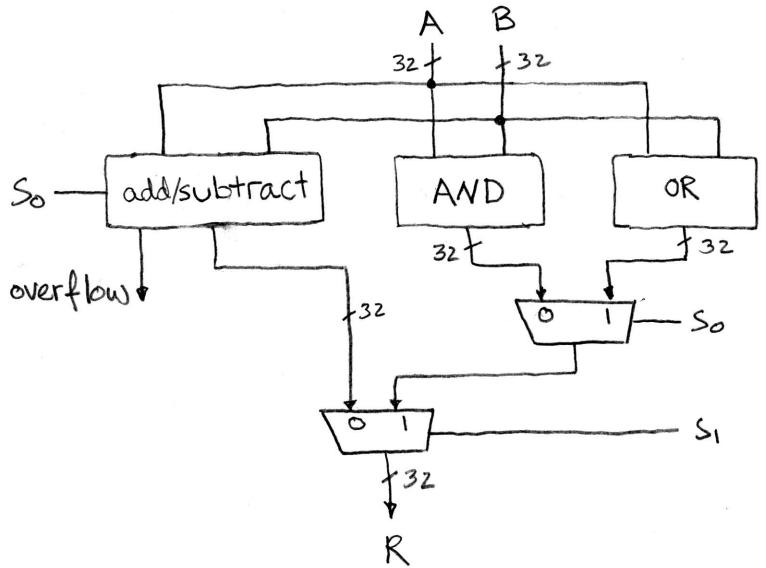
Arithmetic and Logic Unit

- Most processors contain a special logic block called "Arithmetic and Logic Unit" (ALU)
- We'll show you an easy one that does ADD, SUB, bitwise AND, bitwise OR



when S=00, R=A+B when S=01, R=A-B when S=10, R=A AND B when S=11, R=A OR B

Our simple ALU





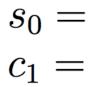
Adder/Subtracter Design -- how?

- Truth-table, then determine canonical form, then minimize and implement as we've seen before
- Look at breaking the problem down into smaller pieces that we can cascade or hierarchically layer



Adder/Subtracter – One-bit adder LSB...

	a_3	a_2	a_1	a_0	
+	b_3	b_2	b_1	b_0	
	S 3	s_2	s_1	s ₀	





Adder/Subtracter – One-bit adder (1/2)...

						a_i	\mathbf{b}_i	\mathbf{c}_i	Si	c_{i+1}
						0	0	0	0	0
	0	0	0			0	0	1	1	0
		a_2				0	1	0	1	0
+	b_3	b_2	b_1	b_0		0	1	1	0	1
		s ₂	s ₁	S∩	-	1	0	0	1	0
	0	2	-	0		1	0	1	0	1
						1	1	0	0	1
						1	1	1	1	1

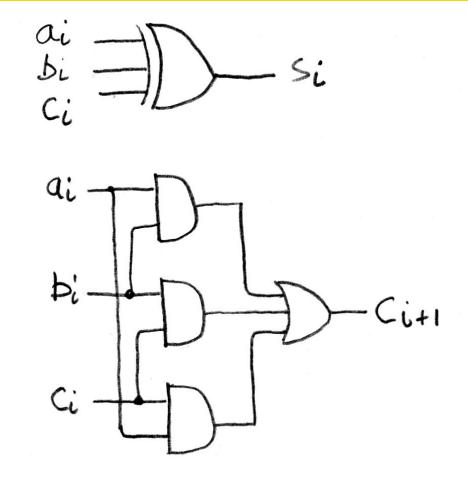
$$s_i =$$

$$c_{i+1} =$$



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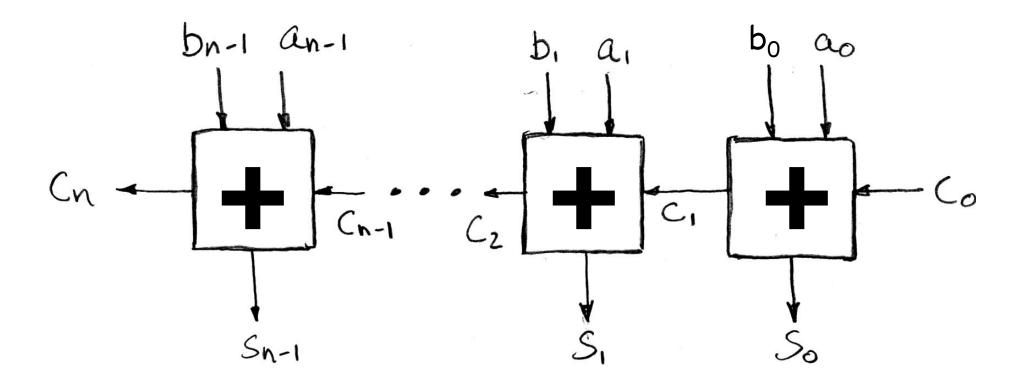
Adder/Subtracter – One-bit adder (2/2)...



$$\begin{aligned} s_i &= \operatorname{XOR}(a_i, b_i, c_i) \\ c_{i+1} &= \operatorname{MAJ}(a_i, b_i, c_i) = a_i b_i + a_i c_i + b_i c_i \end{aligned}$$



N 1-bit adders \Rightarrow 1 N-bit adder



What about overflow? **Overflow** = c_n ?



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What about overflow?Consider a 2-bit signed # & overflow:

 $\cdot 10 = -2 + -2 \text{ or } -1$

$$\cdot 11 = -1 + -2$$
 only

- $\bullet 00 = 0$ NOTHING!
- $\cdot 01 = 1 + 1$ only
- $c_{2} = c_{1} = c_{0}$

- Highest adder
 - $C_1 = Carry-in = C_{in}$, $C_2 = Carry-out = C_{out}$
 - No C_{out} or $C_{in} \Rightarrow$ NO overflow!

What $\cdot C_{in}$, and $C_{out} \Rightarrow NO$ overflow!

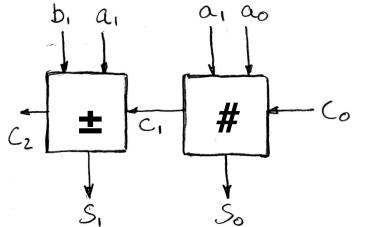
•
$$C_{in}$$
, but no $C_{out} \Rightarrow A, B$ both > 0, overflow!

• C_{out} , but no $C_{in} \Rightarrow A, B$ both < 0, overflow!



op?

- Consider a 2-bit signed # & overflow:
 - $10 = -2 \\ 11 = -1 \\ 00 = 0 \\ 01 = 1$



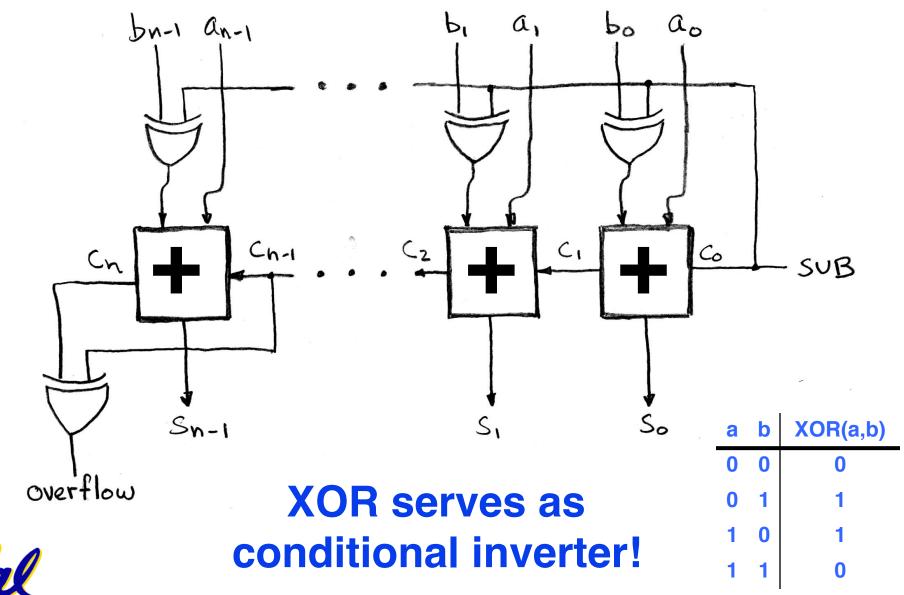
Overflows when...

• C_{in} , but no $C_{out} \Rightarrow A,B$ both > 0, overflow! • C_{out} , but no $C_{in} \Rightarrow A,B$ both < 0, overflow!

overflow = $c_n \operatorname{XOR} c_{n-1}$



Extremely Clever Subtractor



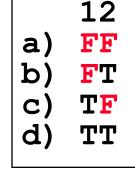
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1) Truth table for mux with 4-bits of signals has 2⁴ rows

2) We could cascade N 1-bit shifters to make 1 N-bit shifter for sll, srl





Peer Instruction Answer

- 1) Truth table for mux with 4-bits of signals controls 16 inputs, for a total of 20 inputs, so truth table is 2²⁰ rows...FALSE
- 2) We could cascade N 1-bit shifters to make 1 N-bit shifter for sll, srl ... TRUE
- 1) Truth table for mux with 4-bits of signals is 2⁴ rows long
- 2) We could cascade N 1-bit shifters to make 1 N-bit shifter for sll, srl



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"And In conclusion..."

- Use muxes to select among input
 - S input bits selects 2^S inputs
 - Each input can be n-bits wide, indep of S
- Can implement muxes hierarchically
- ALU can be implemented using a mux
 - Coupled with basic block elements
- N-bit adder-subtractor done using N 1bit adders with XOR gates on input
 - XOR serves as conditional inverter

