

Review

- CS61C: Learn 6 great ideas in computer architecture to enable high performance programming via parallelism, not just learn C
 - 1. Layers of Representation/Interpretation
 - 2. Moore's Law
 - 3. Principle of Locality/Memory Hierarchy

 - 5. Performance Measurement and Improvement
 - 6. Dependability via Redundancy



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Putting it all in perspective...

"If the automobile had followed the same development cycle as the computer,

- Robert X. Cringely



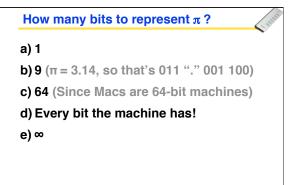


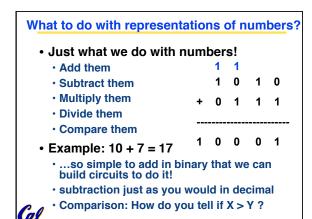


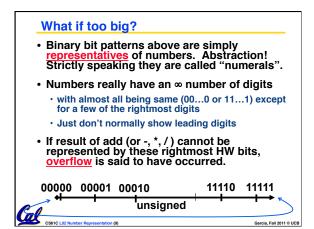
Data input: Analog -> Digital · Real world is analog! To import analog information, we must do two things Sample E.g., for a CD, every 44,100ths of a second, we ask a music signal how loud it is. Quantize For every one of these samples, we figure out where, on a 16-bit (65,536 tic-mark) "yardstick", it lies. Col CSEIC LE

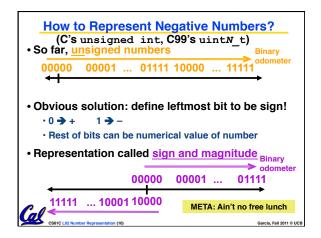


BIG IDEA: Bits can represent anything!! · Characters? • 26 letters \Rightarrow 5 bits (2⁵ = 32) • upper/lower case + punctuation ⇒ 7 bits (in 8) ("ASCII") • standard code to cover all the world's languages ⇒ 8,16,32 bits ("Unicode") www.unicode.com Logical values? · 0 ⇒ False, 1 ⇒ True • colors ? Ex: Red (00) Green (01) Blue (11) · locations / addresses? commands? MEMORIZE: N bits ⇔ at most 2^N things

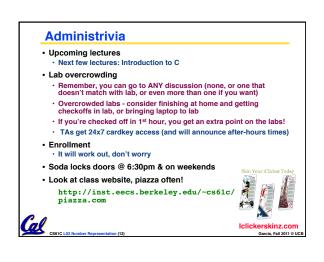








Shortcomings of sign and magnitude? • Arithmetic circuit complicated • Special steps depending whether signs are the same or not • Also, two zeros • 0x00000000 = +0_{ten} • 0x80000000 = -0_{ten} • What would two 0s mean for programming? • Also, incrementing "binary odometer", sometimes increases values, and sometimes decreases!



Great DeCal courses I supervise

- UCBUGG (3 units, P/NP)
 - · UC Berkeley Undergraduate Graphics Group
 - · TuTh 5-7pm in 200 Sutardja Dai
 - · Learn to create a short 3D animation
 - No prereqs (but they might have too many students, so admission not guaranteed)
 - ·http://ucbugg.berkeley.edu
- MS-DOS X (2 units, P/NP)
 - · Macintosh Software Developers for OS X
 - TuTh 7-9pm in 200 Sutardja Dai
 - · Learn to program iOS devices!
 - · No prereqs (other than interest)
 - •http://msdosx.berkeley.edu



CS61C L02 Number Representation (13)

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Another try: complement the bits

- Example: $7_{10} = 00111_2 7_{10} = 11000_2$
- Called One's Complement
- Note: positive numbers have leading 0s, negative numbers have leadings 1s.Binary

00000 00001 ... 01111 dometer

- What is -00000 ? Answer: 11111
- How many positive numbers in N bits?

How many negative numbers?

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Shortcomings of One's complement?

- Arithmetic still a somewhat complicated.
- Still two zeros
 - $0 \times 000000000 = +0_{ten}$
 - $0 \times FFFFFFFFF = -0_{ten}$
- Although used for a while on some computer products, one's complement was eventually abandoned because another solution was better.



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Standard Negative # Representation

- Problem is the negative mappings "overlap" with the positive ones (the two 0s). Want to shift the negative mappings left by one.
 - Solution! For negative numbers, complement, then add 1 to the result
- As with sign and magnitude, & one's compl. leading 0s ⇒ positive, leading 1s ⇒ negative
 - .000000...xxx is ≥ 0, 111111...xxx is < 0
 - except 1...1111 is -1, not -0 (as in sign & mag.)
- This representation is Two's Complement
 - This makes the hardware simple!

(C's int, aka a "signed integer")
(Also C's short, long long, ..., C99's intN t)

CSGIC LUZ Number Representation (16)
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Two's Complement Formula

 Can represent positive and negative numbers in terms of the bit value times a power of 2:

$$d_{31} \times (-(2^{31})) + d_{30} \times 2^{30} + ... + d_2 \times 2^2 + d_1 \times 2^1 + d_0 \times 2^0$$

• Example: 1101_{two} in a nibble?

$$= 1x-(2^3) + 1x2^2 + 0x2^1 + 1x2^0$$

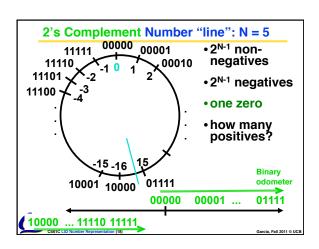
$$= -2^3 + 2^2 + 0 + 2^0$$

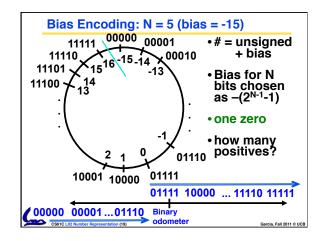
Example: -3 to +3 to -3 (again, in a nibble):

x : 1101
x' : 0010
two
+1 : 0011
two
() ': 1100
two
+1 : 1101
two



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How best to represent -12.75?

- a) 2s Complement (but shift binary pt)
- b) Bias (but shift binary pt)
- c) Combination of 2 encodings
- d) Combination of 3 encodings
- e) We can't

Shifting binary point means "divide number by some power of 2. E.g., $11_{10} = 1011.0_2 \implies 10.110_2 = (11/4)_{10} = 2.75_{10}$

META: We often make design And in summary... We represent "things" in computers as particular bit patterns: N bits ⇒ 2^N things These 5 integer encodings have different benefits; 1s complement and sign/mag have most problems. • unsigned (C99's uintN t): 00000 00001 ... 01111 10000 ... 11111 2's complement (C99's intN t) universal, learn! 00000 00001 ... 10000 ... 11110 11111 Overflow: numbers ∞; computers finite,errors!

META: Ain't no free lunch

REFERENCE: Which base do we use?

- Decimal: great for humans, especially when doing arithmetic
- Hex: if human looking at long strings of binary numbers, its much easier to convert to hex and look 4 bits/symbol
 - · Terrible for arithmetic on paper
- · Binary: what computers use; you will learn how computers do +, -, *, /
 - · To a computer, numbers always binary
 - · Regardless of how number is written:
 - $\cdot 32_{ten} == 32_{10} == 0 \times 20 == 100000_2 == 0 \text{b} 100000$
 - · Use subscripts "ten", "hex", "two" in book, slides when might be confusing

Two's Complement for N=32 $\begin{array}{c} \dots \\ 0.111 \dots 1111 & 1111 & 1111 & 1101_{\text{two}} = \\ 0.111 \dots 1111 & 1111 & 1111 & 1110_{\text{two}} = \\ 0.111 \dots 1111 & 1111 & 1111 & 1111_{\text{two}} = \\ 0.111 \dots 1111 & 1111 & 1111 & 1111_{\text{two}} = \\ 1.000 \dots 0.000 & 0.000 & 0.000_{\text{two}} = \\ 1.000 \dots 0.000 & 0.000 & 0.000_{\text{two}} = \\ 1.000 \dots 0.000 & 0.000 & 0.000_{\text{two}} = \\ 1.000 \dots 0.000 & 0.000 & 0.000_{\text{two}} = \\ 1.000 \dots 0.000 & 0.000 & 0.000_{\text{two}} = \\ 1.000 \dots 0.000 & 0.000 & 0.000_{\text{two}} = \\ 1.000 \dots 0.000 & 0.000 & 0.000_{\text{two}} = \\ 1.000 \dots 0.$ 2,147,483,645_{ten} 2,147,483,646_{ten} -2,147,483,647_{ten} -2,147,483,646_{ten} 1111 ... 1111 1111 1111 1101_{two} = 1111 ... 1111 1111 1111 1110_{two} = 1111 ... 1111 1111 1111 1111_{two} = One zero; 1st bit called sign bit 1 "extra" negative:no positive 2,147,483,648ten

Two's comp. shortcut: Sign extension

- Convert 2's complement number rep. using n bits to more than n bits
- Simply replicate the most significant bit (sign bit) of smaller to fill new bits
 - 2's comp. positive number has infinite 0s
 - · 2's comp. negative number has infinite 1s
 - · Binary representation hides leading bits; sign extension restores some of them
 - 16-bit -4_{ten} to 32-bit:

1111 1111 1111 1100_{two}

