# 61A LECTURE 22 -TAIL CALLS, ITERATORS

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#### **Announcements**

- · Homework 12 due Thursday, not Monday.
  - · Take the time to get started on the project instead!

#### Almost done with Scheme

- · Scheme is a lot simpler than Python, so it has a lot less features than Python does
- · Today we're talking about a feature that Scheme has that Python doesn't!

# Iteration Versus Recursion in Python

In Python, recursive calls always create new active frames

```
Time
                                                             Space
def factorial(n):
                                                 \Theta(n)
                                                              \Theta(n)
    if n == 0:
          return 1
    return n * factorial(n - 1)
                                                 \Theta(n)
                                                             \Theta(1)
def factorial(n):
    total = 1
while n > 0:
     n, total = n - 1, total * n
return total
```

Iteration and Recursion
Reminder: Iteration is a special case of recursion

Idea: The state of iteration can be passed as parameters

```
def factorial(n):
    total = 1 While n > 0: Local names become...
       n, total = n - 1, total * n
    return total
                   Parameters in a recursive function
def factorial(n, total):
    if n == 0:
    return factorial(n - 1, total * n)
```

But this converted version still uses linear space in Python

# Tail Recursion

From the  $Revised^7$  Report on the Algorithmic Language Scheme:

"Implementations of Scheme are required to be properly tail-recursive. This allows the execution of an iterative computation in constant space, even if the iterative computation is described by a syntactically recursive procedure."

```
(define (factorial n total)
 (if (= n \ 0) total
     def factorial(n, total):
   if n == 0:
      return total
   return factorial(n - 1, total * n)
```

#### Tail Calls

A procedure call that has not yet returned is *active*. Some procedure calls are *tail calls*. A Scheme interpreter should support an unbounded number of active tail calls.

A tail call is a call expression in a tail context:

- The last body sub-expression in a lambda expression
- Sub-expressions 2 & 3 in a tail context if expression
- All non-predicate sub-expressions in a tail context cond
- The last sub-expression in a tail context and or or
- The last sub-expression in a tail context begin

# **Eval with Tail Call Optimization**

The return value of the tail call is the return value of the current procedure call.

Therefore, tail calls shouldn't increase the environment size.

In the interpreter, recursive calls to **scheme\_eval** for tail calls must instead be expressed iteratively.

#### Break!



Guido van Rossum "Benevolent Dictator for Life"

- · Remember this guy?
- · Guido on tail call optimization:
- "Personally, I think it is a fine feature for some languages, but I don't think it fits Python"
- · Why do you think this is?

### **Our Sequence Abstraction**

Recall our previous sequence interface:

- A sequence has a finite, known length
- A sequence allows element selection for any element

In the cases we've seen so far, satisfying the sequence interface requires storing the entire sequence in a computer's memory

#### Problems?

- Infinite sequences primes, positive integers
- Really large sequences all Twitter tweets, votes in a presidential election

# The Sequence of Primes

Think about the sequence of prime numbers:

- What's the first one?
- The next one?
- The next one?
- How about the next two?
- How about the 105<sup>th</sup> prime?
  - Our sequence abstraction would give an instant answer

# Implicit Sequences

- We compute each of the elements on demand
- · Don't explicitly store each element
- Called an implicit sequence

# A Python Example

**Example**: The range class represents a regular sequence of integers

- The range is represented by three values: start, end, and step
- The length and elements are computed on demand
- Constant space for arbitrarily long sequences

$$\begin{split} length &= max \left( \left\lceil \frac{end - start}{step} \right\rceil, 0 \right) \\ elem(k) &= start + k \cdot step \quad \text{(for } k \in [0, length) \text{)} \end{split}$$

#### The Iterator Interface

An iterator is an object that can provide the next element of a (possibly implicit) sequence

The iterator interface has two methods:

- \_\_iter\_\_(self) returns an equivalent iterator
- \_\_next\_\_(self) returns the next element in the sequence
  - If no next, raises StopIteration exception

There are also built in functions  ${\bf next}$  and  ${\bf iter}$  that call the corresponding method on their argument.



```
Rangelter
class RangeIter(object):
    def __init__(self, start, end, step):
        self.current = start
        self.current = start
        self.step = step
        self.sign = 1 if step > 0 else -1

def __next__(self):
        if self.current * self.sign >= self.end * self.sign:
            raise StopIteration
        result = self.current
        self.current += self.step
        return result

def __iter__(self):
        return self
```