61A LECTURE 4 – ENVIRONMENTS 2

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Announcements

- Homework 1 is due tonight, by 11:59pm!
  - Make sure you leave yourself some time to figure out how submission works!
- Homework 2 is out, due Monday by 11:59
- And expect Homework 3 released sometime this weekend…
- Work on the project!

Congratulations!

- You've almost made it through your first week of 61A!
- Just one more day to go!

Higher-Order Functions

Functions are first-class: they can be manipulated as values in Python

Higher-order function: a function that takes a function as an argument value or returns a function as a return value

Higher order functions:

- Express general methods of computation
- Remove repetition from programs
- Separate concerns among functions

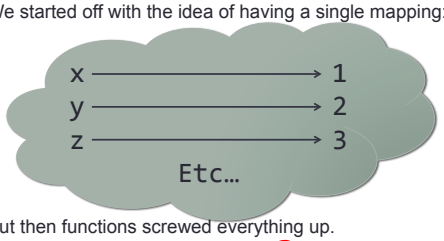
First, some review…

Draw this environment diagram:

```
x = 3

def of_duty()
    return x + 1

def me_maybe(x):
    return of_duty() * x

me_maybe(5)
```

Remember…

- We started off with the idea of having a single mapping:

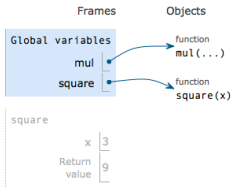


- But then functions screwed everything up.

Remember…

- Then we used environment diagrams (v0.1)…

```
1 from operator import mul
2 def square(x):
3     return mul(x, x)
4 square(3)
```



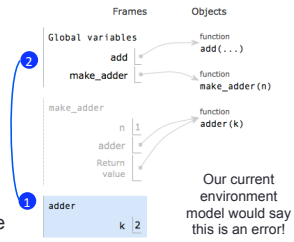
- …but even the almighty environment diagram isn't good enough (yet)

Functions screw everything up again!

- More specifically, higher-order functions!

```
1 from operator import add
2
3 def make_adder(n):
4     def adder(k):
5         return add(n, k)
6     return adder
7
8 make_adder(1)(2)
```

Where does n come from?



Our current environment model would say this is an error!

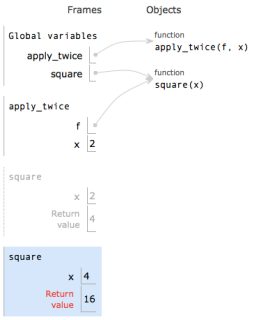
- Old model is inadequate

Environments and higher-order functions

- **Higher-order function:** a function that takes a function as an argument value or returns a function as a return value
  - **Functions as arguments:**
    - The environment model we learned already handles that!
    - We'll discuss an example today
  - **Functions as return values:**
    - We need to extend our model a little
    - Change: functions need to know where they were defined
    - Most things stay the same

Functions as arguments

```
1 def apply_twice(f, x):
2     return f(f(x))
3
4 def square(x):
5     return x * x
6
7 result = apply_twice(square, 2)
```



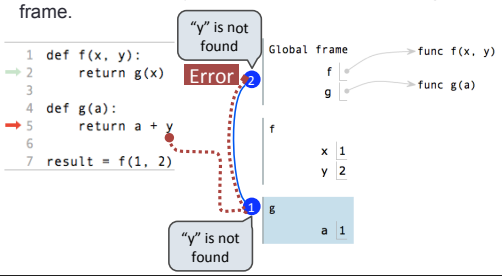
Demo: http://goo.gl/CBLjw

Break!

Environments for non-nested functions (review)

- The environment during a call to a non-nested function consists of the newly created local frame and the global frame.

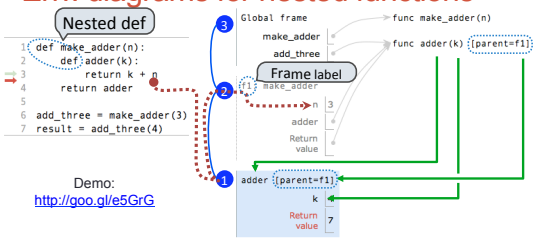
```
1 def f(x, y):
2     return g(x)
3
4 def g(a):
5     return a + y
6
7 result = f(1, 2)
```



What changes with nested functions?

- This is the most important slide of the lecture
- **Before:**
  - The environment during a function call consists of the new local frame and the global frame
  - Check the local frame
  - If not there, check the global frame
- **Now:**
  - The environment during a function call consists of the new local frame and *the environment in which the function was defined*
  - Check the local frame
  - If not there, check the rest of the environment

Env. diagrams for nested functions



Demo: http://goo.gl/e5GrG

Every user-defined function has a parent frame

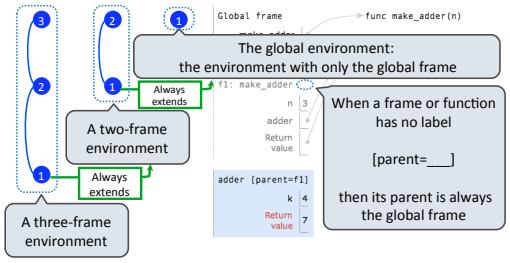
The parent frame of a function is the frame in which it was defined

Every local frame has a parent frame

The parent of a local frame is the parent of the function called

The structure of environments

A frame extends the environment that begins with its parent



How to draw an environment diagram

When defining a function:

Create a function value with signature <name>(<formal parameters>)

For nested definitions, label the parent as the first frame of the current environment

Bind <name> to the function value in the first frame of the current environment

When calling a function:

1. Add a local frame labeled with the <name> of the function
2. If the function has a parent label, copy it to this frame
3. Bind the <formal parameters> to the arguments in this frame
4. Execute the body of the function in the environment that starts with this frame

Example: function composition

- You may be familiar with function composition from your math classes…

Composition operator

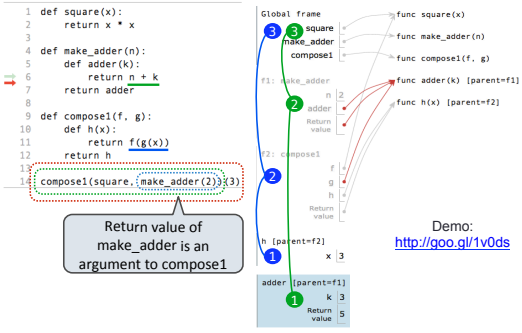
$$h = f \circ g$$

One output function — Two input functions

$$h(x) = f(g(x))$$

- Code example!

Environment for function composition



Demo: http://goo.gl/1v0ds

Closing remarks…

- We basically only changed one thing: functions now keep an additional bit of information
- With this, your environment model is now complete!
- Practice makes perfect
- Remember it well – if you ever can't figure out why a variable has a certain value, draw the diagram!