## CS 61A Structure and Interpretation of Computer Programs Summer 2013

## INSTRUCTIONS

- You have 2 hours to complete the exam.
- The exam is closed book, closed notes, closed computer, closed calculator, except one hand-written 8.5 " $\times 11^{\prime \prime}$ crib sheet of your own creation and the official 61A midterm 1 study guide attached to the back of this exam.
- Mark your answers ON THE EXAM ITSELF. If you are not sure of your answer you may wish to provide a brief explanation.

| Last name |  |
| :--- | :--- |
| First name |  |
| SID |  |
| Login |  |
| TA \& section time |  |
| Name of the person to <br> your left |  |
| Name of the person to <br> your right |  |
| All the work on this exam <br> is my own. (please sign) |  |

## 1. (9 points) Do you feel lucky, punk?

For each of the following expressions, write the value to which it evalutes in the interactive Python interpreter. The first two rows have been provided as examples.

- In the Evaluates to column, write the value to which the expression evaluates. If it evaluates to a function value, write Function. If evaluation causes an error, write Error.

Assume that you have started Python 3 and executed the following statements:

```
lucky = [3, 4, 5, 6, 7]
beginning = [lucky, [3, 4, 5, 6, 7]]
punk = beginning[1]
```

| Expression | Evaluates to |
| :--- | :---: |
| $3+3$ | 6 |
| $1 / 0$ | ERROR |
| lucky [1] |  |
| beginning[1] == lucky |  |
| beginning[1] is lucky |  |
| punk[2:] |  |
| punk == lucky |  |

Now, assume the following line is executed in the same interpreter session:

```
beginning[0].append(10)
```

| Expression | Evaluates to |
| :--- | :--- |
| lucky |  |
| beginning[0] |  |
| beginning[1] |  |
| punk == lucky |  |

## 2. (6 points) Not with a fizzle, but with a bang

(a) $(2 \mathrm{pt})$ Consider the following function definition.

```
def fizzle(n):
        if n <= 0:
            return n
        elif n % 23 == 0:
            return n
        return fizzle(n - 1)
```

Circle the correct order of growth for a call to fizzle(n):

$$
\begin{array}{lllllll}
\Theta(1) & \Theta(\log n) & \Theta(\sqrt{n}) & \Theta(n) & \Theta\left(n^{2}\right) & \Theta\left(n^{3}\right) & \Theta\left(2^{n}\right)
\end{array}
$$

(b) ( 2 pt ) Now consider the following function definitions.

```
def boom(n):
    if n == 0:
            return "BOOM!"
        return boom(n - 1)
def explode(n):
    if n == 0:
            return boom(n)
        i = 0
        while i < n:
            boom(n)
            i += 1
        return boom(n)
```

Circle the correct order of growth for a call to explode ( $n$ ):
$\Theta(1)$
$\Theta(\log n)$
$\Theta(\sqrt{n})$
$\Theta(n)$
$\Theta\left(n^{2}\right)$
$\Theta\left(n^{3}\right)$
$\Theta\left(2^{n}\right)$
(c) $(2 \mathrm{pt})$ Now consider the following function definition.

```
def dreams(n):
    if n<= 0:
        return n
        if n > 0:
            return n + dreams(n // 2)
```

Circle the correct order of growth for a call to dreams ( n ):
$\Theta(1)$
$\Theta(\log n)$
$\Theta(\sqrt{n})$
$\Theta(n)$
$\Theta\left(n^{2}\right)$
$\Theta\left(n^{3}\right)$
$\Theta\left(2^{n}\right)$

## 3. (12 points) Cupcakes cupcakes cupcakes cupcakes cupcakes

(a) ( $6 \mathbf{p t}$ ) Fill in the environment diagram that results from executing the code below until the entire program is finished, an error occurs, or all frames are filled. You need only show the final state of each frame. You may not need to use all of the spaces or frames.
A complete answer will:

- Add all missing names, labels, and parent annotations to all local frames.
- Add all missing values created during execution.
- Show the return value for each local frame.

```
def cup(cake):
    if len(cake) != 1:
        frosting = cake.pop(0)
        cup(cake)
        cake.append(frosting)
frosting = [1, 2, 3]
cup(frosting)
```






(b) ( $6 \mathbf{p t}$ ) Fill in the environment diagram that results from executing the code below until the entire program is finished, an error occurs, or all frames are filled. You need only show the final state of each frame. You may not need to use all of the spaces or frames.
A complete answer will:

- Add all missing names, labels, and parent annotations to all local frames.
- Add all missing values created during execution.
- Show the return value for each local frame.



## 4. (4 points) Good job, Mark

Mark is tired of having to dig around BearFacts to look up student information, so he wrote a script to create a dictionary of student info. However, when he did so, he was sleep-deprived. As such, he accidentally swapped the keys and the values! Now he's stuck with a dictionary that maps any single piece of student information to the student's login:

```
>>> info['Eric Tzeng'] # info is mark's faulty dictionary
'cs61a-ta'
>>> info['eric.tzeng@berkeley.edu']
'cs61a-ta'
```

Mark is too tired to fix this, so you'll have to do it for him. We'll do this by writing a get_info function. It should take a student login string and a faulty info dictionary as its two arguments and return a list containing all of that student's information. The returned list can contain a student's information in any order, but it must contain all of the information for a student found in the faulty dictionary.

```
>>> get_info('cs61a-ta', info)
['Eric Tzeng', 'eric.tzeng@berkeley.edu']
```

You may assume that no two students have duplicate information. However, you may not assume that names and emails are the only pieces of information stored in the dictionary.

```
def get_info(login, info_dict):
    """Retrieve student information based on the student's login, using the
    provided (faulty) info_dict.
    >>> mark_dict = {'Andrew Huang': 'cs61a-tf', 'awesomeandrew@example.com': 'cs61a-tf',
    ... 'Robert Huang': 'cs61a-td', 'coolrob42@example.com': 'cs61a-td'}
    >>> get_info('cs61a-td', mark_dict)
    ['Robert Huang', 'coolrob42@example.com'] # order doesn't matter
    >>> get_info('cs61a-tf', mark_dict)
    ['awesomeandrew@example.com', 'Andrew Huang'] # order doesn't matter
    """
```


## 5. (5 points) Express yourself

In the first week of class, we learned that expressions like mul (sub (4, 5), add (2, 3)) can be represented as expression trees. In this problem we use our Tree data structure to further explore this idea.
We propose representing expressions using a binary tree such as the Tree class you have seen in lecture. In this binary tree representation, leaves always represent atomic values such as 2 or True, and non-leaf nodes always represent function calls. For example, the expression mul (sub (4, 5), add (2, 3)) corresponds to the following binary expression tree:


Write a function evaluate, which takes a binary expression Tree and returns what that expression would evaluate to. You may assume that all operators will take exactly 2 arguments, and that nodes always have either 0 or 2 children (never 1).
The class definition for Tree can be found in the midterm study guide.

```
def evaluate(exp):
    """Evaluates exp, which is an expression tree.
    >>> from operator import add, sub, mul
    >>> exp = Tree(3) # 3
    >>> evaluate(exp)
    3
    >>> exp = Tree(add, Tree(3), Tree(4)) # add(3, 4)
    >>> evaluate(exp)
    7
    >>> exp = Tree(mul,
    ... Tree(add, Tree(3), Tree(5)),
    ... Tree(sub, Tree(5), Tree(2))) # mul(add(3, 5), sub(5, 2))
    >>> evaluate(exp)
    24
    """
```


## 6. (8 points) The private life of Albert Wu

Albert keeps all of his top secret information in a binary tree. This prevents the layperson from reading his data. However, well trained computer scientists (such as you) can still access his information.

As a further layer of protection, Albert turns some of the nodes in his trees into Eert nodes. Eert nodes, which have Tree as their base class, are like normal Tree nodes, except they swap their left and right branches. (Albert settles for nothing less than the most advanced encryption techniques known to man.)
(a) (3 pt) Complete the __init__ method for the Eert class on the next page. Make sure to use inheritance as much as possible. The Eert class should work as follows:

```
>>> e = Eert("61A account info",
... Tree("Username: cs61a-te"),
... Tree("Password: imsocool"))
>>> e.entry # unchanged
"61A account info"
>>> e.left.entry # swapped with right
"Password: imsocool"
>>> e.right.entry # swapped with left
"Username: cs61a-te"
```

(b) (5 pt) Complete the definitions of the decrypt methods for both the Tree and Eert classes on the next page. When the decrypt method is invoked on a binary tree containing Tree and Eert nodes, it returns a copy of the binary tree, but with all Eert nodes replaced with Tree nodes. During this replacement, you should also swap the left and the right back to their proper positions! Here is a graphical representation of the process:

Original:


Decrypted:


In terms of actual Python code, it should work as follows:

```
>>> old = Tree("League of Legends accounts",
... Eert("Main account", # swaps username and password positions
... Tree("Username: citrusdrink"),
... Tree("Password: imdiamond1")),
... Tree("Smurf account",
... Tree("Username: yummycitrusdrink"),
... Eert("Password: ishouldbeapro"))) # no children, so no swapping
>>> new = old.decrypt()
>>> old.left.left.entry # this got swapped because of the Eert
"Password: imdiamond1"
>>> new.left.left.entry # no longer swapped
"Username: citrusdrink"
>>> old.right.right.entry
"Password: ishouldbeapro"
>>> new.right.right.entry
"Password: ishouldbeapro"
```

```
class Tree(object):
    def __init__(self, entry, left=None, right=None):
        self.entry = entry
        self.left = left
        self.right = right
    def decrypt(self):
        "*** PART B ***"
```

class Eert(Tree):
def __init__(self, entry, left=None, right=None):
"*** PART A ***"
def decrypt(self):
"*** PART B ***"
7. (6 points) kp it

Complete the definition of the skip procedure in Scheme. The skip procedure should take a list as its only argument and return a copy of the list with every other element removed, beginning with the first element:

```
STk> (skip '(1 2 3 4 5))
(2 4)
STk> (skip '(a (b c) d e))
((b c) e)
STk> (skip '(50))
()
```

(define (skip lst)
8. (0 points) Express yourself (v2)

Express your feelings in the space below through your choice of creative medium, such as poetry or illustration.

