# CS61A Lecture 21 

## Amir Kamil <br> UC Berkeley March 11, 2013

## Announcements

- HW7 due on Wednesday
$\square$ Ants project out


## Looking Up Names

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withdraw_fee = 1
def withdraw(self, amount): return Account.withdraw(self, amount + withdraw_fee)

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Not all languages work this way


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A function might want to operate on multiple data types.

Message passing enables us to accomplish all of the above, as we will see today and next time

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Strings are important: they represent language and programs.
In Python, all objects produce two string representations:

- The "str" is legible to humans.
-The "repr" is legible to the Python interpreter.
When the "str" and "repr" strings are the same, that's evidence that a programming language is legible by humans!

The "repr" String for an Object

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>>> repr(min)
'<built-in function min>'

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The result of calling str on the value of an expression is what Python prints using the print function.

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```
>>> today.
```

$\qquad$

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``` \(\qquad\)
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'2012-10-08'
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## Inheritance and Polymorphism

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98
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Classes that implement __repr__ and __str__ methods that return Python- and human-readable strings thereby implement an interface for producing Python string representations.

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Classes that implement __repr__ and __str__ methods that return Python- and human-readable strings thereby implement an interface for producing Python string representations.

Classes that implement __len__ and __getitem__ are sequences.

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+, +=
[], []=
 getitem__, __setitem $\qquad$ __getattr__, __getattribute $\qquad$ setattr $\qquad$
a[i] is equivalent to type(a).__getitem__(a, i)

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    def __repr__(self):
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    def __str__(self):
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    def __add__(self, num):
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    def __add__(self, num):
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        numer1 = self.numerator * num.denominator
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                                    self.denominator)
    def __add__(self, num):
        denom = self.denominator * num.denominator
        numer1 = self.numerator * num.denominator
        numer2 = self.denominator * num.numerator
        return Rational(numer1 + numer2, denom)
```


## Example: Rational Numbers

```
class Rational(object):
    def __init__(self, numer, denom):
    g = gcd(numer, denom)
    self.numerator = numer // g
    self.denominator = denom // g
def __repr__(self):
    return 'Rational({0}, {1})'.format(self.numerator,
                                    self.denominator)
def __str__(self):
    return '{0}/{1}'.format(self.numerator,
                                    self.denominator)
    def ___add__(self, num):
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    def __eq__(self, num):
        return (self.numerator == num.numerator and
        self.denominator == num.denominator)
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The @property decorator on a method designates that it will be called whenever it is looked up on an instance.

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The @property decorator on a method designates that it will be called whenever it is looked up on an instance.

It allows zero-argument methods to be called without an explicit call expression.

