

# CS61A Lecture 17

Amir Kamil UC Berkeley March 1, 2013



#### □ HW6 due next Thursday

#### □ Trends project due on Tuesday

- □ Partners are required; find one in lab or on Piazza
- □ Will not work in IDLE
- New bug submission policy; see Piazza







Sometimes, removing repetition requires restructuring the code

```
def find_quadratic_root(a, b, c, plus=True):
    """Applies the quadratic formula to the polynomial
    ax^{2} + bx + c.""
    if plus:
        return (-b + sqrt(square(b) - 4 * a * c)) / (2 * a)
    else:
        return (-b - sqrt(square(b) - 4 * a * c)) / (2 * a)
def find_quadratic_root(a, b, c, plus=True):
    """Applies the quadratic formula to the polynomial
    ax^{2} + bx + c."""
    disc_term = sqrt(square(b) - 4 * a * c)
    if not plus:
        disc term *= -1
    return (-b + disc_term) / (2 * a)
```



Write the test of a function before you write a function

A test will clarify the (one) job of the function Your tests can help identify tricky edge cases

Develop incrementally and test each piece before moving on

You can't depend upon code that hasn't been tested Run your old tests again after you make new changes

## **Hog Contest**



#### Contest rules:

- □ All entries run against every other entry
- $\Box$  An entry wins a match if its true win rate is > 0.5
- All strategies must be deterministic, pure functions and must not use pre-computed data
- Extra credit for entries with the most wins or the highest cumulative win rate
- Total of 54 valid submissions

We used **itertools.combinations** to determine the set of matches



Congratulations to the team of Colin Lockard and Sherry Xu, who achieved a perfect 53-0 record <u>and</u> the highest win rate (28.77)!

Second-most wins (51-2): Eric Holt and Anna Carey

Second-highest win rate (28.70): Don Mai and Jeechee Chen

Third-highest in both (50-3, 28.67): Sean Scofield and Frank Lu

Complete rankings will be posted on the website

## **Computing Win Rates Exactly**



A state in the game: (who rolls next?, player score, opponent score)



Requires access to both strategies, which must be deterministic



Optimal strategy given an opponent:

- At each state, compute probability of winning for each allowed number of dice
- Choose the number of dice that maximizes the probability

The perfect strategy: use iterative improvement!

- □ Initial guess: always roll 5
- □ Update to: optimal opponent of current strategy
- Done when: 0.5 win rate against optimal opponent

Takes only 16 steps to converge!

Can also compute perfect strategy directly using table

## A Function with Evolving Behavior



Let's model a bank account that has a balance of \$100



#### **Persistent Local State**





Example: http://goo.gl/5LZ6F

## **Reminder: Local Assignment**





Execution rule for assignment statements:

- 1. Evaluate all expressions right of =, from left to right.
- 2. Bind the names on the left the resulting values in the first frame of the current environment.



def make\_withdraw(balance):

"""Return a withdraw function with a starting balance."""

def withdraw(amount):

nonlocal balance

if amount > balance:

```
return 'Insufficient funds'
```

balance = balance - amount

return balance

return withdraw



Re-bind balance where it was bound previously



nonlocal <name>, <name 2>, ...

Effect: Future assignments to that name change its pre-existing binding in the **first non-local frame** of the current environment in which that

name is bound.

Python Docs: an "enclosing scope"

From the Python 3 language reference:

Names listed in a <u>nonlocal</u> statement must refer to pre-existing bindings in an enclosing scope. Names listed in a nonlocal <u>statement</u> must not collide with pre-existing bindings in the local scope.

http://docs.python.org/release/3.1.3/reference/simple\_stmts.html#the-nonlocal-statement

http://www.python.org/dev/peps/pep-3104/

# Effects o

Effects of Assignn	nent Statements
Status <ul> <li>No nonlocal statement</li> <li>"x" is not bound locally</li> </ul>	Effect Create a new binding from name "x" to object 2 in the first frame of the current environment.
<ul> <li>No nonlocal statement</li> <li>"x" is bound locally</li> </ul>	Re-bind name "x" to object 2 in the first frame of the current env.
<ul> <li>nonlocal x</li> <li>"x" is bound in a non-local frame</li> </ul>	Re-bind "x" to 2 in the first non-local frame of the current environment in which it is bound.
<ul> <li>nonlocal x</li> <li>"x" is not bound in a non- local frame</li> </ul>	SyntaxError: no binding for nonlocal 'x' found
<ul> <li>nonlocal x</li> <li>"x" is bound in a</li> </ul>	SyntaxError: name 'x' is parameter and nonlocal

• "x" is bound in a non-local frame

• "x" also bound locally

$$\mathbf{x} = 2$$



Python pre-computes which frame contains each name before executing the body of a function.

Therefore, within the body of a function, all instances of a name must refer to the same frame.



UnboundLocalError: local variable 'balance' referenced before assignment



Mutable values can be changed without a nonlocal statement.



Example: <u>http://goo.gl/cEpmz</u>

### **Creating Two Withdraw Functions**



Example: <u>http://goo.gl/glTyB</u>

#### Multiple References to a Withdraw Function







- Ability to maintain some state that is local to a function, but evolves over successive calls to that function.
- The binding for balance in the first non-local frame of the environment associated with an instance of withdraw is inaccessible to the rest of the program.
- An abstraction of a bank account that manages its own internal state.







Expressions are referentially transparent if substituting an expression with its value does not change the meaning of a program.



mul(add(2, mul(4, 6)), 3)
mul(add(2, 24 ), 3)
mul( 26 , 3)



Mutation is a *side effect* (like printing)

Side effects violate the condition of referential transparency because they do more than just return a value; they change the state of the computer.