

Code:

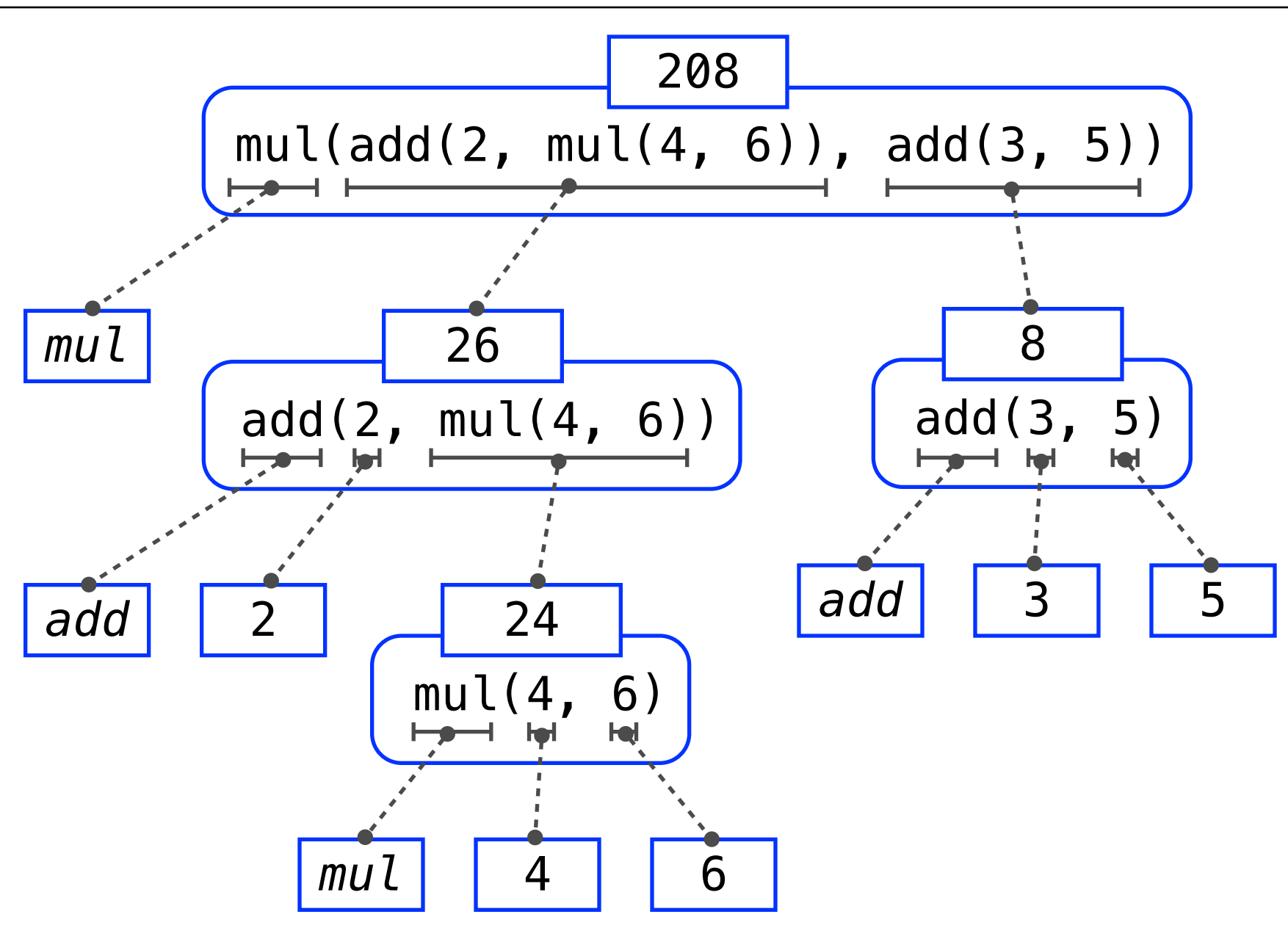
```

1 from math import pi
2 tau = 2 * pi

```

Frames:

A name is bound to a value
In a frame, there is at most one binding per name



Pure Functions

- 2 → `abs(number):` → 2
- 2, 10 → `pow(x, y):` → 1024

Non-Pure Functions

- 2 → `print(...):` → None

display "-2"

Code:

```

1 from operator import mul
2 def square(x):
3     return mul(x, x)
4 square(-2)

```

Frames:

- Global frame: `mul` → `func mul(...)`, `square` → `func square(x)`
- Local frame: `square` (parent: Global frame), `x` → -2, `Return value` → 4

Defining:

```

>>> def square(x):
      return mul(x, x)

```

Call expression: `square(2+2)`

- operator: `square`
- function: `square`
- operand: `2+2`
- argument: `4`

Defining:

```

>>> def square(x):
      return mul(x, x)

```

Calling/Applying:

```

4 square(x):
   return mul(x, x)

```

Argument: `x`, Return value: `16`

Compound statement

```

<header>:
<statement>
...
<separating header>:
<statement>
<statement>
...

```

Code:

```

def abs_value(x):
1 statement,
3 clauses,
3 headers,
3 suites,
2 boolean contexts
if x > 0:
    return x
elif x == 0:
    return 0
else:
    return -x

```

A name evaluates to the value bound to that name in the earliest frame of the current environment in which that name is found.

```

1 from operator import mul
2 def square(x):
3     return mul(x, x)
4 square(square(3))

```

```

1 def f(x, y):
2     return g(x)
3
4 def g(a):
5     return a + y
6
7 result = f(1, 2)

```

Global frame: `f` → `func f(x, y)`, `g` → `func g(a)`

Local frame: `f` (parent: Global frame), `x` → 1, `y` → 2, `a` → 1

Error: "y" is not found

- An environment is a sequence of frames
- An environment for a non-nested function (no def within def) consists of one local frame, followed by the global frame

Evaluation rule for call expressions:

- Evaluate the operator and operand subexpressions.
- Apply the function that is the value of the operator subexpression to the arguments that are the values of the operand subexpressions.

Applying user-defined functions:

- Create a new local frame with the same parent as the function that was applied.
- Bind the arguments to the function's formal parameter names in that frame.
- Execute the body of the function in the environment beginning at that frame.

Execution rule for def statements:

- Create a new function value with the specified name, formal parameters, and function body.
- Its parent is the first frame of the current environment.
- Bind the name of the function to the function value in the first frame of the current environment.

Execution rule for assignment statements:

- Evaluate the expression(s) on the right of the equal sign.
- Simultaneously bind the names on the left to those values, in the first frame of the current environment.

Execution rule for conditional statements:

Each clause is considered in order.

- Evaluate the header's expression.
- If it is a true value, execute the suite, then skip the remaining clauses in the statement.

Evaluation rule for or expressions:

- Evaluate the subexpression <left>.
- If the result is a true value *v*, then the expression evaluates to *v*.
- Otherwise, the expression evaluates to the value of the subexpression <right>.

Evaluation rule for and expressions:

- Evaluate the subexpression <left>.
- If the result is a false value *v*, then the expression evaluates to *v*.
- Otherwise, the expression evaluates to the value of the subexpression <right>.

Evaluation rule for not expressions:

- Evaluate <exp>; The value is True if the result is a false value, and False otherwise.

Execution rule for while statements:

- Evaluate the header's expression.
- If it is a true value, execute the (whole) suite, then return to step 1.

The global environment: the environment with only the global frame

When a frame or function has no label [parent=___] then its parent is always the global frame

A frame extends the environment that begins with its parent

Higher-order function: A function that takes a function as an argument value or returns a function as a return value

Nested def statements: Functions defined within other function bodies are bound to names in the local frame

```

def cube(k):
    return pow(k, 3)

def summation(n, term):
    """Sum the first n terms of a sequence.

    >>> summation(5, cube)
    255
    """
    total, k = 0, 1
    while k <= n:
        total, k = total + term(k), k + 1
    return total

```

Function of a single argument (not called term)

A formal parameter that will be bound to a function

The cube function is passed as an argument value

The function bound to term gets called here

$0 + 1^3 + 2^3 + 3^3 + 4^3 + 5^3$

