

61A Lecture 31

Wednesday, November 20

Announcements

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- Project 4 due Thursday 11/21 @ 11:59pm.

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- Extra reader office hours in 405 Soda this week.

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- Recursive art contest entries will be due Monday 12/2 @ 11:59pm (After Thanksgiving).

Declarative Languages

Databases

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toy_id	toy	color	cost	weight
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SQL is an example of a declarative programming language.

It separates *what* to compute from *how* it is computed.

The language interpreter is free to compute the result in any way it wants.

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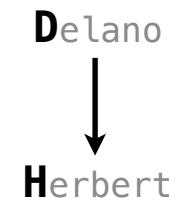
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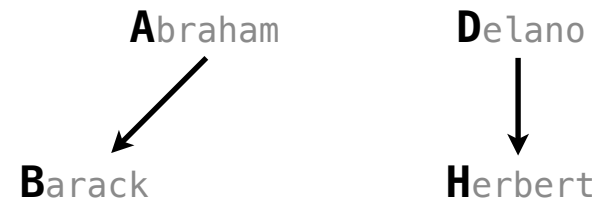
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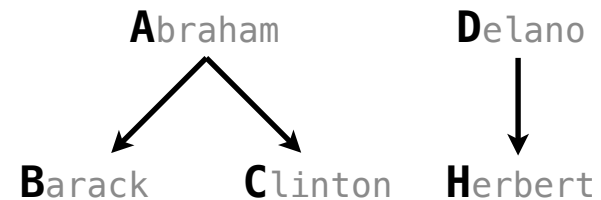
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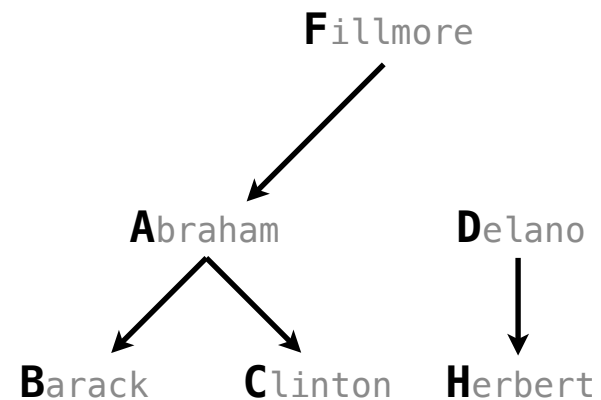
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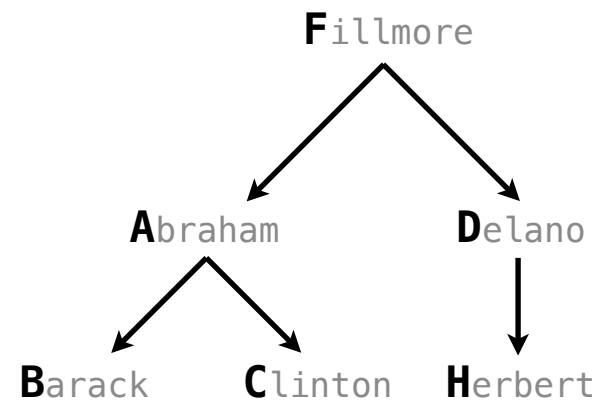
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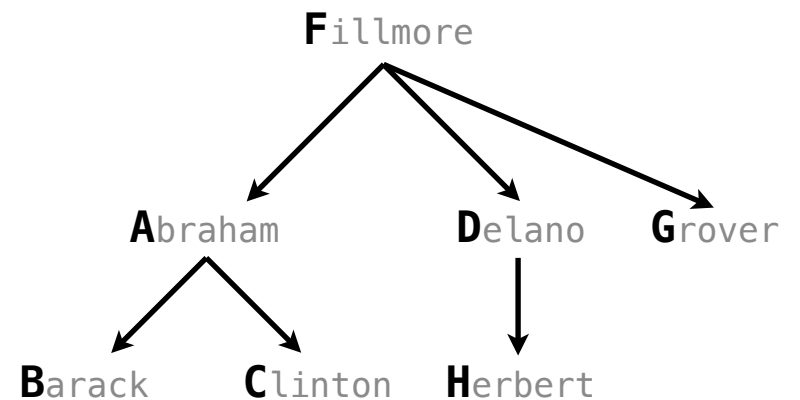
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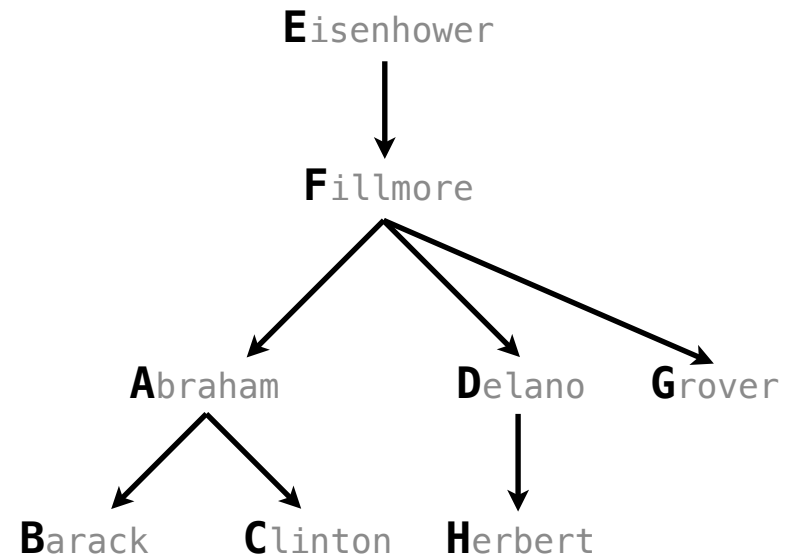
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( ? 1 2 3)      add
```

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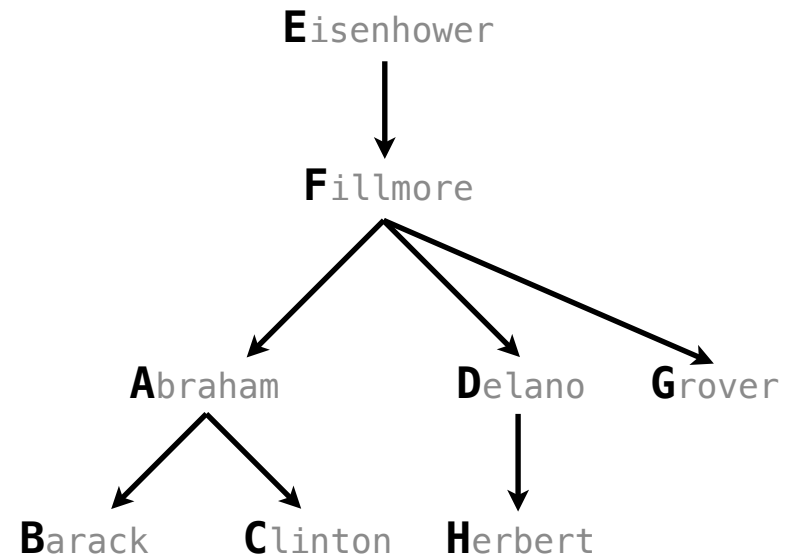
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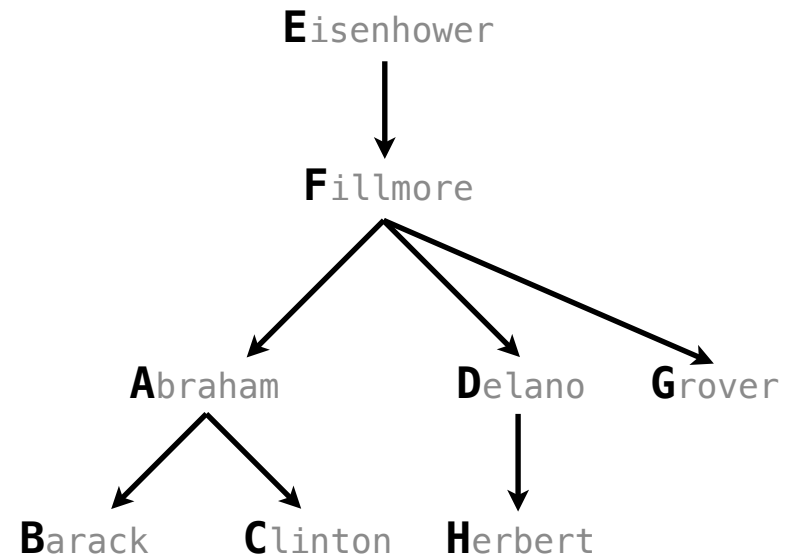


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logic> (fact (parent eisenhower fillmore))
logic> (query (parent abraham ?puppy))
```



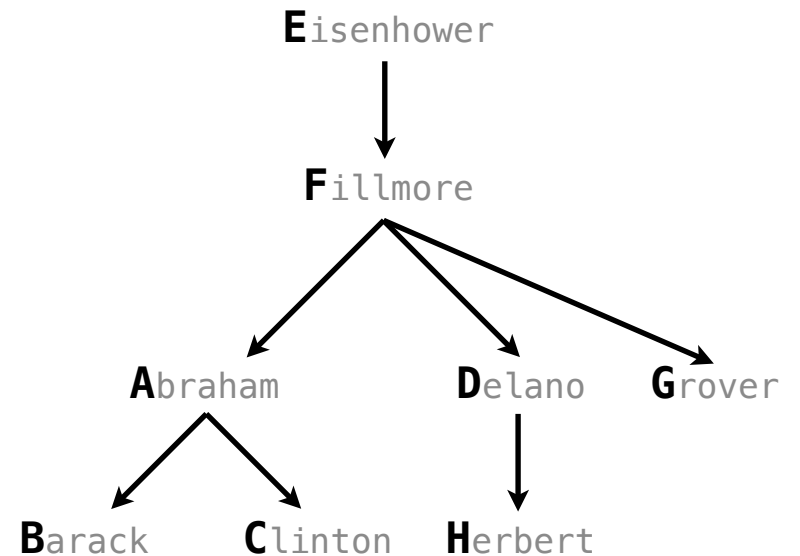
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A variable can
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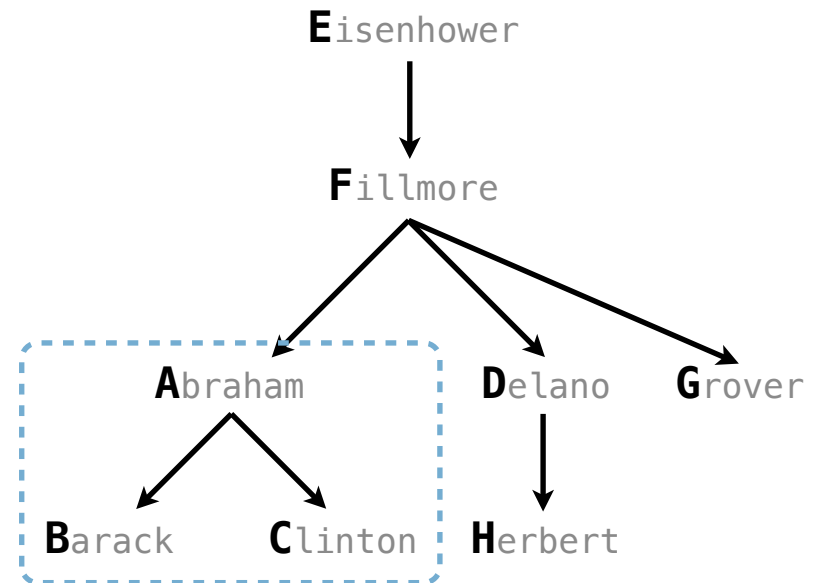
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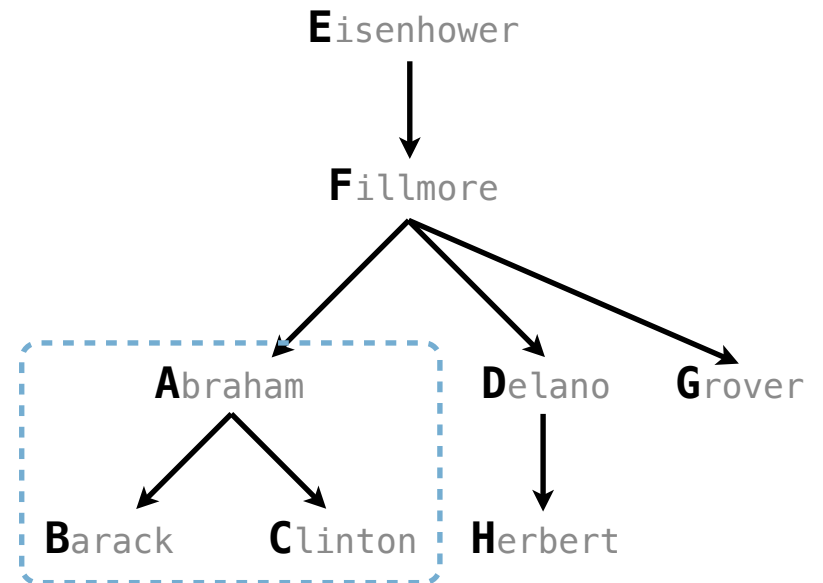
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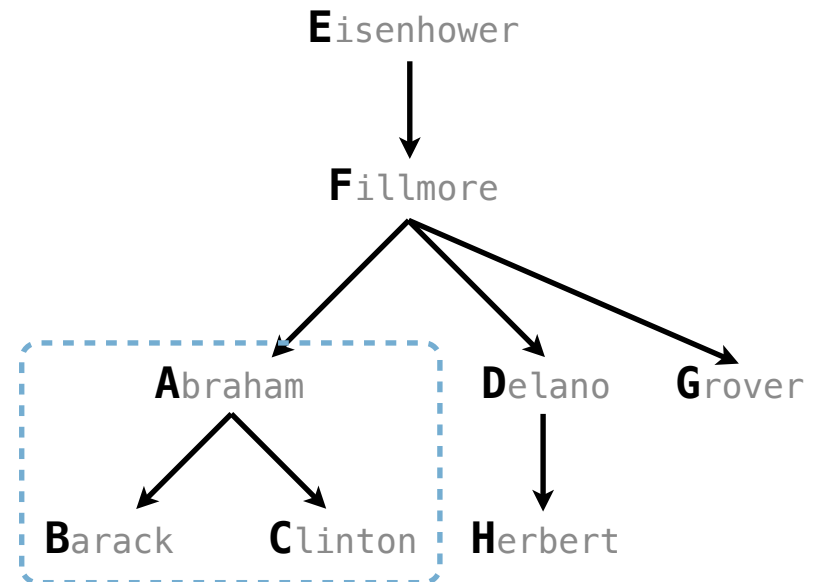
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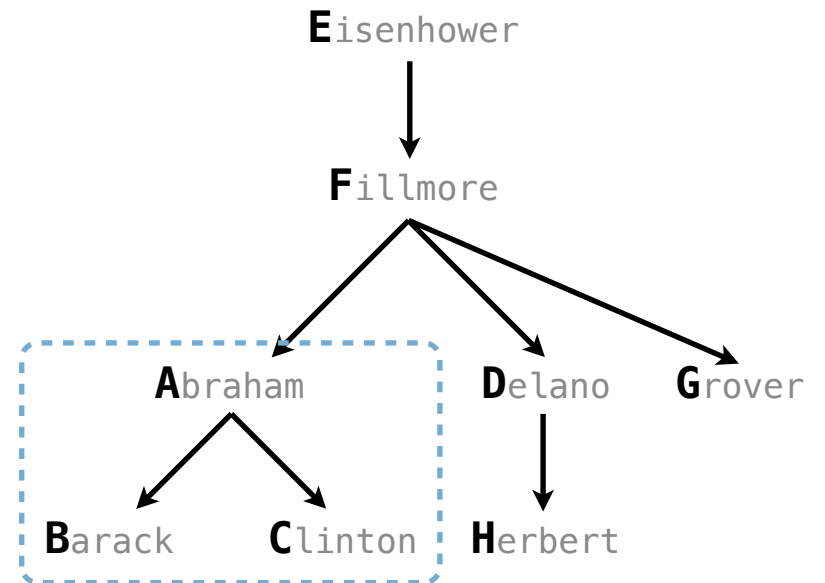
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A variable can have any name



Queries

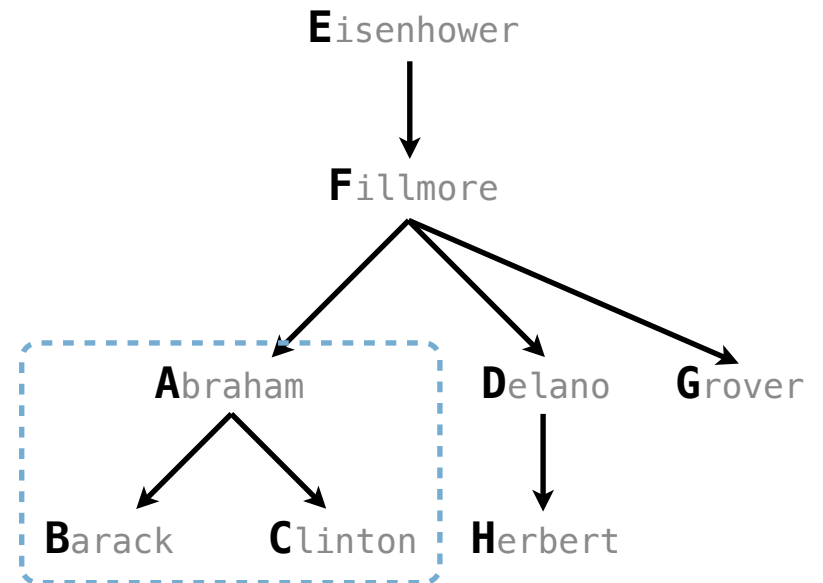
A *query* contains one or more relations that may contain variables.

Variables are symbols starting with **?**

```
logic> (fact (parent delano herbert))
logic> (fact (parent abraham barack))
logic> (fact (parent abraham clinton))
logic> (fact (parent fillmore abraham))
logic> (fact (parent fillmore delano))
logic> (fact (parent fillmore grover))
logic> (fact (parent eisenhower fillmore))
logic> (query (parent abraham ?puppy))
Success!
puppy: barack
puppy: clinton
```

A variable can have any name

Each line is an assignment of variables to values



Queries

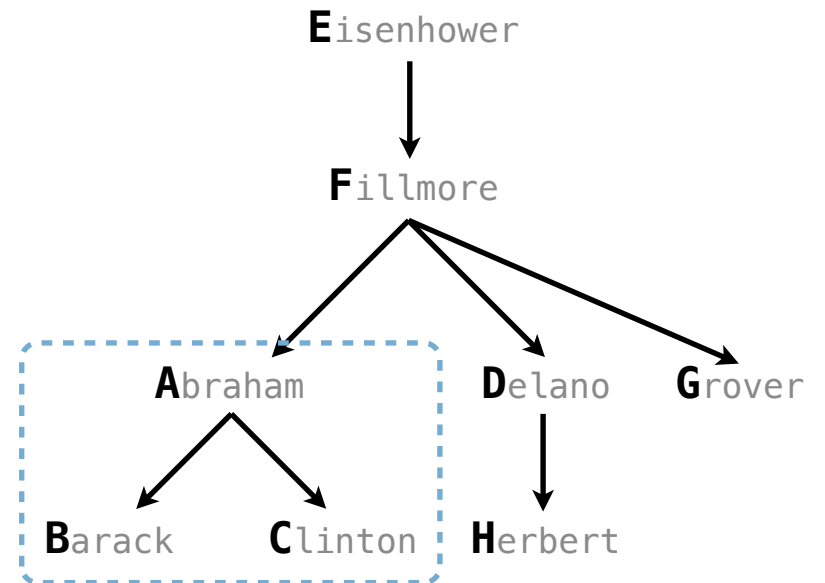
A *query* contains one or more relations that may contain variables.

Variables are symbols starting with **?**

```
logic> (fact (parent delano herbert))
logic> (fact (parent abraham barack))
logic> (fact (parent abraham clinton))
logic> (fact (parent fillmore abraham))
logic> (fact (parent fillmore delano))
logic> (fact (parent fillmore grover))
logic> (fact (parent eisenhower fillmore))
logic> (query (parent abraham ?puppy))
Success!
puppy: barack
puppy: clinton
```

A variable can have any name

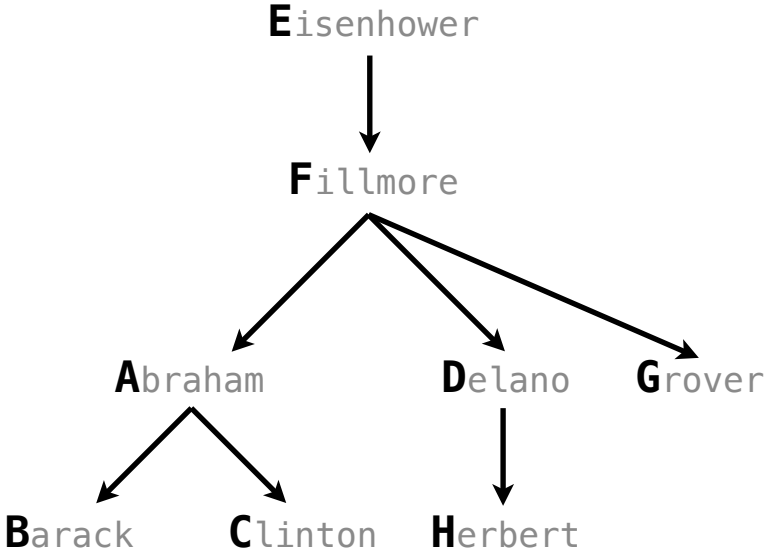
Each line is an assignment of variables to values



(Demo)

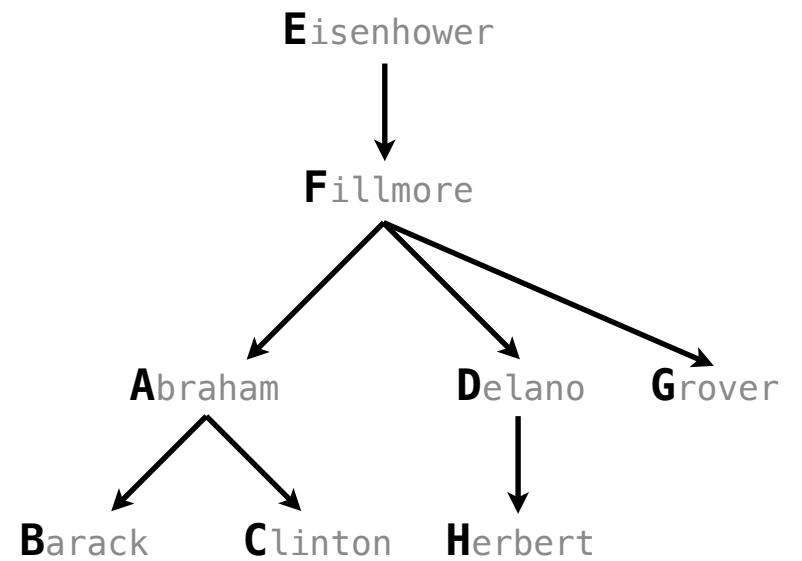
Compound Facts and Queries

Compound Facts



Compound Facts

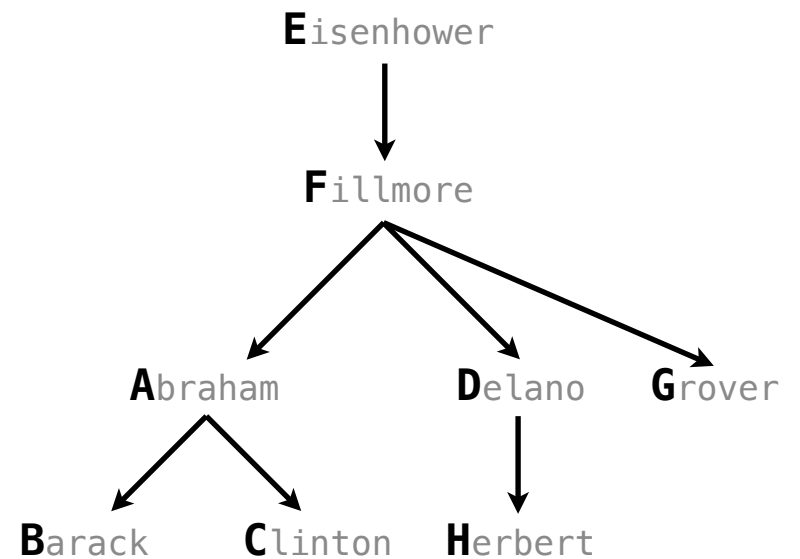
A fact can include multiple relations and variables as well.



Compound Facts

A fact can include multiple relations and variables as well.

(fact <conclusion> <hypothesis₀> <hypothesis₁> ... <hypothesis_N>)

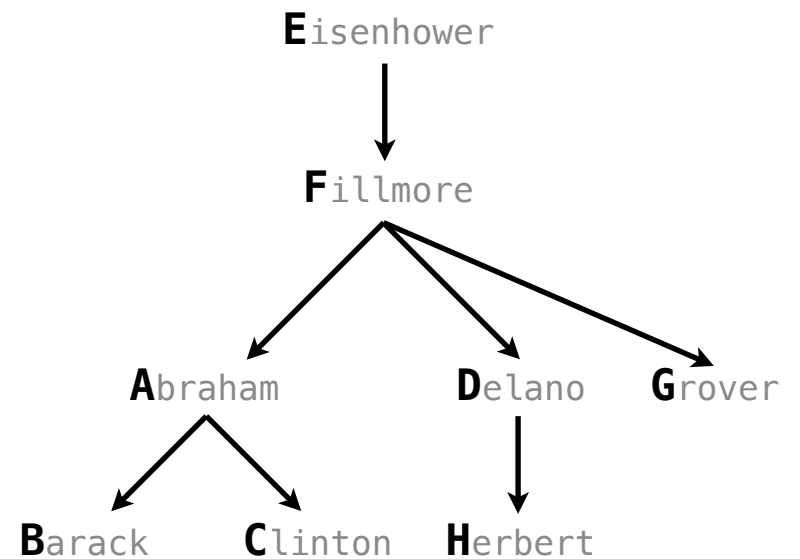


Compound Facts

A fact can include multiple relations and variables as well.

(fact <conclusion> <hypothesis₀> <hypothesis₁> ... <hypothesis_N>)

Means <conclusion> is true if all the <hypothesis_k> are true.



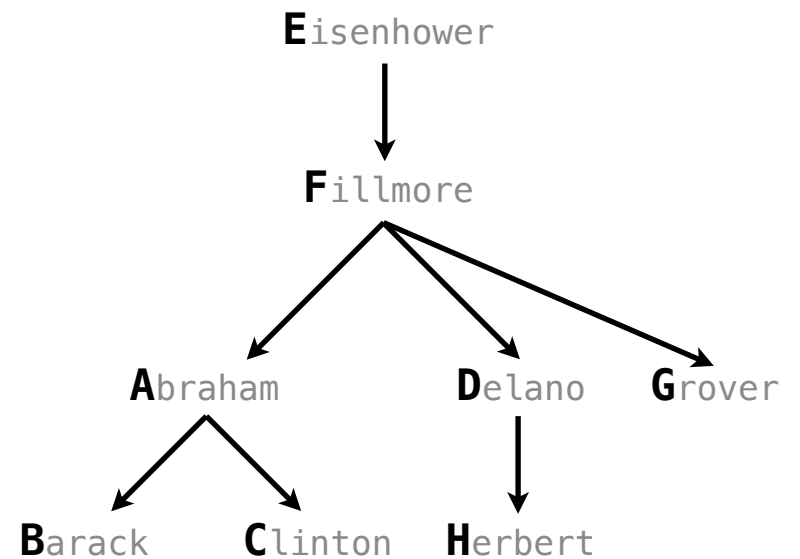
Compound Facts

A fact can include multiple relations and variables as well.

```
(fact <conclusion> <hypothesis0> <hypothesis1> ... <hypothesisN>)
```

Means <conclusion> is true if all the <hypothesis_k> are true.

```
logic> (fact (child ?c ?p) (parent ?p ?c))
```



Compound Facts

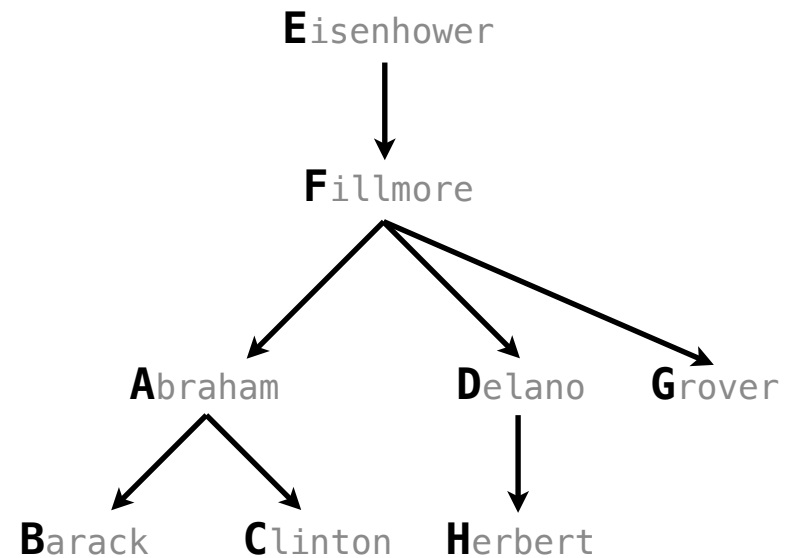
A fact can include multiple relations and variables as well.

```
(fact <conclusion> <hypothesis0> <hypothesis1> ... <hypothesisN>)
```

Means <conclusion> is true if all the <hypothesis_k> are true.

```
logic> (fact (child ?c ?p) (parent ?p ?c))
```

```
logic> (query (child herbert delano))
```



Compound Facts

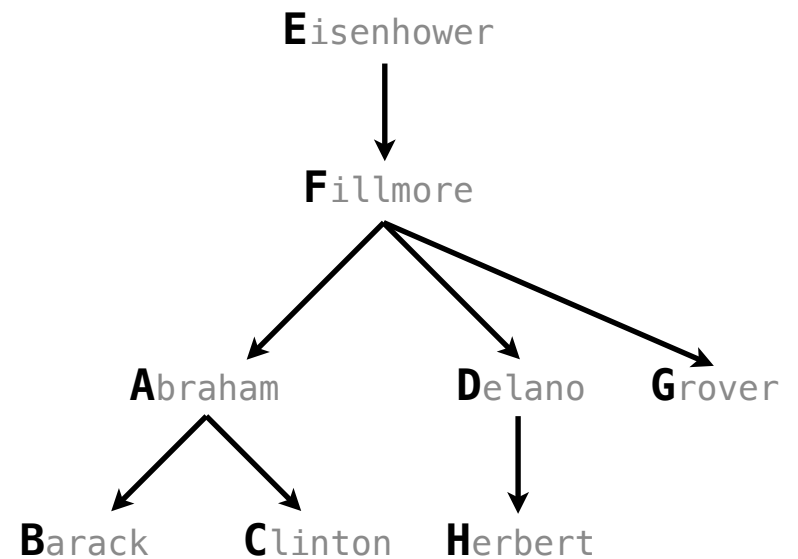
A fact can include multiple relations and variables as well.

```
(fact <conclusion> <hypothesis0> <hypothesis1> ... <hypothesisN>)
```

Means <conclusion> is true if all the <hypothesis_k> are true.

```
logic> (fact (child ?c ?p) (parent ?p ?c))
```

```
logic> (query (child herbert delano))  
Success!
```



Compound Facts

A fact can include multiple relations and variables as well.

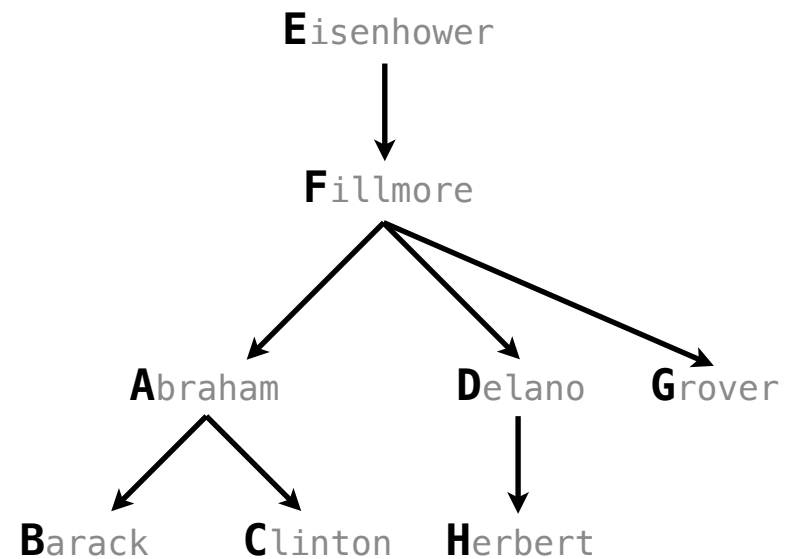
```
(fact <conclusion> <hypothesis0> <hypothesis1> ... <hypothesisN>)
```

Means <conclusion> is true if all the <hypothesis_k> are true.

```
logic> (fact (child ?c ?p) (parent ?p ?c))
```

```
logic> (query (child herbert delano))  
Success!
```

```
logic> (query (child eisenhower clinton))
```



Compound Facts

A fact can include multiple relations and variables as well.

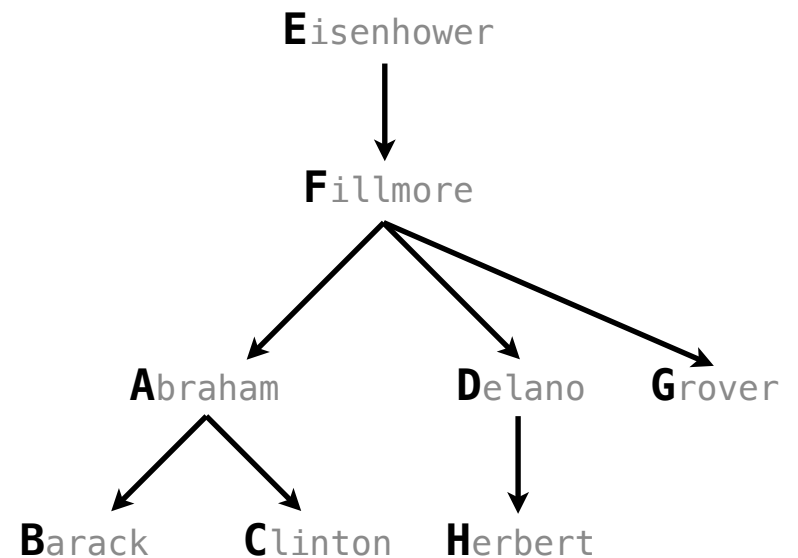
```
(fact <conclusion> <hypothesis0> <hypothesis1> ... <hypothesisN>)
```

Means <conclusion> is true if all the <hypothesis_k> are true.

```
logic> (fact (child ?c ?p) (parent ?p ?c))
```

```
logic> (query (child herbert delano))  
Success!
```

```
logic> (query (child eisenhower clinton))  
Failure.
```



Compound Facts

A fact can include multiple relations and variables as well.

```
(fact <conclusion> <hypothesis0> <hypothesis1> ... <hypothesisN>)
```

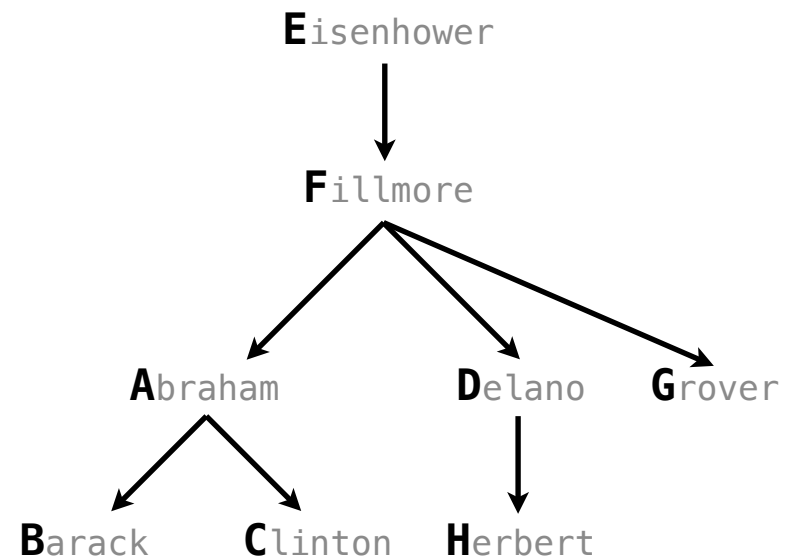
Means <conclusion> is true if all the <hypothesis_k> are true.

```
logic> (fact (child ?c ?p) (parent ?p ?c))
```

```
logic> (query (child herbert delano))  
Success!
```

```
logic> (query (child eisenhower clinton))  
Failure.
```

```
logic> (query (child ?kid fillmore))
```



Compound Facts

A fact can include multiple relations and variables as well.

```
(fact <conclusion> <hypothesis0> <hypothesis1> ... <hypothesisN>)
```

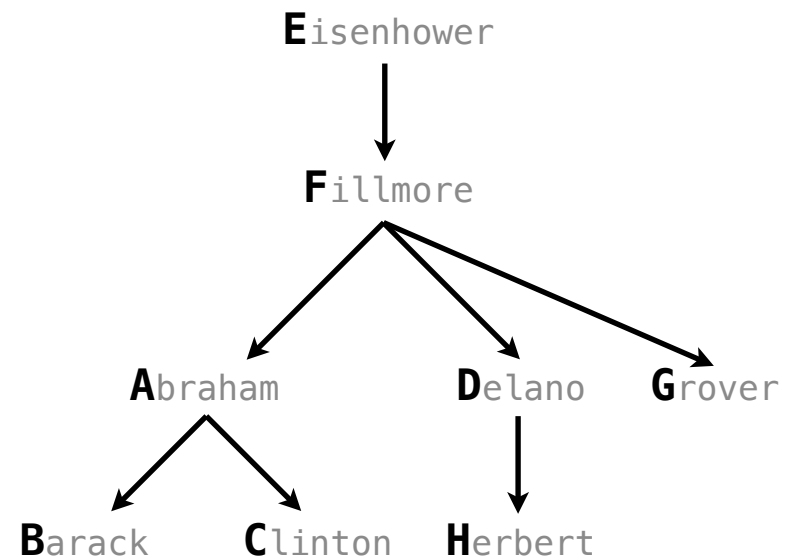
Means <conclusion> is true if all the <hypothesis_k> are true.

```
logic> (fact (child ?c ?p) (parent ?p ?c))
```

```
logic> (query (child herbert delano))  
Success!
```

```
logic> (query (child eisenhower clinton))  
Failure.
```

```
logic> (query (child ?kid fillmore))  
Success!
```



Compound Facts

A fact can include multiple relations and variables as well.

```
(fact <conclusion> <hypothesis0> <hypothesis1> ... <hypothesisN>)
```

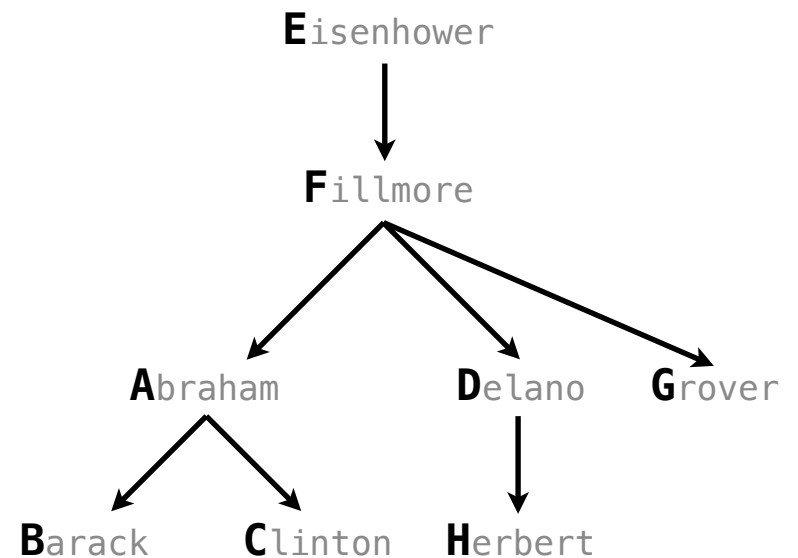
Means <conclusion> is true if all the <hypothesis_k> are true.

```
logic> (fact (child ?c ?p) (parent ?p ?c))
```

```
logic> (query (child herbert delano))  
Success!
```

```
logic> (query (child eisenhower clinton))  
Failure.
```

```
logic> (query (child ?kid fillmore))  
Success!  
kid: abraham
```



Compound Facts

A fact can include multiple relations and variables as well.

```
(fact <conclusion> <hypothesis0> <hypothesis1> ... <hypothesisN>)
```

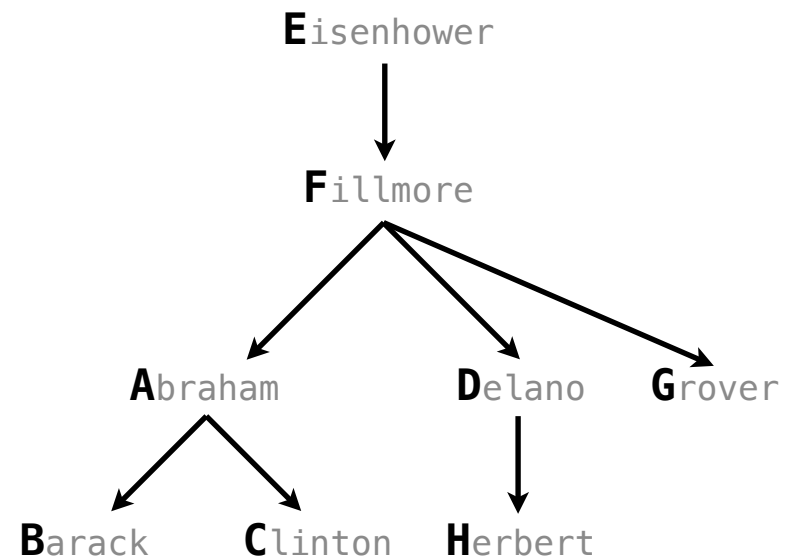
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logic> (fact (child ?c ?p) (parent ?p ?c))
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logic> (query (child herbert delano))  
Success!
```

```
logic> (query (child eisenhower clinton))  
Failure.
```

```
logic> (query (child ?kid fillmore))  
Success!  
kid: abraham  
kid: delano
```



Compound Facts

A fact can include multiple relations and variables as well.

```
(fact <conclusion> <hypothesis0> <hypothesis1> ... <hypothesisN>)
```

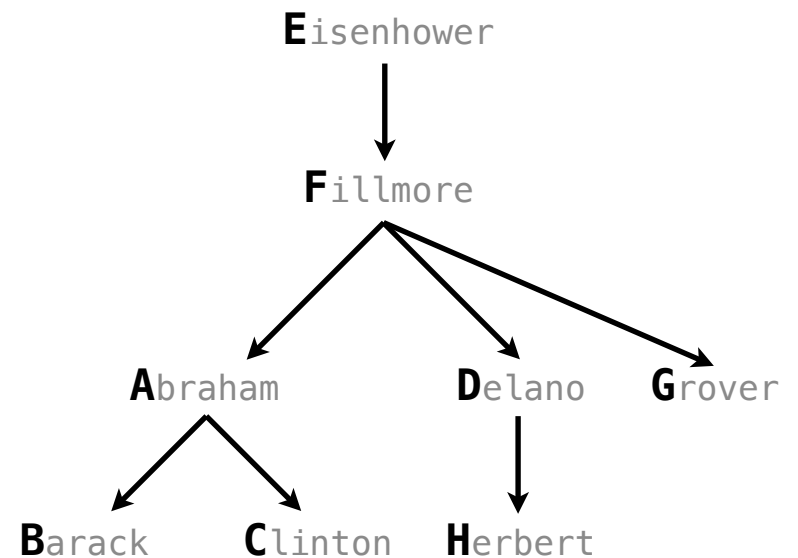
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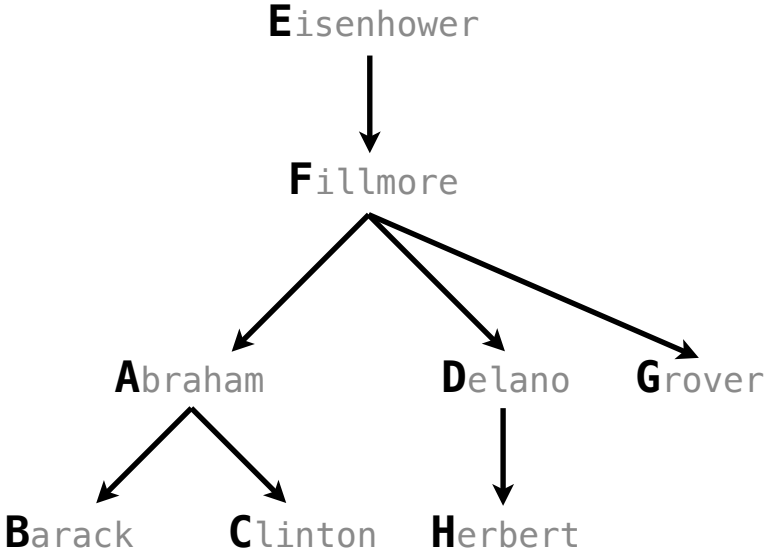
```
logic> (query (child herbert delano))  
Success!
```

```
logic> (query (child eisenhower clinton))  
Failure.
```

```
logic> (query (child ?kid fillmore))  
Success!  
kid: abraham  
kid: delano  
kid: grover
```

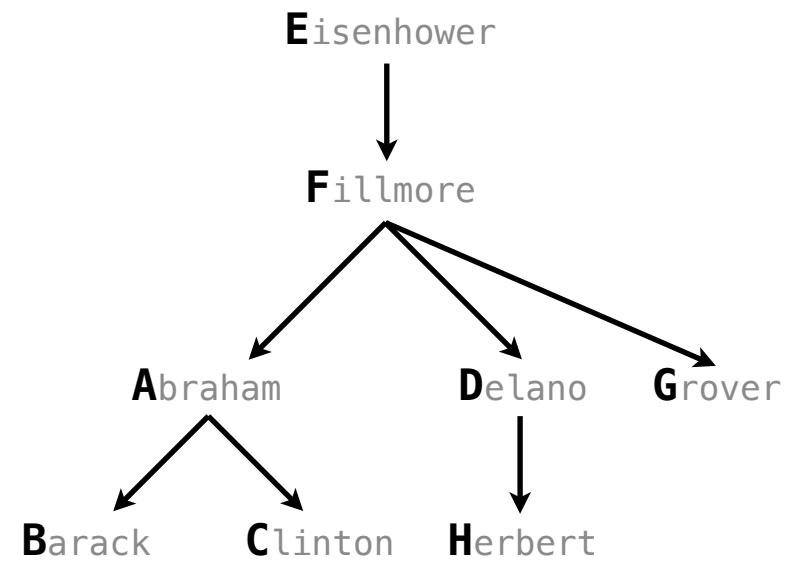


Compound Queries



Compound Queries

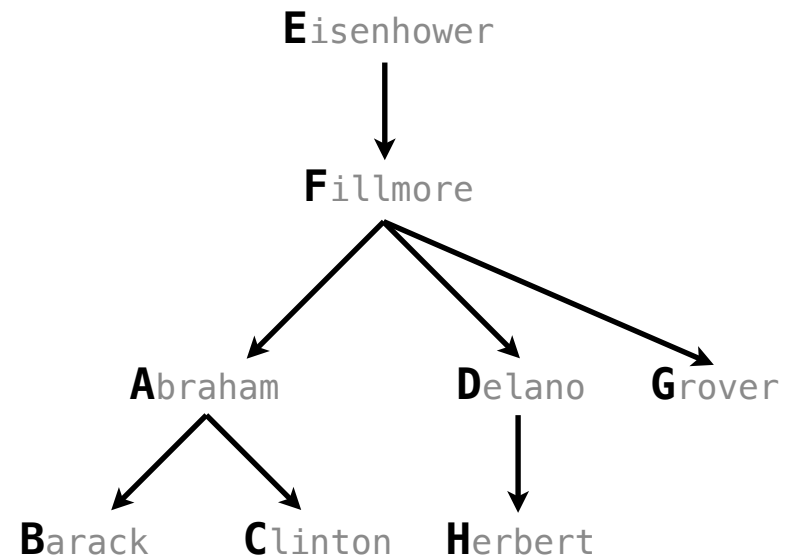
An assignment must satisfy all relations in a query.



Compound Queries

An assignment must satisfy all relations in a query.

(query <relation₀> <relation₁> ... <relation_N>)

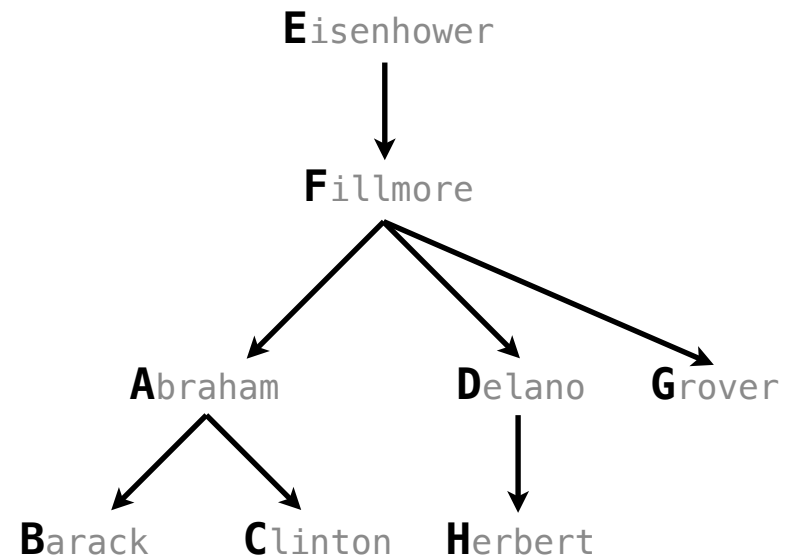


Compound Queries

An assignment must satisfy all relations in a query.

(query `<relation0>` `<relation1>` ... `<relationN>`)

is satisfied if all the `<relationk>` are true.



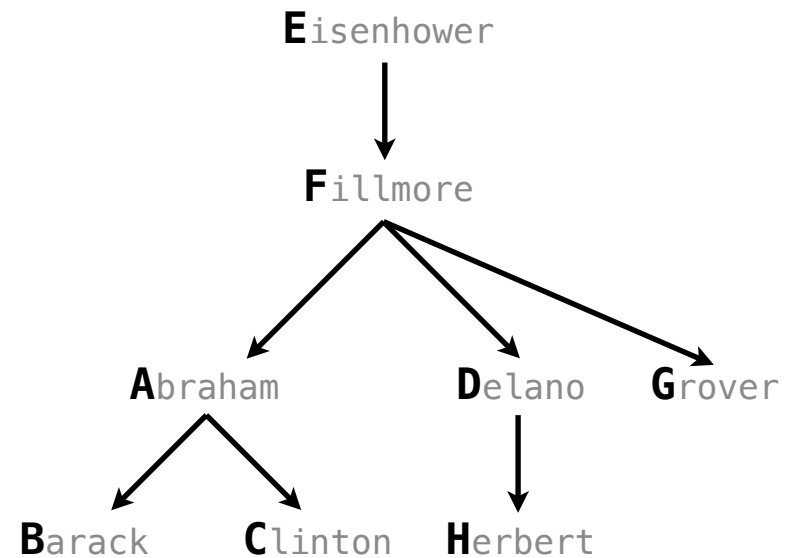
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`(query <relation0> <relation1> ... <relationN>)`

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`logic> (fact (child ?c ?p) (parent ?p ?c))`



Compound Queries

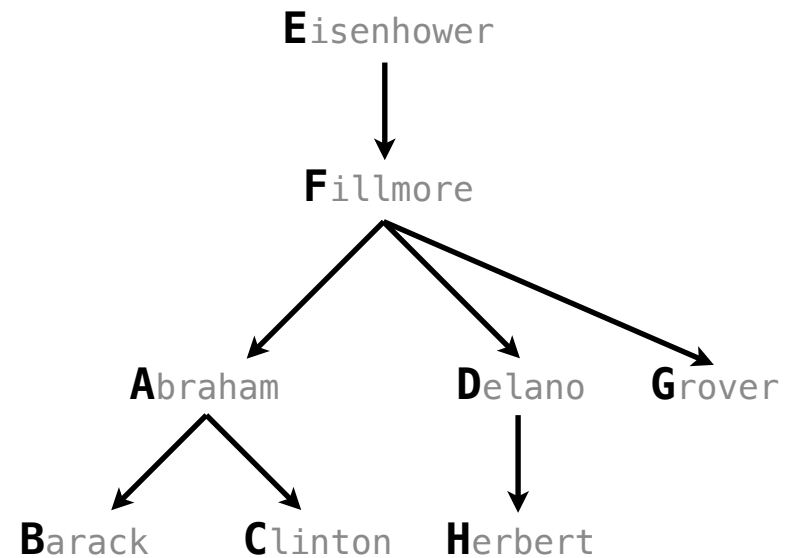
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```
logic> (fact (child ?c ?p) (parent ?p ?c))
```

```
logic> (query (parent ?grampa ?kid))
```



Compound Queries

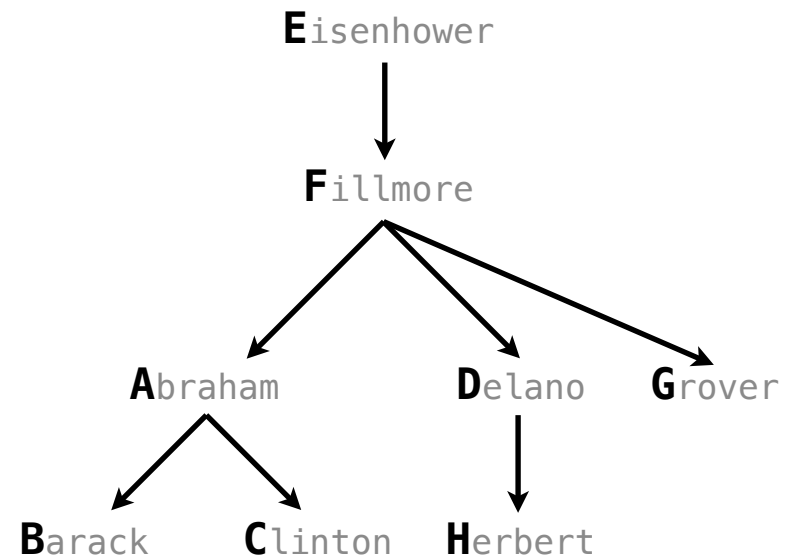
An assignment must satisfy all relations in a query.

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(query <relation0> <relation1> ... <relationN>)
```

is satisfied if all the <relation_k> are true.

```
logic> (fact (child ?c ?p) (parent ?p ?c))
```

```
logic> (query (parent ?grampa ?kid)  
             (child clinton ?kid))
```



Compound Queries

An assignment must satisfy all relations in a query.

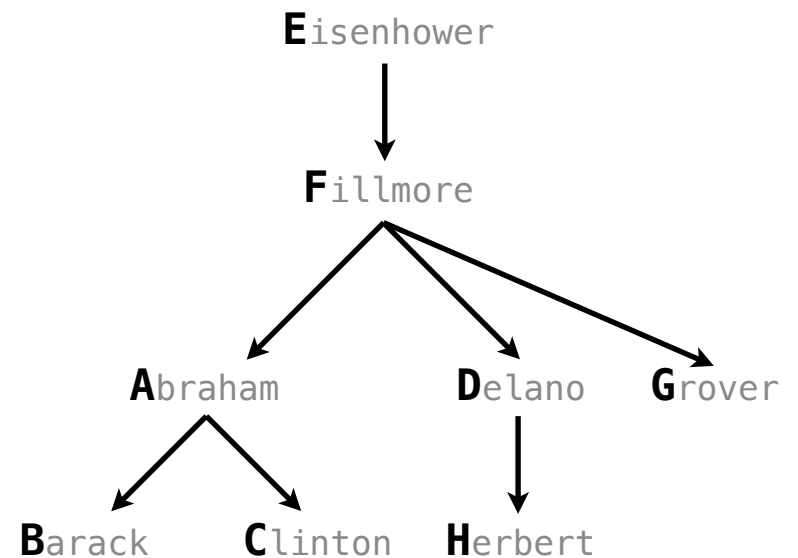
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```

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```
logic> (fact (child ?c ?p) (parent ?p ?c))
```

```
logic> (query (parent ?grampa ?kid)  
            (child clinton ?kid))
```

Success!



Compound Queries

An assignment must satisfy all relations in a query.

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```

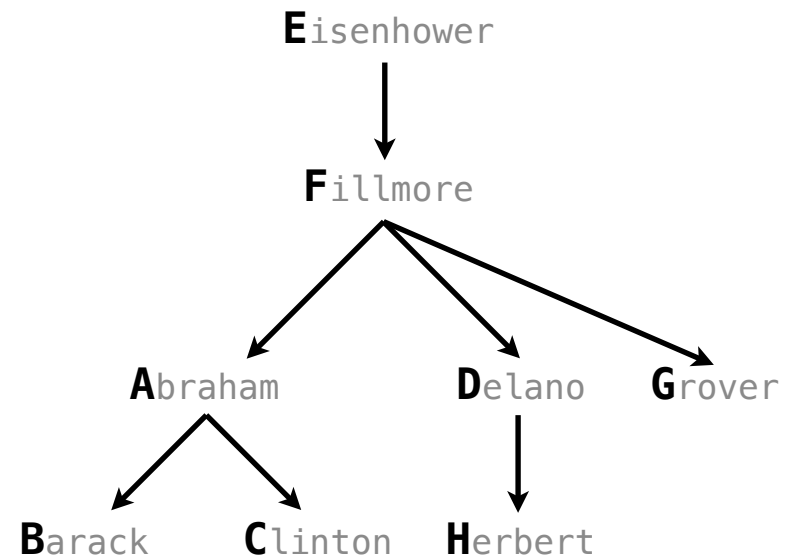
is satisfied if all the <relation_k> are true.

```
logic> (fact (child ?c ?p) (parent ?p ?c))
```

```
logic> (query (parent ?grampa ?kid)
              (child clinton ?kid))
```

Success!

```
grampa: fillmore    kid: abraham
```



Compound Queries

An assignment must satisfy all relations in a query.

(query <relation₀> <relation₁> ... <relation_N>)

is satisfied if all the <relation_k> are true.

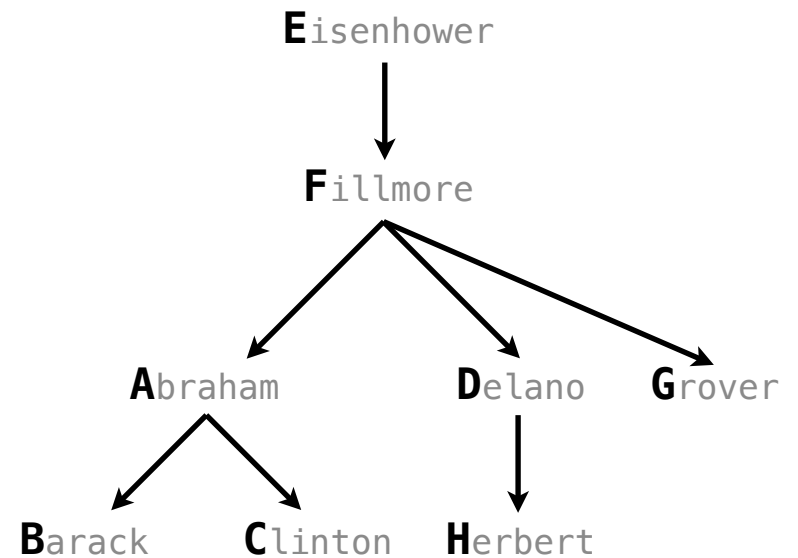
```
logic> (fact (child ?c ?p) (parent ?p ?c))
```

```
logic> (query (parent ?grampa ?kid)
              (child clinton ?kid))
```

Success!

```
grampa: fillmore    kid: abraham
```

```
logic> (query (child ?y ?x))
```



Compound Queries

An assignment must satisfy all relations in a query.

`(query <relation0> <relation1> ... <relationN>)`

is satisfied if all the `<relationk>` are true.

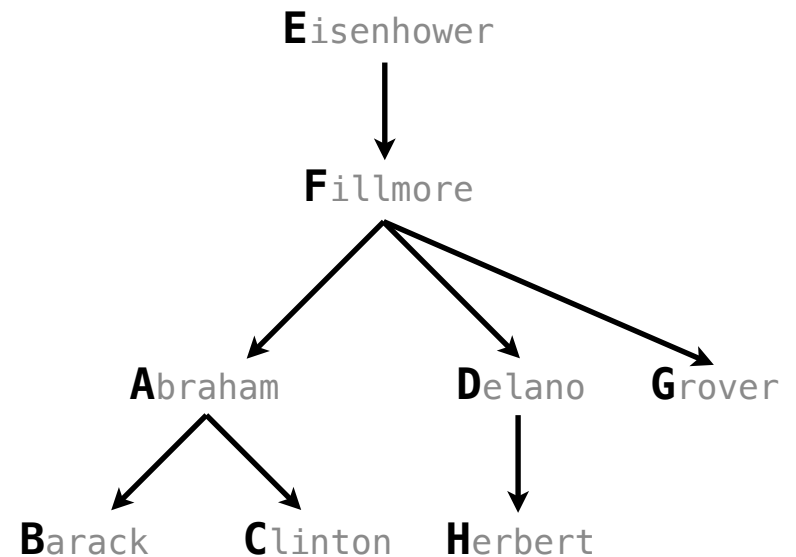
```
logic> (fact (child ?c ?p) (parent ?p ?c))
```

```
logic> (query (parent ?grampa ?kid)
              (child clinton ?kid))
```

Success!

```
grampa: fillmore    kid: abraham
```

```
logic> (query (child ?y ?x)
              (child ?x eisenhower))
```



Compound Queries

An assignment must satisfy all relations in a query.

`(query <relation0> <relation1> ... <relationN>)`

is satisfied if all the `<relationk>` are true.

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logic> (fact (child ?c ?p) (parent ?p ?c))
```

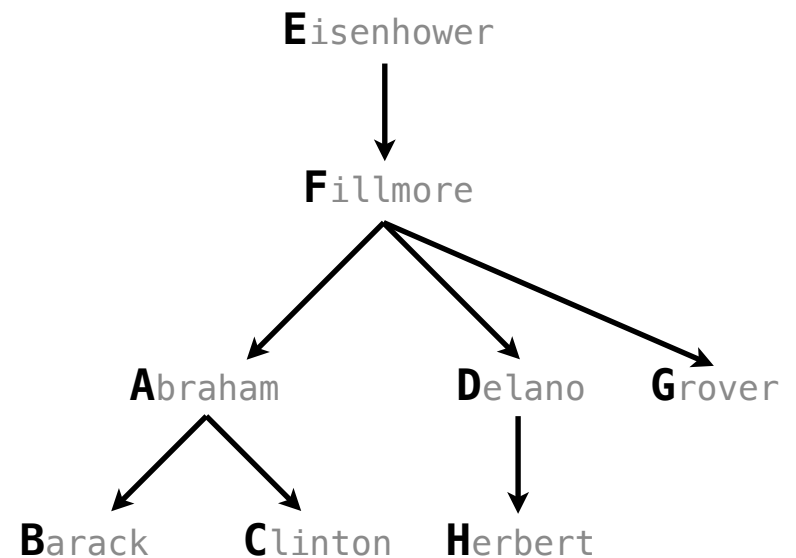
```
logic> (query (parent ?grampa ?kid)
              (child clinton ?kid))
```

Success!

```
grampa: fillmore    kid: abraham
```

```
logic> (query (child ?y ?x)
              (child ?x eisenhower))
```

Success!



Compound Queries

An assignment must satisfy all relations in a query.

`(query <relation0> <relation1> ... <relationN>)`

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```
logic> (fact (child ?c ?p) (parent ?p ?c))
```

```
logic> (query (parent ?grampa ?kid)
              (child clinton ?kid))
```

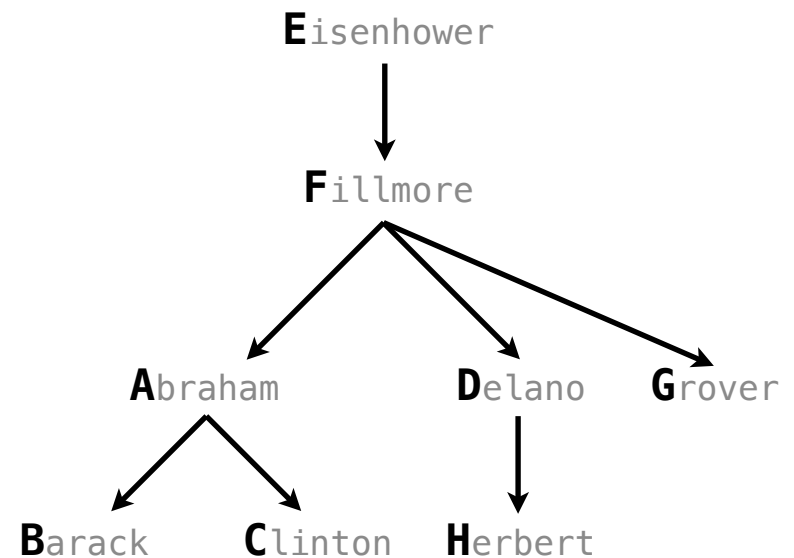
Success!

```
grampa: fillmore    kid: abraham
```

```
logic> (query (child ?y ?x)
              (child ?x eisenhower))
```

Success!

```
y: abraham    x: fillmore
```



Compound Queries

An assignment must satisfy all relations in a query.

(query <relation₀> <relation₁> ... <relation_N>)

is satisfied if all the <relation_k> are true.

```
logic> (fact (child ?c ?p) (parent ?p ?c))
```

```
logic> (query (parent ?grampa ?kid)
              (child clinton ?kid))
```

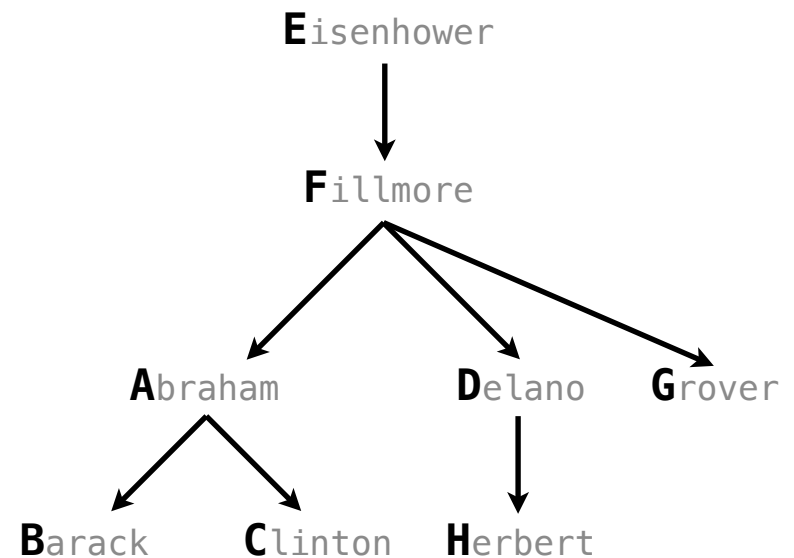
Success!

```
grampa: fillmore    kid: abraham
```

```
logic> (query (child ?y ?x)
              (child ?x eisenhower))
```

Success!

```
y: abraham    x: fillmore
y: delano     x: fillmore
```



Compound Queries

An assignment must satisfy all relations in a query.

`(query <relation0> <relation1> ... <relationN>)`

is satisfied if all the `<relationk>` are true.

```
logic> (fact (child ?c ?p) (parent ?p ?c))
```

```
logic> (query (parent ?grampa ?kid)
              (child clinton ?kid))
```

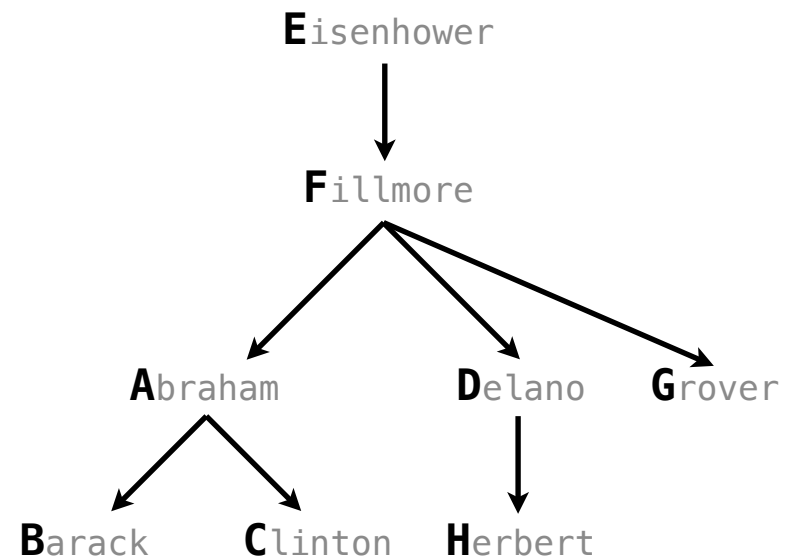
Success!

```
grampa: fillmore    kid: abraham
```

```
logic> (query (child ?y ?x)
              (child ?x eisenhower))
```

Success!

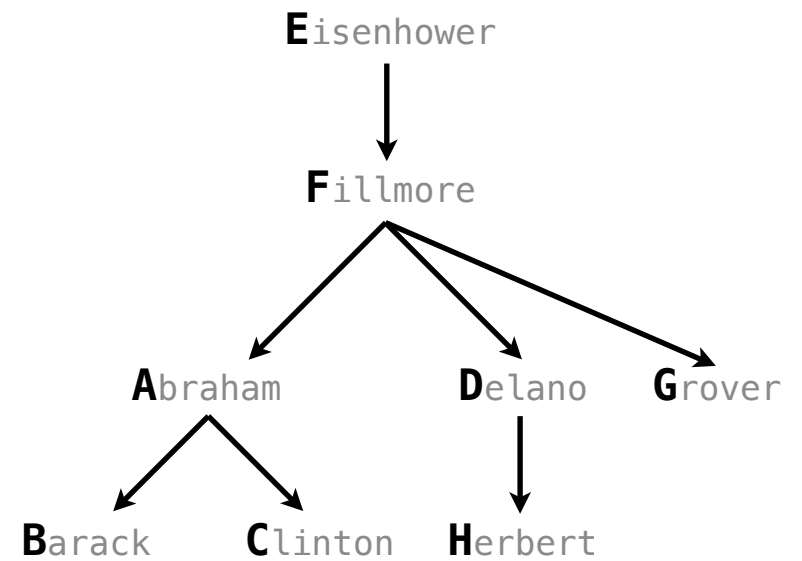
```
y: abraham    x: fillmore
y: delano     x: fillmore
y: grover     x: fillmore
```



Recursive Facts

Recursive Facts

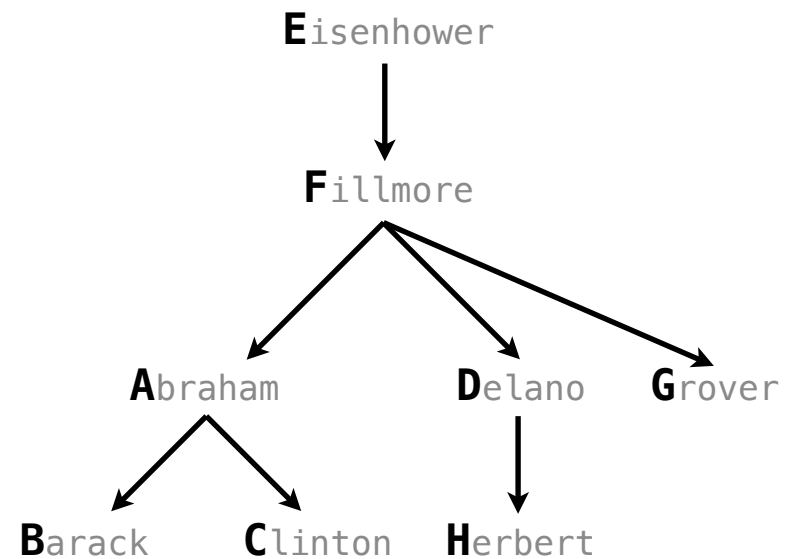
A fact is recursive if the same relation is mentioned in a hypothesis and the conclusion.



Recursive Facts

A fact is recursive if the same relation is mentioned in a hypothesis and the conclusion.

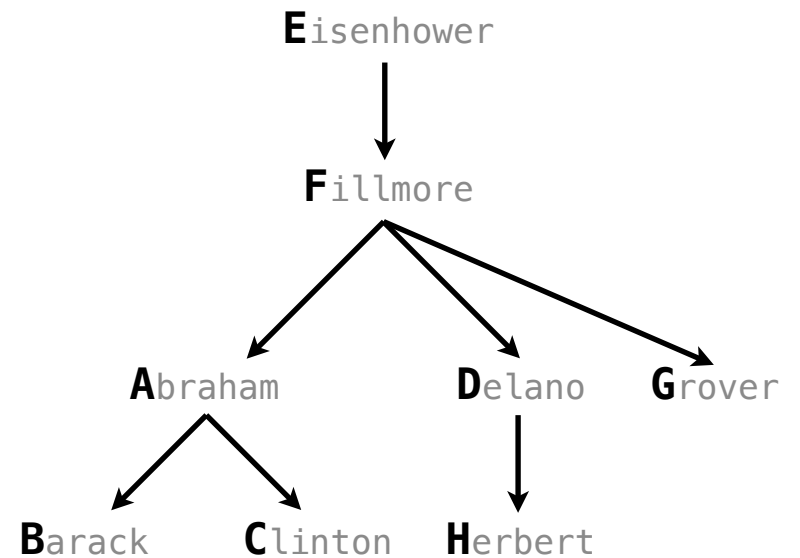
```
logic> (fact (ancestor ?a ?y) (parent ?a ?y))
```



Recursive Facts

A fact is recursive if the same relation is mentioned in a hypothesis and the conclusion.

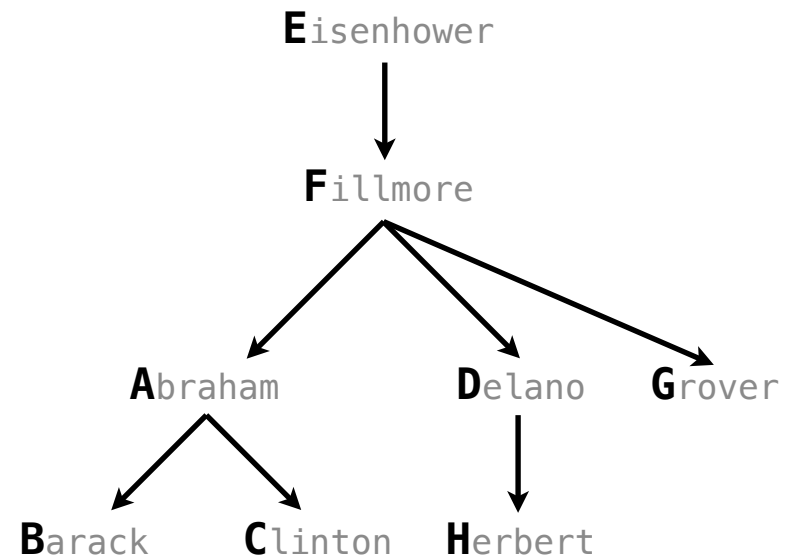
```
logic> (fact (ancestor ?a ?y) (parent ?a ?y))  
logic> (fact (ancestor ?a ?y) (parent ?a ?z) (ancestor ?z ?y))
```



Recursive Facts

A fact is recursive if the same relation is mentioned in a hypothesis and the conclusion.

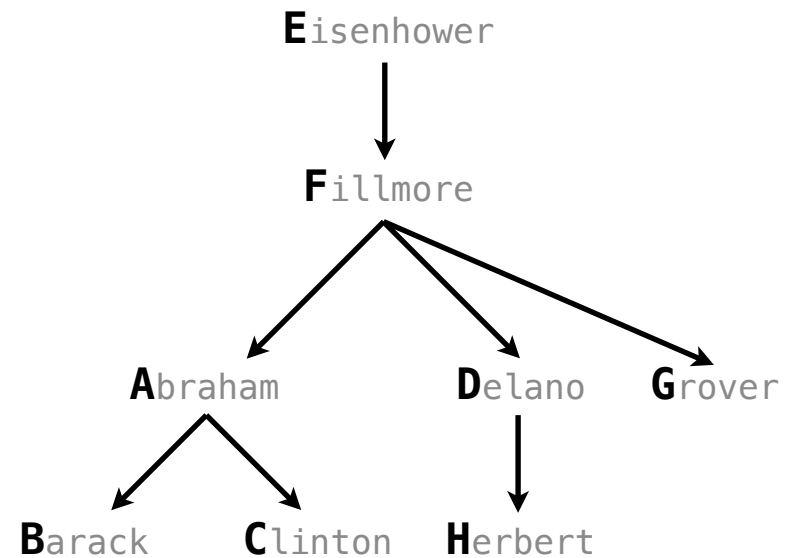
```
logic> (fact (ancestor ?a ?y) (parent ?a ?y))  
logic> (fact (ancestor ?a ?y) (parent ?a ?z) (ancestor ?z ?y))  
  
logic> (query (ancestor ?a herbert))
```



Recursive Facts

A fact is recursive if the same relation is mentioned in a hypothesis and the conclusion.

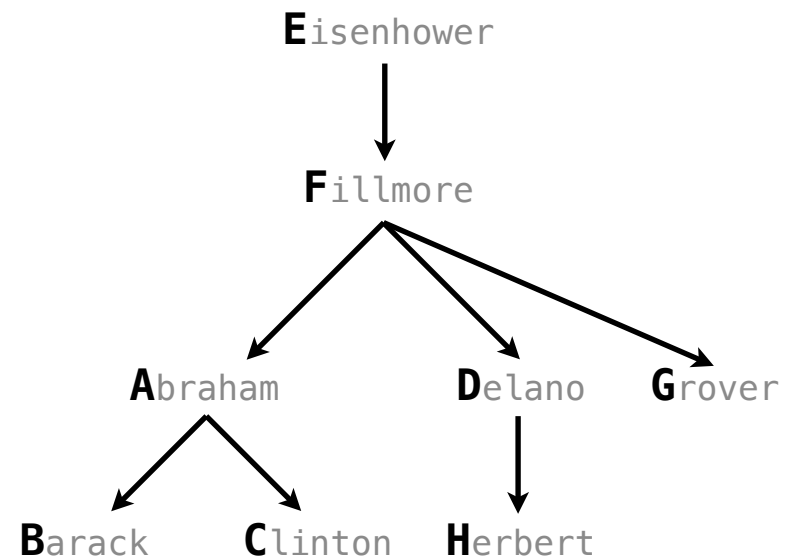
```
logic> (fact (ancestor ?a ?y) (parent ?a ?y))  
logic> (fact (ancestor ?a ?y) (parent ?a ?z) (ancestor ?z ?y))  
  
logic> (query (ancestor ?a herbert))  
Success!
```



Recursive Facts

A fact is recursive if the same relation is mentioned in a hypothesis and the conclusion.

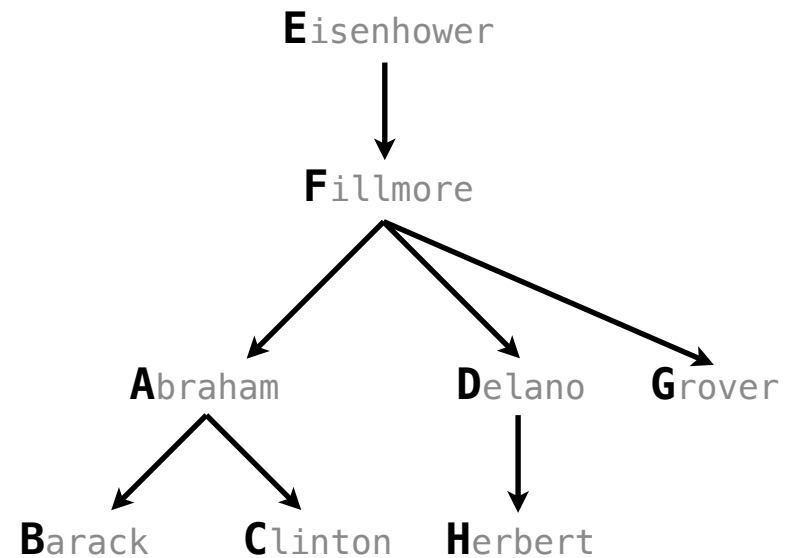
```
logic> (fact (ancestor ?a ?y) (parent ?a ?y))  
logic> (fact (ancestor ?a ?y) (parent ?a ?z) (ancestor ?z ?y))  
  
logic> (query (ancestor ?a herbert))  
Success!  
a: delano
```



Recursive Facts

A fact is recursive if the same relation is mentioned in a hypothesis and the conclusion.

```
logic> (fact (ancestor ?a ?y) (parent ?a ?y))  
logic> (fact (ancestor ?a ?y) (parent ?a ?z) (ancestor ?z ?y))  
  
logic> (query (ancestor ?a herbert))  
Success!  
a: delano  
a: fillmore
```



Recursive Facts

A fact is recursive if the same relation is mentioned in a hypothesis and the conclusion.

```
logic> (fact (ancestor ?a ?y) (parent ?a ?y))  
logic> (fact (ancestor ?a ?y) (parent ?a ?z) (ancestor ?z ?y))
```

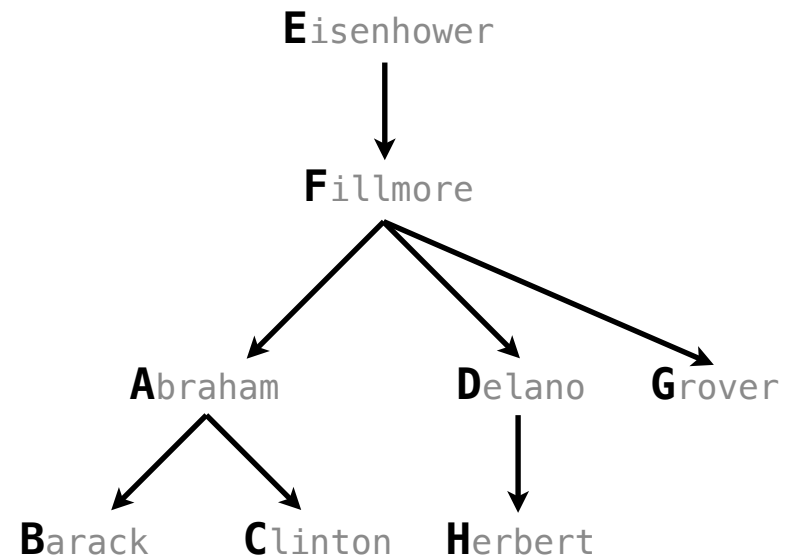
```
logic> (query (ancestor ?a herbert))
```

Success!

a: delano

a: fillmore

a: eisenhower



Recursive Facts

A fact is recursive if the same relation is mentioned in a hypothesis and the conclusion.

```
logic> (fact (ancestor ?a ?y) (parent ?a ?y))  
logic> (fact (ancestor ?a ?y) (parent ?a ?z) (ancestor ?z ?y))
```

```
logic> (query (ancestor ?a herbert))
```

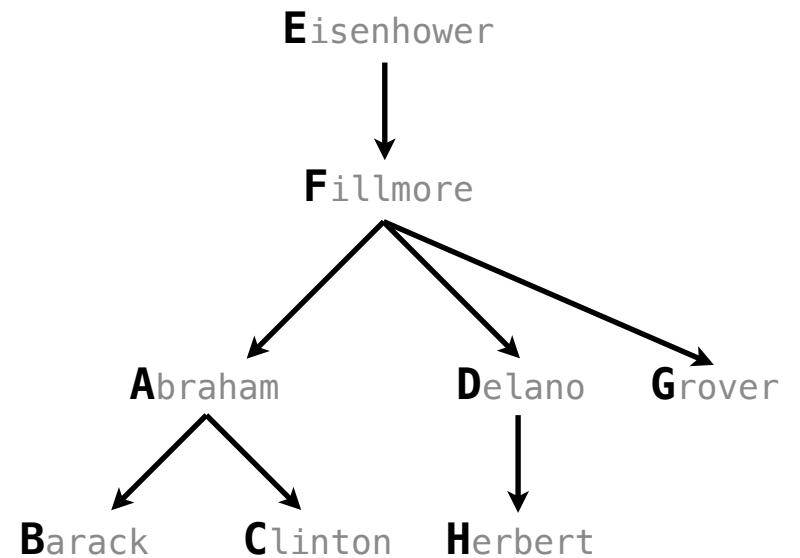
Success!

a: delano

a: fillmore

a: eisenhower

```
logic> (query (ancestor ?a barack))
```



Recursive Facts

A fact is recursive if the same relation is mentioned in a hypothesis and the conclusion.

```
logic> (fact (ancestor ?a ?y) (parent ?a ?y))  
logic> (fact (ancestor ?a ?y) (parent ?a ?z) (ancestor ?z ?y))
```

```
logic> (query (ancestor ?a herbert))
```

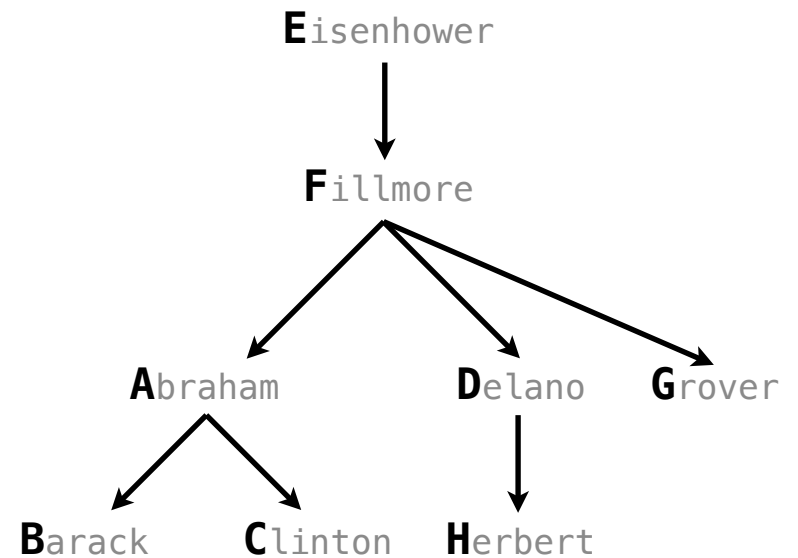
Success!

a: delano

a: fillmore

a: eisenhower

```
logic> (query (ancestor ?a barack)  
            (ancestor ?a herbert))
```



Recursive Facts

A fact is recursive if the same relation is mentioned in a hypothesis and the conclusion.

```
logic> (fact (ancestor ?a ?y) (parent ?a ?y))  
logic> (fact (ancestor ?a ?y) (parent ?a ?z) (ancestor ?z ?y))
```

```
logic> (query (ancestor ?a herbert))
```

Success!

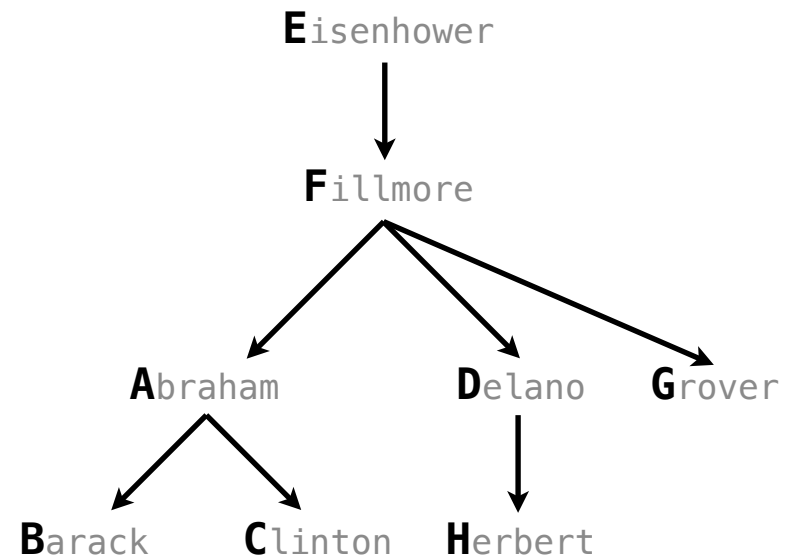
a: delano

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a: eisenhower

```
logic> (query (ancestor ?a barack)  
            (ancestor ?a herbert))
```

Success!



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```

```
logic> (query (ancestor ?a herbert))
```

Success!

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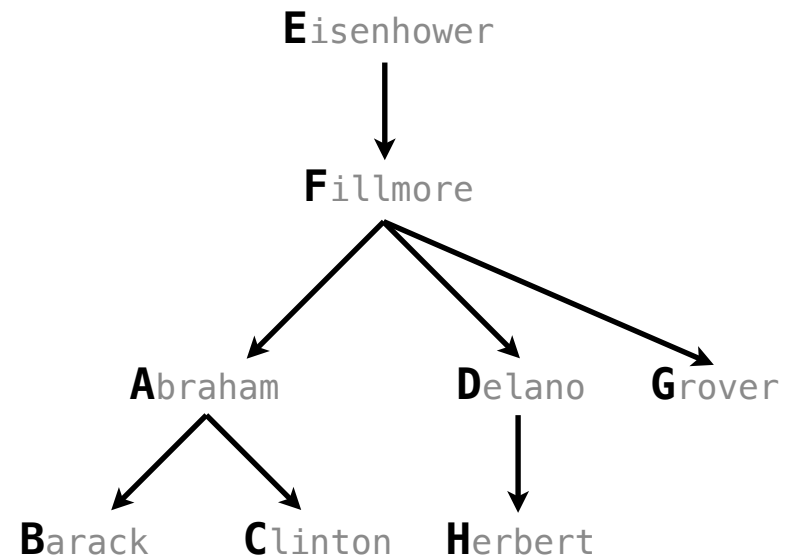
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logic> (query (ancestor ?a barack)  
             (ancestor ?a herbert))
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Success!

a: fillmore



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logic> (query (ancestor ?a herbert))
```

Success!

a: delano

a: fillmore

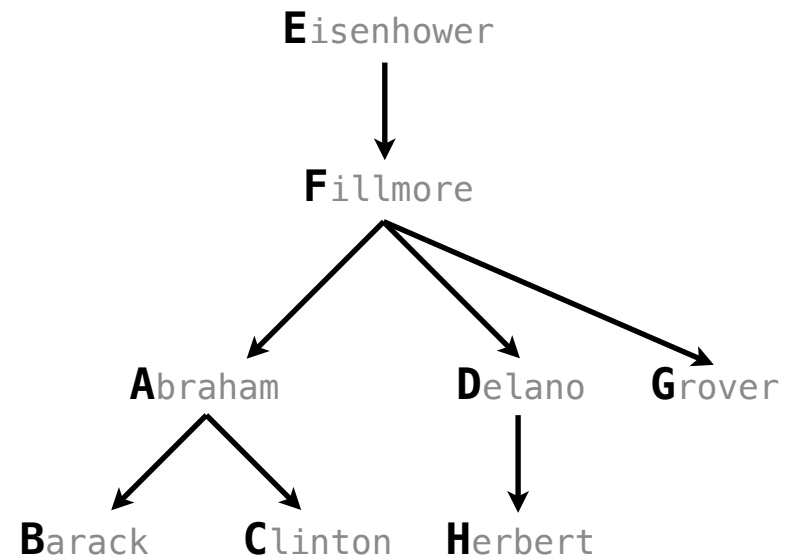
a: eisenhower

```
logic> (query (ancestor ?a barack)  
            (ancestor ?a herbert))
```

Success!

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a: eisenhower



Searching to Satisfy Queries

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The Logic interpreter performs a search in the space of relations for each query to find satisfying assignments.

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```
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```

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a: fillmore ←
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```
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```

```
logic> (fact (parent delano herbert))
```


Searching to Satisfy Queries

The Logic interpreter performs a search in the space of relations for each query to find satisfying assignments.

```
logic> (query (ancestor ?a herbert))
```

```
Success!
```

```
a: delano
```

```
a: fillmore ←
```

```
a: eisenhower
```

```
logic> (fact (parent delano herbert))
```

```
logic> (fact (parent fillmore delano))
```

Searching to Satisfy Queries

The Logic interpreter performs a search in the space of relations for each query to find satisfying assignments.

```
logic> (query (ancestor ?a herbert))
```

```
Success!
```

```
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```

```
a: fillmore ←
```

```
a: eisenhower
```

```
logic> (fact (parent delano herbert))
```

```
logic> (fact (parent fillmore delano))
```

```
logic> (fact (ancestor ?a ?y) (parent ?a ?y))
```

Searching to Satisfy Queries

The Logic interpreter performs a search in the space of relations for each query to find satisfying assignments.

```
logic> (query (ancestor ?a herbert))
```

```
Success!
```

```
a: delano
```

```
a: fillmore ←
```

```
a: eisenhower
```

```
logic> (fact (parent delano herbert))
```

```
logic> (fact (parent fillmore delano))
```

```
logic> (fact (ancestor ?a ?y) (parent ?a ?y))
```

```
logic> (fact (ancestor ?a ?y) (parent ?a ?z) (ancestor ?z ?y))
```

Searching to Satisfy Queries

The Logic interpreter performs a search in the space of relations for each query to find satisfying assignments.

```
logic> (query (ancestor ?a herbert))
```

```
Success!
```

```
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```

```
a: fillmore ←
```

```
a: eisenhower
```

```
logic> (fact (parent delano herbert))
```

```
logic> (fact (parent fillmore delano))
```

```
logic> (fact (ancestor ?a ?y) (parent ?a ?y))
```

```
logic> (fact (ancestor ?a ?y) (parent ?a ?z) (ancestor ?z ?y))
```

```
(parent delano herbert) ; (1), a simple fact
```

Searching to Satisfy Queries

The Logic interpreter performs a search in the space of relations for each query to find satisfying assignments.

```
logic> (query (ancestor ?a herbert))
```

```
Success!
```

```
a: delano
```

```
a: fillmore ←
```

```
a: eisenhower
```

```
logic> (fact (parent delano herbert))
```

```
logic> (fact (parent fillmore delano))
```

```
logic> (fact (ancestor ?a ?y) (parent ?a ?y))
```

```
logic> (fact (ancestor ?a ?y) (parent ?a ?z) (ancestor ?z ?y))
```

```
(parent delano herbert)      ; (1), a simple fact
```

```
(ancestor delano herbert)   ; (2), from (1) and the 1st ancestor fact
```

Searching to Satisfy Queries

The Logic interpreter performs a search in the space of relations for each query to find satisfying assignments.

```
logic> (query (ancestor ?a herbert))
```

```
Success!
```

```
a: delano
```

```
a: fillmore ←
```

```
a: eisenhower
```

```
logic> (fact (parent delano herbert))
```

```
logic> (fact (parent fillmore delano))
```

```
logic> (fact (ancestor ?a ?y) (parent ?a ?y))
```

```
logic> (fact (ancestor ?a ?y) (parent ?a ?z) (ancestor ?z ?y))
```

```
(parent delano herbert)      ; (1), a simple fact
```

```
(ancestor delano herbert)   ; (2), from (1) and the 1st ancestor fact
```

```
(parent fillmore delano)    ; (3), a simple fact
```

Searching to Satisfy Queries

The Logic interpreter performs a search in the space of relations for each query to find satisfying assignments.

```
logic> (query (ancestor ?a herbert))
```

```
Success!
```

```
a: delano
```

```
a: fillmore ←
```

```
a: eisenhower
```

```
logic> (fact (parent delano herbert))
```

```
logic> (fact (parent fillmore delano))
```

```
logic> (fact (ancestor ?a ?y) (parent ?a ?y))
```

```
logic> (fact (ancestor ?a ?y) (parent ?a ?z) (ancestor ?z ?y))
```

```
(parent delano herbert) ; (1), a simple fact
```

```
(ancestor delano herbert) ; (2), from (1) and the 1st ancestor fact
```

```
(parent fillmore delano) ; (3), a simple fact
```

```
(ancestor fillmore herbert) ; (4), from (2), (3), & the 2nd ancestor fact
```

Hierarchical Facts

Hierarchical Facts

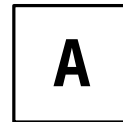
Hierarchical Facts

Relations can contain relations in addition to symbols.

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```
logic> (fact (dog (name abraham) (color white)))
```



Hierarchical Facts

Relations can contain relations in addition to symbols.

```
logic> (fact (dog (name abraham) (color white)))
```

```
logic> (fact (dog (name barack) (color tan)))
```

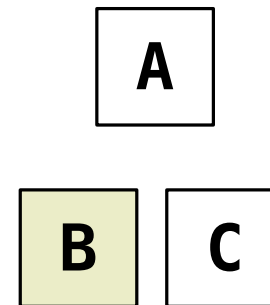
A

B

Hierarchical Facts

Relations can contain relations in addition to symbols.

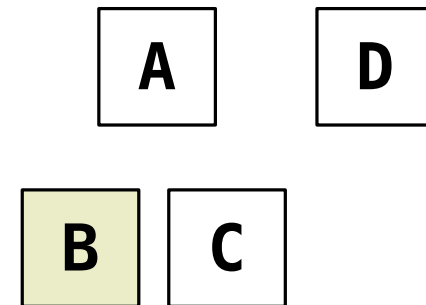
```
logic> (fact (dog (name abraham) (color white)))  
logic> (fact (dog (name barack) (color tan)))  
logic> (fact (dog (name clinton) (color white)))
```



Hierarchical Facts

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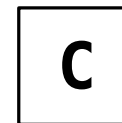
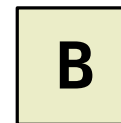
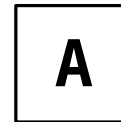
```
logic> (fact (dog (name abraham) (color white)))  
logic> (fact (dog (name barack) (color tan)))  
logic> (fact (dog (name clinton) (color white)))  
logic> (fact (dog (name delano) (color white)))
```



Hierarchical Facts

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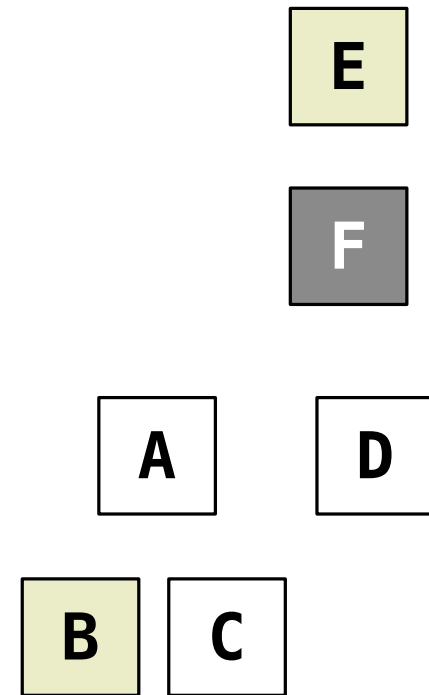
```
logic> (fact (dog (name abraham) (color white)))  
logic> (fact (dog (name barack) (color tan)))  
logic> (fact (dog (name clinton) (color white)))  
logic> (fact (dog (name delano) (color white)))  
logic> (fact (dog (name eisenhower) (color tan)))
```



Hierarchical Facts

Relations can contain relations in addition to symbols.

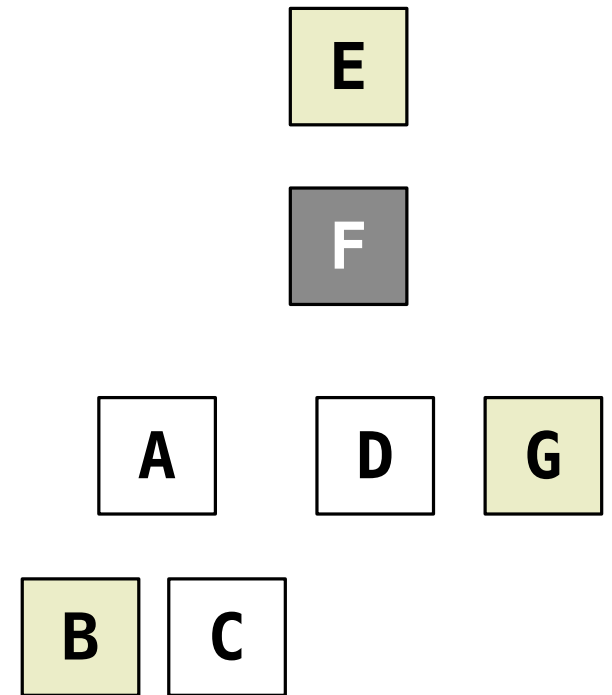
```
logic> (fact (dog (name abraham) (color white)))  
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logic> (fact (dog (name clinton) (color white)))  
logic> (fact (dog (name delano) (color white)))  
logic> (fact (dog (name eisenhower) (color tan)))  
logic> (fact (dog (name fillmore) (color gray)))
```



Hierarchical Facts

Relations can contain relations in addition to symbols.

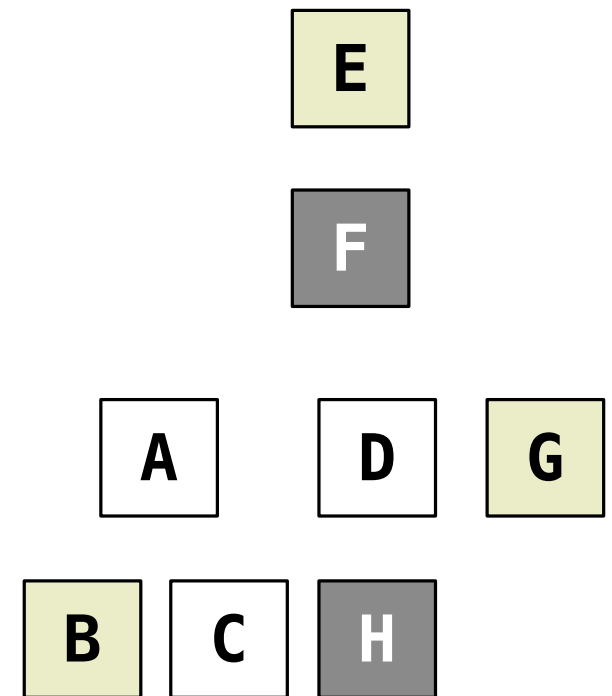
```
logic> (fact (dog (name abraham) (color white)))  
logic> (fact (dog (name barack) (color tan)))  
logic> (fact (dog (name clinton) (color white)))  
logic> (fact (dog (name delano) (color white)))  
logic> (fact (dog (name eisenhower) (color tan)))  
logic> (fact (dog (name fillmore) (color gray)))  
logic> (fact (dog (name grover) (color tan)))
```



Hierarchical Facts

Relations can contain relations in addition to symbols.

```
logic> (fact (dog (name abraham) (color white)))  
logic> (fact (dog (name barack) (color tan)))  
logic> (fact (dog (name clinton) (color white)))  
logic> (fact (dog (name delano) (color white)))  
logic> (fact (dog (name eisenhower) (color tan)))  
logic> (fact (dog (name fillmore) (color gray)))  
logic> (fact (dog (name grover) (color tan)))  
logic> (fact (dog (name herbert) (color gray)))
```



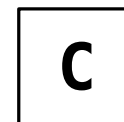
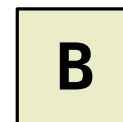
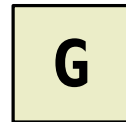
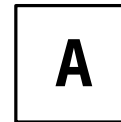
Hierarchical Facts

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logic> (fact (dog (name abraham) (color white)))  
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logic> (fact (dog (name clinton) (color white)))  
logic> (fact (dog (name delano) (color white)))  
logic> (fact (dog (name eisenhower) (color tan)))  
logic> (fact (dog (name fillmore) (color gray)))  
logic> (fact (dog (name grover) (color tan)))  
logic> (fact (dog (name herbert) (color gray)))
```



Variables can refer to symbols or whole relations.



Hierarchical Facts

Relations can contain relations in addition to symbols.

```
logic> (fact (dog (name abraham) (color white)))  
logic> (fact (dog (name barack) (color tan)))  
logic> (fact (dog (name clinton) (color white)))  
logic> (fact (dog (name delano) (color white)))  
logic> (fact (dog (name eisenhower) (color tan)))  
logic> (fact (dog (name fillmore) (color gray)))  
logic> (fact (dog (name grover) (color tan)))  
logic> (fact (dog (name herbert) (color gray)))
```

Variables can refer to symbols or whole relations.

```
logic> (query (dog (name clinton) (color ?color)))
```

E

F

A

D

G

B

C

H

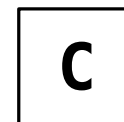
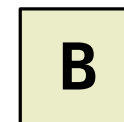
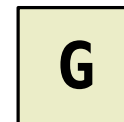
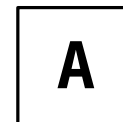
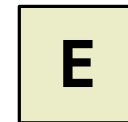
Hierarchical Facts

Relations can contain relations in addition to symbols.

```
logic> (fact (dog (name abraham) (color white)))  
logic> (fact (dog (name barack) (color tan)))  
logic> (fact (dog (name clinton) (color white)))  
logic> (fact (dog (name delano) (color white)))  
logic> (fact (dog (name eisenhower) (color tan)))  
logic> (fact (dog (name fillmore) (color gray)))  
logic> (fact (dog (name grover) (color tan)))  
logic> (fact (dog (name herbert) (color gray)))
```

Variables can refer to symbols or whole relations.

```
logic> (query (dog (name clinton) (color ?color)))  
Success!
```



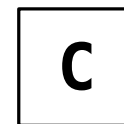
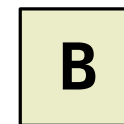
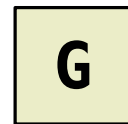
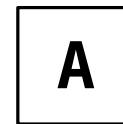
Hierarchical Facts

Relations can contain relations in addition to symbols.

```
logic> (fact (dog (name abraham) (color white)))
logic> (fact (dog (name barack) (color tan)))
logic> (fact (dog (name clinton) (color white)))
logic> (fact (dog (name delano) (color white)))
logic> (fact (dog (name eisenhower) (color tan)))
logic> (fact (dog (name fillmore) (color gray)))
logic> (fact (dog (name grover) (color tan)))
logic> (fact (dog (name herbert) (color gray)))
```

Variables can refer to symbols or whole relations.

```
logic> (query (dog (name clinton) (color ?color)))
Success!
color: white
```



Hierarchical Facts

Relations can contain relations in addition to symbols.

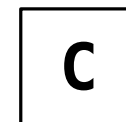
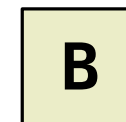
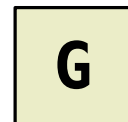
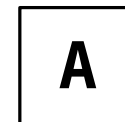
```
logic> (fact (dog (name abraham) (color white)))
logic> (fact (dog (name barack) (color tan)))
logic> (fact (dog (name clinton) (color white)))
logic> (fact (dog (name delano) (color white)))
logic> (fact (dog (name eisenhower) (color tan)))
logic> (fact (dog (name fillmore) (color gray)))
logic> (fact (dog (name grover) (color tan)))
logic> (fact (dog (name herbert) (color gray)))
```



Variables can refer to symbols or whole relations.

```
logic> (query (dog (name clinton) (color ?color)))
Success!
color: white

logic> (query (dog (name clinton) ?stats))
```



Hierarchical Facts

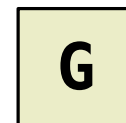
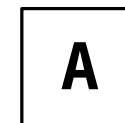
Relations can contain relations in addition to symbols.

```
logic> (fact (dog (name abraham) (color white)))
logic> (fact (dog (name barack) (color tan)))
logic> (fact (dog (name clinton) (color white)))
logic> (fact (dog (name delano) (color white)))
logic> (fact (dog (name eisenhower) (color tan)))
logic> (fact (dog (name fillmore) (color gray)))
logic> (fact (dog (name grover) (color tan)))
logic> (fact (dog (name herbert) (color gray)))
```

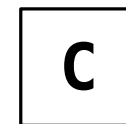
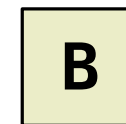


Variables can refer to symbols or whole relations.

```
logic> (query (dog (name clinton) (color ?color)))
Success!
color: white
```



```
logic> (query (dog (name clinton) ?stats))
Success!
```



Hierarchical Facts

Relations can contain relations in addition to symbols.

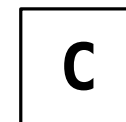
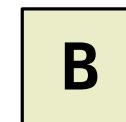
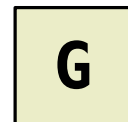
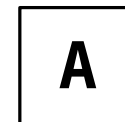
```
logic> (fact (dog (name abraham) (color white)))
logic> (fact (dog (name barack) (color tan)))
logic> (fact (dog (name clinton) (color white)))
logic> (fact (dog (name delano) (color white)))
logic> (fact (dog (name eisenhower) (color tan)))
logic> (fact (dog (name fillmore) (color gray)))
logic> (fact (dog (name grover) (color tan)))
logic> (fact (dog (name herbert) (color gray)))
```



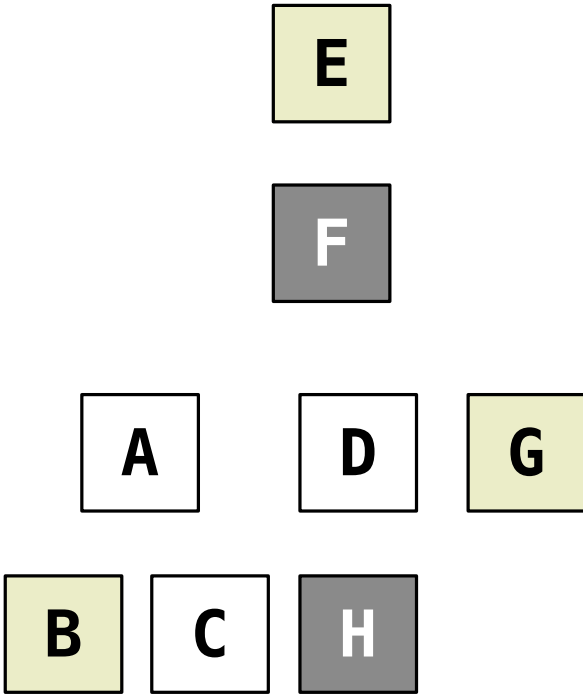
Variables can refer to symbols or whole relations.

```
logic> (query (dog (name clinton) (color ?color)))
Success!
color: white

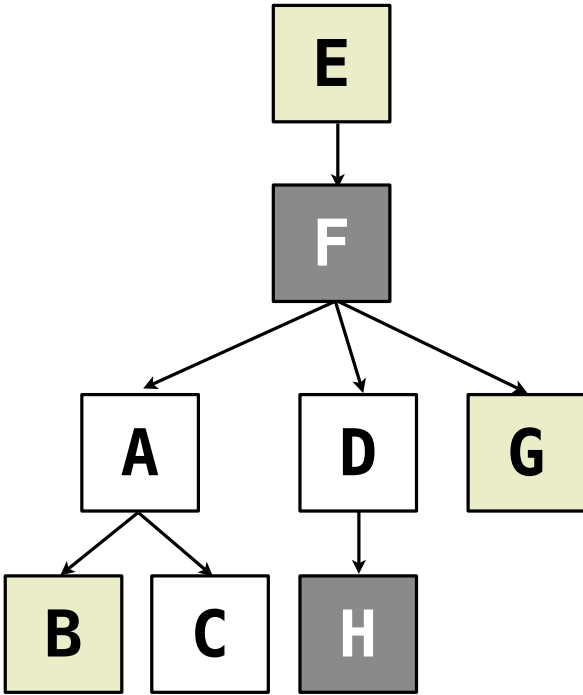
logic> (query (dog (name clinton) ?stats))
Success!
stats: (color white)
```



Combining Multiple Data Sources

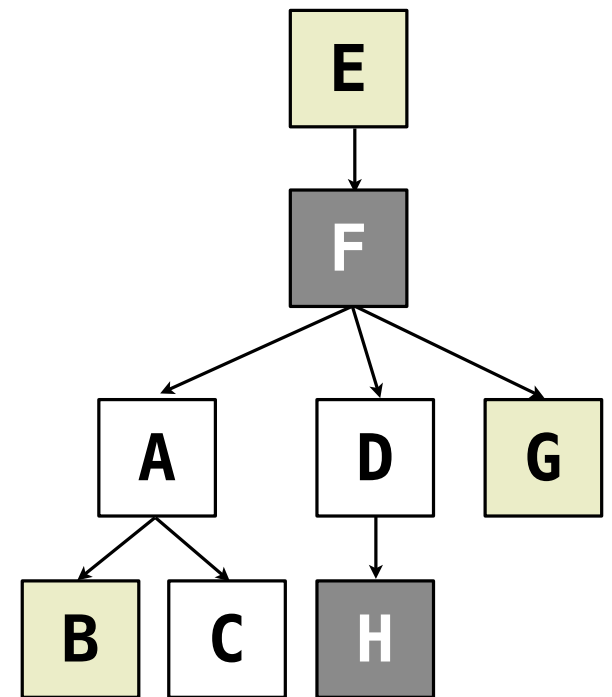


Combining Multiple Data Sources



Combining Multiple Data Sources

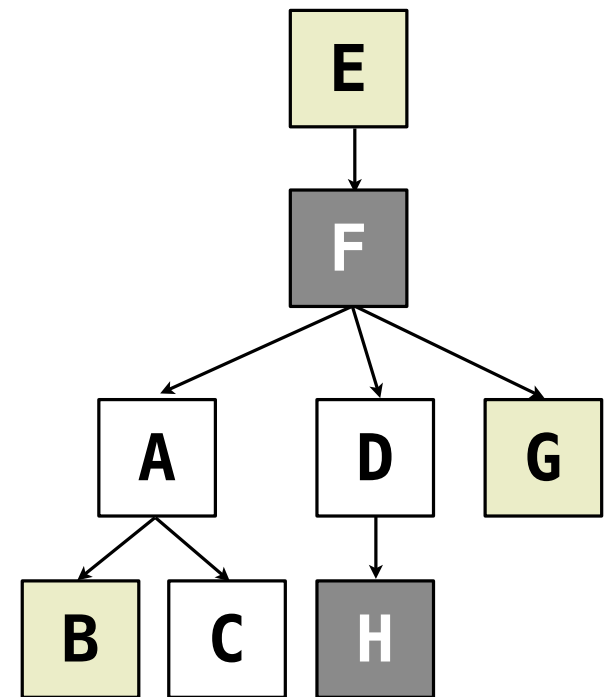
Which dogs have an ancestor of the same color?



Combining Multiple Data Sources

Which dogs have an ancestor of the same color?

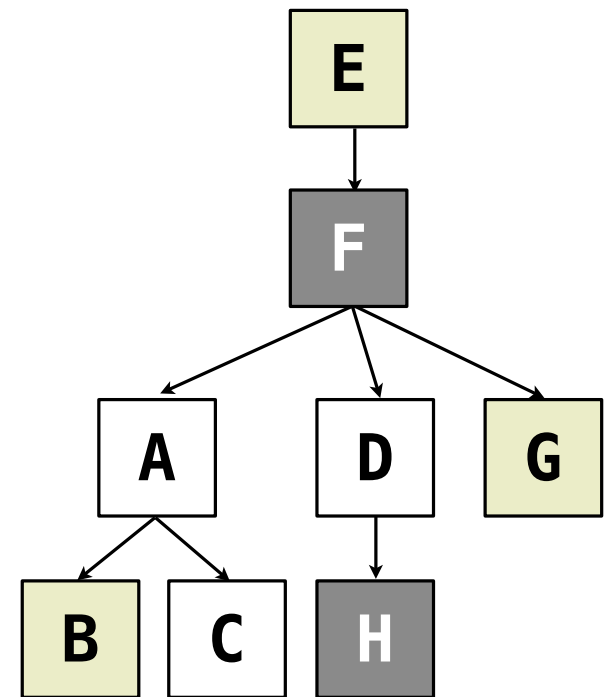
```
logic> (query (dog (name ?x) (color ?fur)))
```



Combining Multiple Data Sources

Which dogs have an ancestor of the same color?

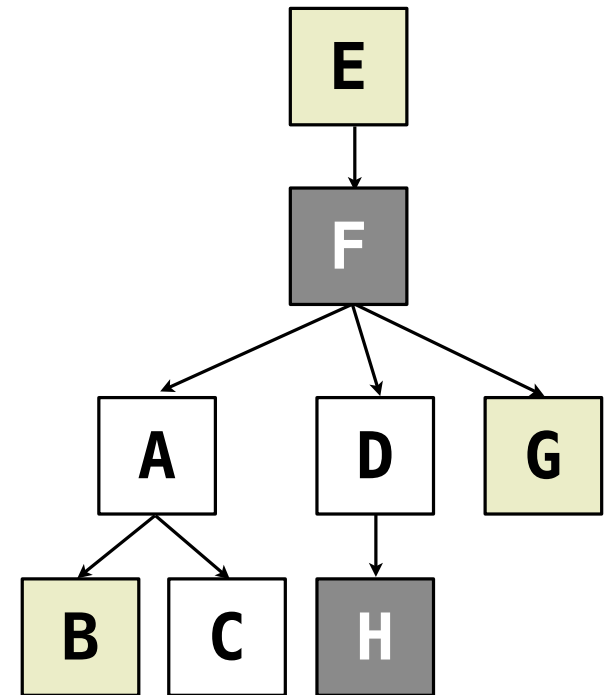
```
logic> (query (dog (name ?x) (color ?fur))  
            (ancestor ?y ?x))
```



Combining Multiple Data Sources

Which dogs have an ancestor of the same color?

```
logic> (query (dog (name ?x) (color ?fur))  
             (ancestor ?y ?x)  
             (dog (name ?y) (color ?fur)))
```

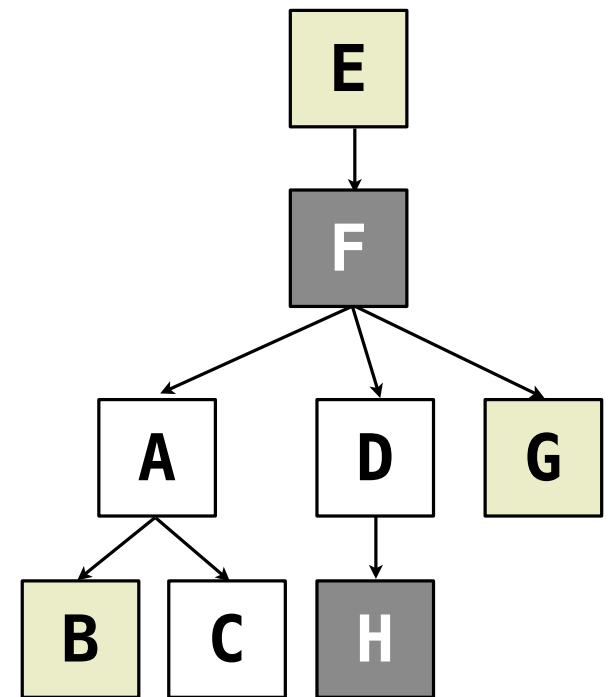


Combining Multiple Data Sources

Which dogs have an ancestor of the same color?

```
logic> (query (dog (name ?x) (color ?fur))  
            (ancestor ?y ?x)  
            (dog (name ?y) (color ?fur)))
```

Success!



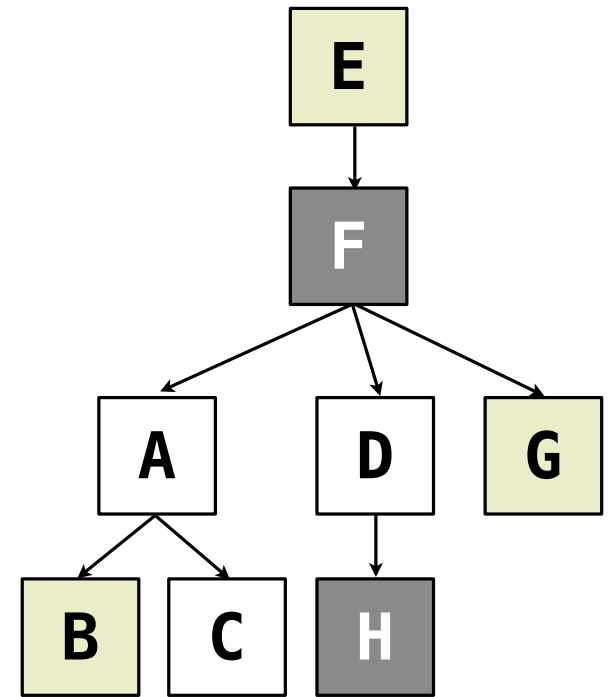
Combining Multiple Data Sources

Which dogs have an ancestor of the same color?

```
logic> (query (dog (name ?x) (color ?fur))  
            (ancestor ?y ?x)  
            (dog (name ?y) (color ?fur)))
```

Success!

x: barack fur: tan y: eisenhower



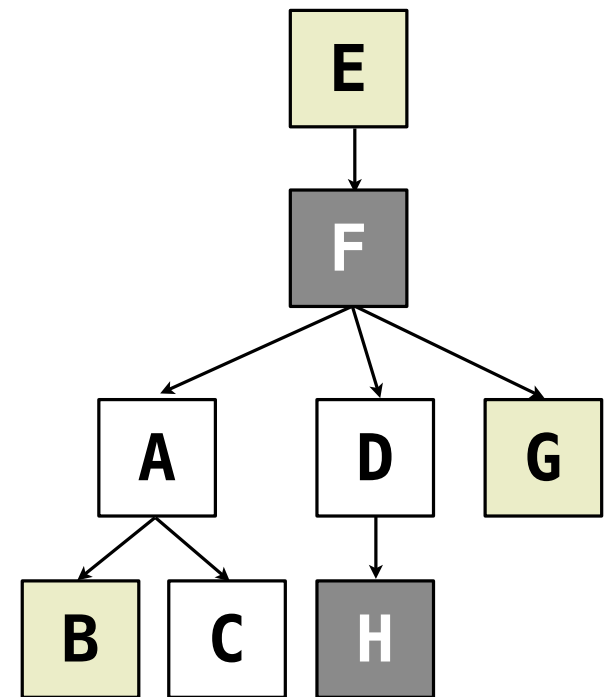
Combining Multiple Data Sources

Which dogs have an ancestor of the same color?

```
logic> (query (dog (name ?x) (color ?fur))  
            (ancestor ?y ?x)  
            (dog (name ?y) (color ?fur)))
```

Success!

```
x: barack      fur: tan      y: eisenhower  
x: clinton    fur: white    y: abraham
```



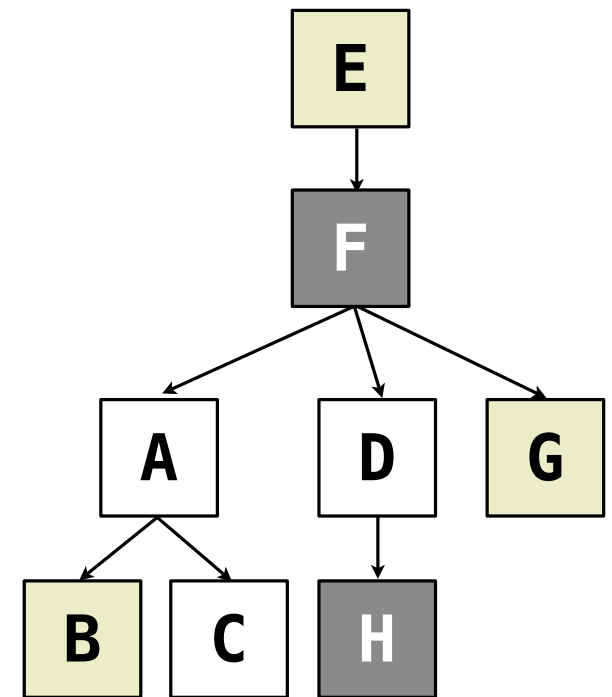
Combining Multiple Data Sources

Which dogs have an ancestor of the same color?

```
logic> (query (dog (name ?x) (color ?fur))  
            (ancestor ?y ?x)  
            (dog (name ?y) (color ?fur)))
```

Success!

```
x: barack      fur: tan      y: eisenhower  
x: clinton    fur: white    y: abraham  
x: grover     fur: tan      y: eisenhower
```



Combining Multiple Data Sources

Which dogs have an ancestor of the same color?

```
logic> (query (dog (name ?x) (color ?fur))  
             (ancestor ?y ?x)  
             (dog (name ?y) (color ?fur)))
```

Success!

x: barack	fur: tan	y: eisenhower
x: clinton	fur: white	y: abraham
x: grover	fur: tan	y: eisenhower
x: herbert	fur: gray	y: fillmore

