61A Lecture 8

Wednesday, September 18

Hog Contest Rules

- Up to two people submit one entry; Max of one entry per person.
- \bullet Your score is the number of entries against which you win more than 50% of the time.
- All strategies must be deterministic, pure functions of the current player scores! Non-deterministic strategies will be disqualified.
- One more special rule: *Ham Hijinks*. Choose -1 to swap the 4-sided and 6-sided dice.
- To enter: <code>submit projlcontest</code> with a file hog.py that defines a final_strategy function by <code>Thursday 10/3 @ 11:59pm</code>
- All winning entries will receive 2 points of extra credit
- The real prize: honor and glory

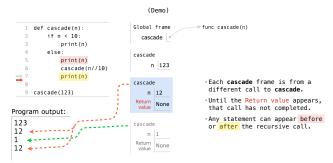
Fall 2011 Winners Keegan Mann, Yan Duan & Ziming Li, Brian Prike & Zhenghao Qian, Parker Schuh & Robert Chatham Fall 2012 Winners

Fall 2013 Winners

Chenyang Yuan, Joseph Hui YOUR NAME COULD BE HERE...
FOREVER!

http://inst.eecs.berkeley.edu/~cs61a/fa13/proj/hog_contest/hog_contest.html

The Cascade Function



Example: http://goo.gl/090qzK

Announcements

- Project 1 is due Thursday 9/19 @ 11:59pm
- •Midterm 1 is on Monday 9/23 from 7pm to 9pm
- *2 review sessions on Saturday 9/21 2pm-4pm and 4pm-6pm in 1 Pimentel
- *HKN review session on Sunday 9/22 from 4pm to 7pm in 2050 Valley LSB
- Extra office hours over the weekend
- *Includes topics up to and including this lecture
- "Fill out the form on the website if you cannot attend
- *Homework 3 is due in two weeks: Tuesday 10/1 @ 11:59pm

 *It contains lots of recursion problems, for practice!
- •Optional Hog strategy contest ends Thursday 10/3 @ 11:59pm

Order of Recursive Calls

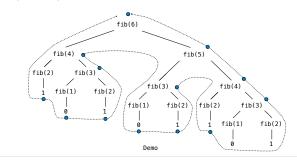
Two Definitions of Cascade

- If two implementations are equally clear, then shorter is usually better.
- $\boldsymbol{\cdot}$ In this case, the longer implementation is more clear (at least to me).
- $\boldsymbol{\cdot}$ When learning to write recursive functions, put the base cases first.
- $\boldsymbol{\cdot}$ Both are recursive functions, even though only the first has typical structure.

Tree Recursion

A Tree-Recursive Process

The computational process of **fib** evolves into a tree structure



Example: Counting Partitions

Tree Recursion

Tree–shaped processes arise whenever executing the body of a recursive function makes ${\bf more\ than\ one}\ {\bf call\ to\ that\ function.}$

```
n: 1, 2, 3, 4, 5, 6, 7, 8, 9, ..., 35
fib(n): 0, 1, 1, 2, 3, 5, 8, 13, 21, ..., 5,702,887
```

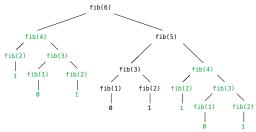
```
def fib(n):
    if n == 1:
        return 0
    elif n == 2:
        return 1
    else:
        return fib(n-2) + fib(n-1)
```



http://en.wikipedia.org/wiki/File:Fibonacci.jpg

Repetition in Tree-Recursive Computation

This process is highly repetitive; fib is called on the same argument multiple times.



We can speed up this computation dramatically in a few weeks by remembering results.

Counting Partitions

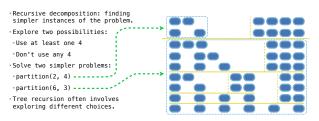
The number of partitions of a positive integer n, using parts up to size m, is the number of ways in which n can be expressed as the sum of positive integer parts up to m in increasing order.

2 + 4 = 6 1 + 1 + 4 = 6 3 + 3 = 6 1 + 2 + 3 = 6 1 + 1 + 1 + 3 = 6 2 + 2 + 2 = 6 1 + 1 + 2 + 2 = 6 1 + 1 + 1 + 1 + 2 = 6 1 + 1 + 1 + 1 + 1 + 1 = 6

Counting Partitions

The number of **partitions** of a positive integer **n**, using parts up to size **m**, is the number of ways in which **n** can be expressed as the sum of positive integer parts up to **m** in increasing order.

partition(6, 4)



Winning Hog

Counting Partitions

The number of partitions of a positive integer n, using parts up to size m, is the number of ways in which ${\bf n}$ can be expressed as the sum of positive integer parts up to m in increasing order.

```
Recursive decomposition: finding simpler instances of the problem.

Explore two possibilities:

Use at least one 4

Don't use any 4

Solve two simpler problems:

-partition(2, 4)

-partition(6, 3)

Tree recursion often involves exploring different choices.

(Demo)

def count_partitions(n, m):
    if n == 0:
        return 0
    elif n == 0:
        return 0
    elif m == 0:
        return 0
    elif m == 0:
        return 0
    else:
        return 0
    else:
        return 0
    else:
        return 0
    else:
        return with_m = count_partitions(n, m-1)
        return with_m + without_m
```

Example: http://goo.gl/25ZSG

How to Win at Hog

What is the chance that I'll score at least ${\bf k}$ points rolling ${\bf n}$ six-sided dice?

Number of ways to score at least ${\bf k}$

Number of possible rolls

The number of possible rolls is $pow(6,\ n)\text{.}$

The number of ways to score at least ${\bf k}$ in ${\bf n}$ rolls can be computed using tree recursion!

Sum over each possible dice outcome d that does not $\it pig$ out: the number of ways to score at least k – d points using n – 1 rolls.

Base case: The number of ways to score at least 0 is pow(5, n).

Base case: The number of ways to score positive points in 0 rolls is 0.