61A Lecture 8

Wednesday, September 18

Announcements

- •Project 1 is due Thursday 9/19 @ 11:59pm
- Midterm 1 is on Monday 9/23 from 7pm to 9pm
 - "2 review sessions on Saturday 9/21 2pm-4pm and 4pm-6pm in 1 Pimentel
 - •HKN review session on Sunday 9/22 from 4pm to 7pm in 2050 Valley LSB
 - Extra office hours over the weekend
 - •Includes topics up to and including this lecture
 - •Fill out the form on the website if you cannot attend
- Homework 3 is due in two weeks: Tuesday 10/1 @ 11:59pm
 - •It contains lots of recursion problems, for practice!
- •Optional Hog strategy contest ends Thursday 10/3 @ 11:59pm

Hog Contest Rules

- Up to two people submit one entry; Max of one entry per person.
- Your score is the number of entries against which you win more than 50% of the time.
- All strategies must be deterministic, pure functions of the current player scores! Non-deterministic strategies will be disqualified.
- One more special rule: Ham Hijinks. Choose -1 to swap the 4-sided and 6-sided dice.
- To enter: *submit proj1contest* with a file hog.py that defines a final_strategy function by **Thursday 10/3 @ 11:59pm**
- All winning entries will receive 2 points of extra credit
- The real prize: honor and glory

Fall 2011 Winners

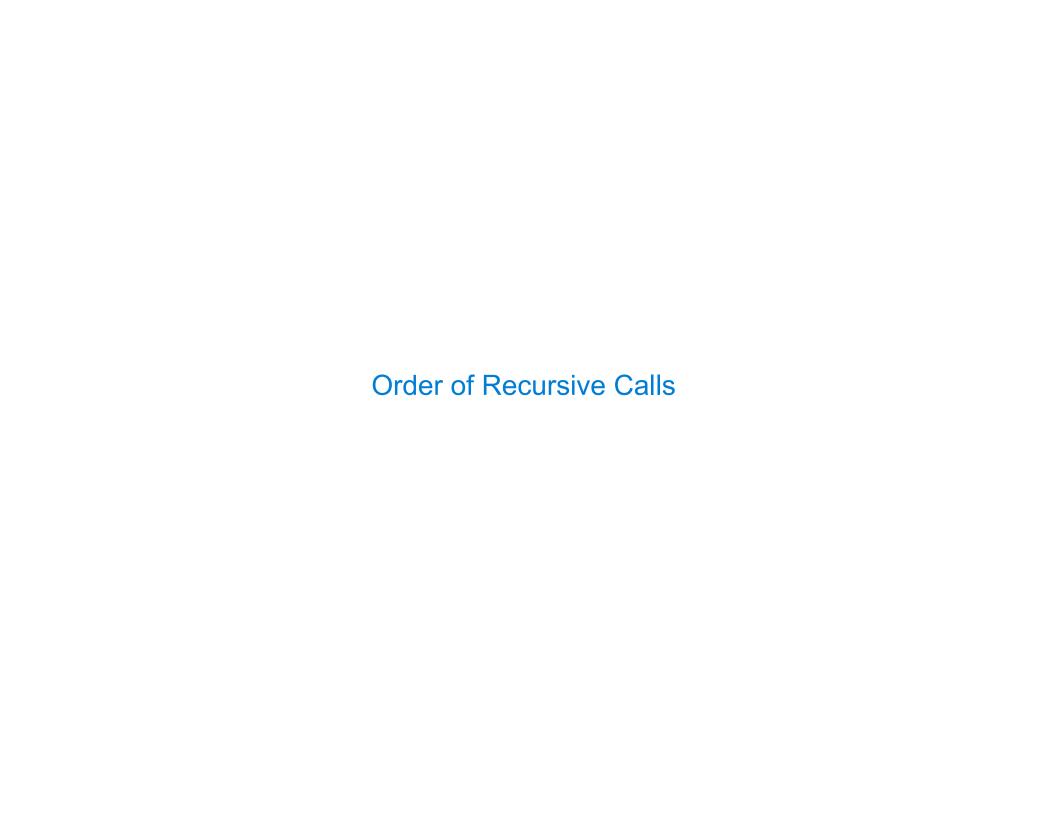
Keegan Mann, Yan Duan & Ziming Li, Brian Prike & Zhenghao Qian, Parker Schuh & Robert Chatham

Fall 2012 Winners

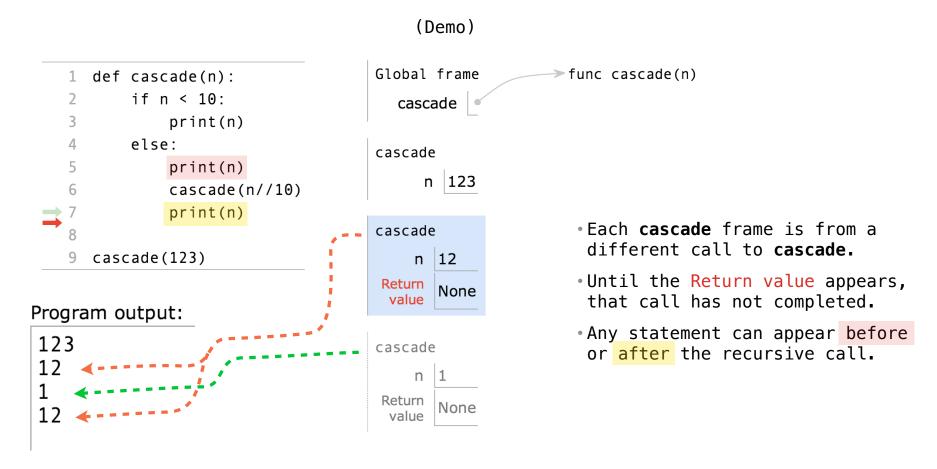
Chenyang Yuan, Joseph Hui

Fall 2013 Winners

YOUR NAME COULD BE HERE...
FOREVER!



The Cascade Function



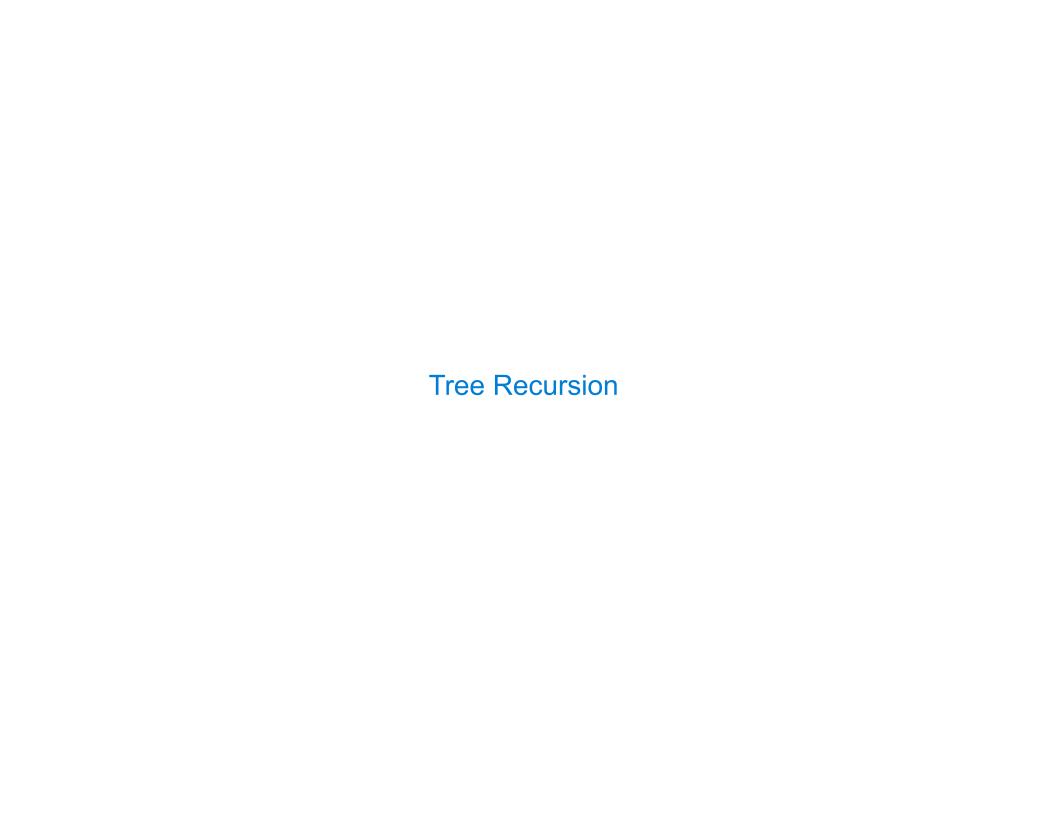
Example: http://goo.gl/090qzK

Two Definitions of Cascade

(Demo)

```
def cascade(n):
    if n < 10:
        print(n)
        print(n)
        if n >= 10:
        cascade(n//10)
        print(n)
        cascade(n//10)
        print(n)
```

- If two implementations are equally clear, then shorter is usually better.
- In this case, the longer implementation is more clear (at least to me).
- When learning to write recursive functions, put the base cases first.
- Both are recursive functions, even though only the first has typical structure.



Tree Recursion

Tree—shaped processes arise whenever executing the body of a recursive function makes **more than one** call to that function.

```
n: 1, 2, 3, 4, 5, 6, 7, 8, 9, ..., 35

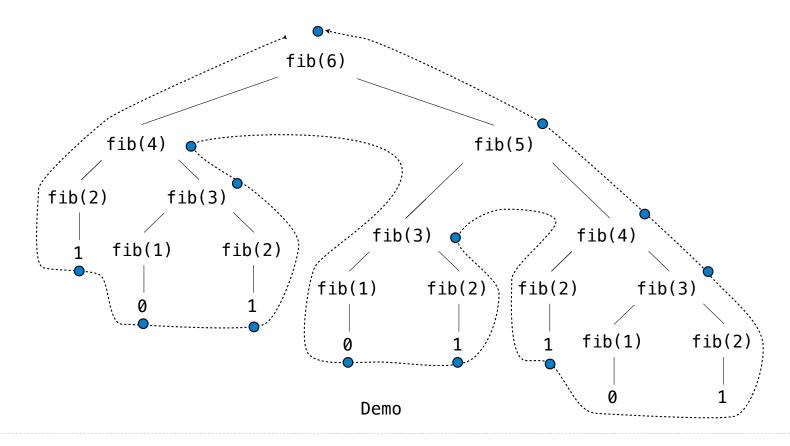
fib(n): 0, 1, 1, 2, 3, 5, 8, 13, 21, ..., 5,702,887
```

```
def fib(n):
    if n == 1:
        return 0
    elif n == 2:
        return 1
    else:
        return fib(n-2) + fib(n-1)
```



A Tree-Recursive Process

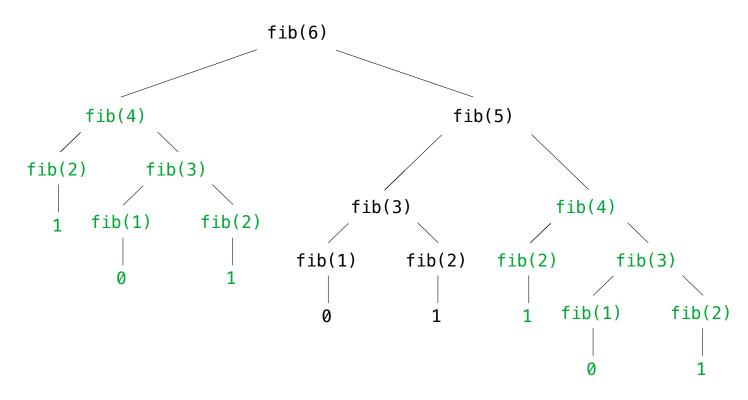
The computational process of **fib** evolves into a tree structure



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Repetition in Tree-Recursive Computation

This process is highly repetitive; fib is called on the same argument multiple times.



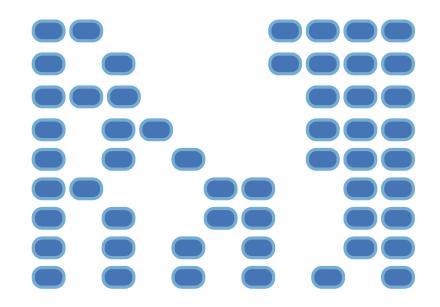
We can speed up this computation dramatically in a few weeks by remembering results.

Example: Counting Partitions

Counting Partitions

The number of **partitions** of a positive integer \mathbf{n} , using parts up to size \mathbf{m} , is the number of ways in which \mathbf{n} can be expressed as the sum of positive integer parts up to \mathbf{m} in increasing order.

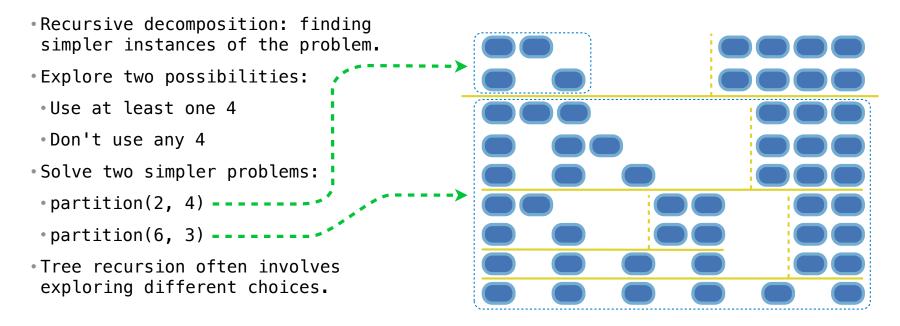
partition(6, 4)



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partition(6, 4)



Counting Partitions

The number of **partitions** of a positive integer n, using parts up to size m, is the number of ways in which n can be expressed as the sum of positive integer parts up to m in increasing order.

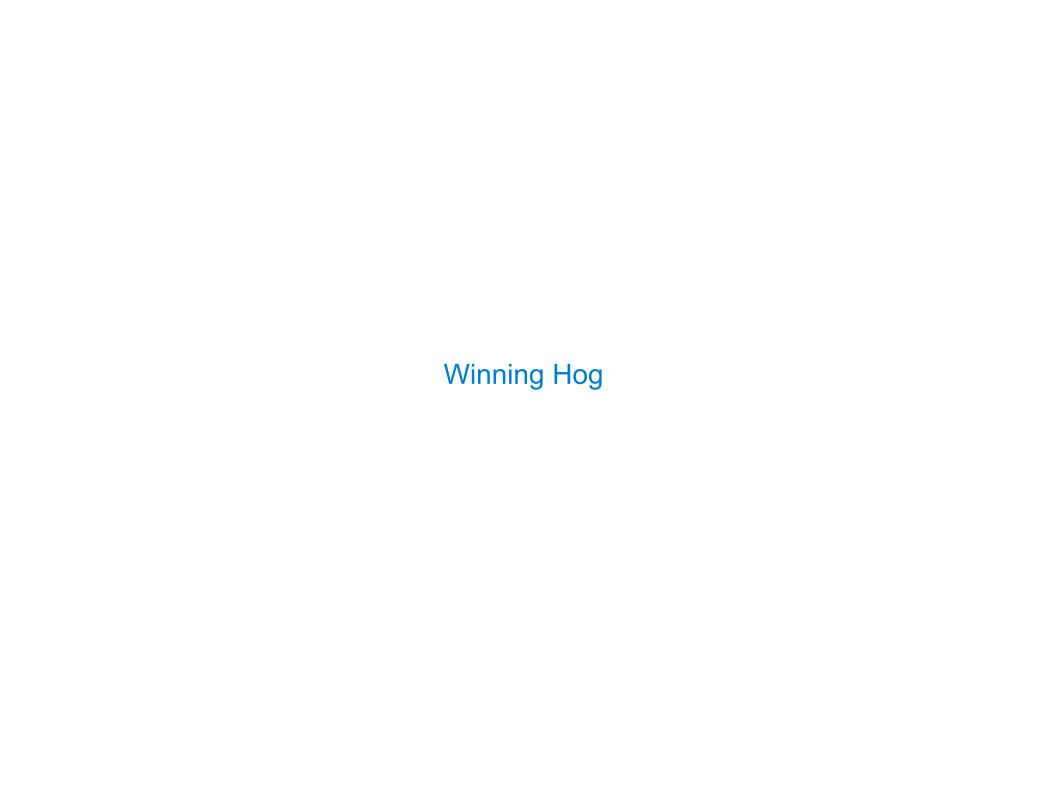
```
    Recursive decomposition: finding

                                       def count partitions(n, m):
simpler instances of the problem.
                                           if n == 0:
                                               return 1
•Explore two possibilities:
                                           elif n < 0:
•Use at least one 4
                                               return 0
Don't use any 4
                                           elif m == 0:
                                               return 0
•Solve two simpler problems:
•partition(2, 4) -----
                                          --> with m = count partitions(n-m, m)
•partition(6, 3) ------ without m = count partitions(n, m-1)
                                               return with m + without m

    Tree recursion often involves

exploring different choices.
                                       (Demo)
```

Example: http://goo.gl/25ZSGK



How to Win at Hog

What is the chance that I'll score at least k points rolling n six-sided dice?

Number of ways to score at least ${\bf k}$

Number of possible rolls

The number of possible rolls is pow(6, n).

The number of ways to score at least \mathbf{k} in \mathbf{n} rolls can be computed using tree recursion!

Sum over each possible dice outcome ${\bf d}$ that does not pig out: the number of ways to score at least ${\bf k}$ — ${\bf d}$ points using ${\bf n}$ — ${\bf 1}$ rolls.

Base case: The number of ways to score at least 0 is pow(5, n).

Base case: The number of ways to score positive points in 0 rolls is 0.