## 61A Lecture 4

Monday, September 9

## Announcements

Homework 1 due Tuesday 9/10 at 5pm; Late homework is not accepted!

•Quiz on Wednesday 9/11 released at 1pm, due Thursday 9/12 at 11:59pm

Open-computer: You can use the Python interpreter, watch course videos, and read the online text (<u>http://composingprograms.com</u>).

 $\ensuremath{\cdot} No \ensuremath{ external resources:}$  Please don't search for answers, talk to your classmates, etc.

-Content Covered: Lectures through last Friday 9/6; Same topics as Homework 1.

-Project 1 due next Thursday 9/19 at 11:59pm



### **Discussion Question**

Complete the following definition by placing an expression in			
<pre>def choose(total, selection):     """Return the number of ways to choose SELECTION items from TOTAL.</pre>			
choose(n, k) is typically defined in math as: n! / (n-k)! / k!			
>>> choose(5, 2) 10 >>> choose(20, 6) 38760 """			
<pre>ways = 1 selected = 0 while selected &lt; selection:     selected = selected + 1</pre>			
<pre>ways, total = ways *total // selected, total - 1 return ways</pre>			
Example: <u>http://goo.gl/38ch3o</u>			

**Iteration Example** 

## **Default Arguments**

(Demo)

# Designing Functions

	<pre>def square(x):     """Return X * X."""</pre>	<pre>def choose(n, d):     """Return the number of ways to choose D of N it</pre>
А	function's <i>domain</i> is the set	of all inputs it might possibly take as arguments.
	x is a number	n and d are positive integers with n greater than or equal to d.
А	function's <i>range</i> is the set	of output values it might possibly return.
	return value is a positive number	return value is a positive integer
Α	pure function's <b>behavior</b> is	the relationship it creates between input and output.
	return value is the square of the input	return value is the number of ways to choose d of n items.

ems."""

Characteristics of Functions



Generalization

## Generalizing Patterns with Arguments

Regular geometric shapes relate length and area.



**Higher-Order Functions** 

## Generalizing Over Computational Processes

The common structure among functions may be a computational process, rather than a number.

$$\sum_{k=1}^{5} \underbrace{k}_{k=1}^{5} = 1 + 2 + 3 + 4 + 5 = 15$$
$$\sum_{k=1}^{5} \underbrace{k}_{k=1}^{3} = 1^{3} + 2^{3} + 3^{3} + 4^{3} + 5^{3} = 225$$
$$\sum_{k=1}^{5} \underbrace{k}_{(4k-3) \cdot (4k-1)} = \frac{8}{3} + \frac{8}{35} + \frac{8}{99} + \frac{8}{195} + \frac{8}{323} = 3.04$$

(Demo)







### The Purpose of Higher-Order Functions

Functions are first-class: Functions can be manipulated as values in our programming language.

Higher-order function: A function that takes a function as an argument value or returns a function as a return value

Higher-order functions:

- Express general methods of computation
- Remove repetition from programs
- Separate concerns among functions

The Game of Hog

(Demo)