## 61A Lecture 2

Wednesday, September 4, 2013

# Names, Assignment, and User-Defined Functions 

Types of Expressions

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Primitive expressions:

## Types of Expressions

Primitive expressions: 2
Number or Numeral

## Types of Expressions

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## Call expressions:

## Types of Expressions



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Discussion Question 1

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>>> \(f=m i n\)
>>> f = max
>>> g, h = min, max
>>> max = g
\(\ggg \max (f(2, g(h(1,5), 3)), 4)\)
```


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Environment diagrams visualize the interpreter's process.

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## Global frame <br> pi 3.1416

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## $\Rightarrow 1$ from math import pi <br> $\rightarrow 2$ tau $=2$ * pi

Code (left):

Global frame
$\begin{array}{ll}\text { pi } & 3.1416\end{array}$

Frames (right):

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Code (left):
Frames (right):

Statements and expressions

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Each name is bound to a value

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                        Assignment statement
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Next to execute
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\section*{Assignment Statements}

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\[
\begin{aligned}
& 1 \quad a=1 \\
\Rightarrow & 2 \quad b=2 \\
\Rightarrow & 3 \quad b, a=a+b, b
\end{aligned}
\]

Global frame
a 1
b 2

\section*{Assignment Statements}


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Execution rule for assignment statements:

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1. Evaluate all expressions to the right of \(=\) from left to right.

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(Demo)

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\begin{aligned}
& 1 \mathrm{f}=\min \\
& 2 \mathrm{f}=\max \\
& 3 \mathrm{~g}, \mathrm{~h}=\min , \max \\
\Rightarrow & 4 \max =\mathrm{g} \\
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func min(...)


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>>> def <name>(<formal parameters>):
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Function signature indicates how many arguments a function takes
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    1 from operator import mul
    def square(x):
return mul(x, x)
square(-2)

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(Demo)

\title{
The Print Function
}

\title{
Pure Functions \& Non-Pure Functions
}

\section*{Pure Functions}
just return values

Non-Pure Functions
have side effects

\section*{Pure Functions \& Non-Pure Functions}

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Pure Functions \\ just return values
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\(-2\)


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Important: The interactive interpreter (>>>) displays the value of an expression, unless it is None

\section*{Nested Expressions with Print}
```

>>> print(print(1), print(2))
1
2
None None

```

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```

func print(...)

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1
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```


1 print(...):


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```

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1
2
None None

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```

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