

61A Lecture 32

Wednesday, November 14

Processing Sequential Data

Many data sets can be viewed and processed sequentially:

- The set of all Twitter posts
- Votes cast in a presidential election
- Sensor readings of an airplane
- The set of all positive integers

However, the sequence interface we developed previously does not always apply.

- A sequence has a finite, known length
- A sequence support element selection for any element

In most cases, satisfying the sequence interface requires storing the entire sequence in a computer's memory.

Today: Efficient representations of sequential data

Implicit Sequences

An implicit sequence is a representation of sequential data that does not explicitly store each element.

Example: The range class represents consecutive integers.

- The range is represented by two values: *start* and *end*.
- The length and elements are computed on demand.
- Constant space for arbitrarily large sequences.

Demo

The Iterator Interface

An iterator is an object that can provide the next element of a (possibly implicit) sequence.

The iterator interface has two methods:

- `__next__`(self) returns the next element in the sequence
- `__iter__`(self) returns an equivalent iterator (Why?)

The `next` function invokes the `__next__` method on its argument.

If there is no next element, then the `__next__` method of an iterator should raise a `StopIteration` exception.



Demo



The For Statement

```
for <name> in <expression>:  
    <suite>
```

1. Evaluate the header <expression>, which yields an iterable object.
2. For each element in that sequence, in order:
 - A. Bind <name> to that element in the first frame of the current environment.
 - B. Execute the <suite>.

An iterable object has a method `__iter__` that returns an iterator.

```
>>> counts = [1, 2, 3]  
>>> for item in counts:  
    print(item)
```

```
1  
2  
3
```

```
>>> counts = [1, 2, 3]  
>>> items = counts.__iter__()  
>>> try:  
    while True:  
        item = items.__next__()  
        print(item)  
except StopIteration:  
    pass
```

```
1  
2  
3
```

Generators and Generator Functions

A generator is an iterator backed by a generator function.

A generator function is a function that **yields** values.

When a generator function is called, it returns a generator.

```
>>> def letters_generator():  
    current = 'a'  
    while current <= 'd':  
        yield current  
        current = chr(ord(current)+1)
```

```
>>> for letter in letters_generator():  
    print(letter)
```

```
a  
b  
c  
d
```

Streams

A stream is a recursive list with an *explicit* first element and an *implicit* rest of the list.

```
class Stream(object):
    """A lazily computed recursive list."""
    class empty(object):
        def __repr__(self):
            return 'Stream.empty'
    empty = empty()

    def __init__(self, first, compute_rest=lambda: empty):
        assert callable(compute_rest), 'compute_rest must be callable.'
        self.first = first
        self._compute_rest = compute_rest
        self._rest = None

    @property
    def rest(self):
        """Return the rest of the stream, computing it if necessary."""
        if self._compute_rest is not None:
            self._rest = self._compute_rest()
            self._compute_rest = None
        return self._rest
```

Integer Streams

An integer stream is a stream of consecutive integers.

An integer stream starting at k consists of k and a function that returns the integer stream starting at $k+1$.

```
def make_integer_stream(first=1):  
    """Return a stream of consecutive integers, starting with first.  
  
    >>> s = make_integer_stream(3)  
    >>> s.first  
    3  
    >>> s.rest.first  
    4  
    """  
  
    def compute_rest():  
        return make_integer_stream(first+1)  
    return Stream(first, compute_rest)
```


Mapping a Function over a Stream

Mapping a function over a stream applies a function only to the first element at first, but computes the rest lazily.

```
def map_stream(fn, s):  
    """Map a function fn over the elements of a stream s."""  
    if s is Stream.empty:  
        return s  
    def compute_rest():  
        return map_stream(fn, s.rest)  
    return Stream(fn(s.first), compute_rest)
```

Demo

Filtering a Stream

When filtering a stream, processing continues until an element is kept in the output.


```
def filter_stream(fn, s):
    """Filter stream s with predicate function fn."""
    if s is Stream.empty:
        return s
    def compute_rest():
        return filter_stream(fn, s.rest)
    if fn(s.first):
        return Stream(s.first, compute_rest)
    else:
        return compute_rest()
```

A Stream of Primes

The stream of integers not divisible by any $k \leq n$ is:

- The stream of integers not divisible by any $k < n$,
- Filtered to remove any element divisible by n .
- Called the Sieve of Eratosthenes.

2, 3, ~~4~~, 5, ~~6~~, 7, ~~8~~, ~~9~~, ~~10~~, 11, ~~12~~, 13



Demo