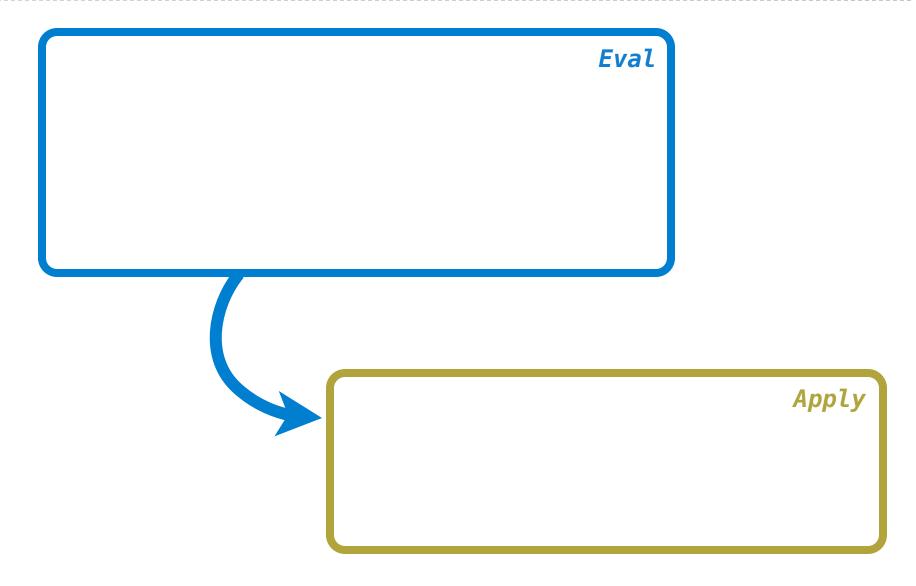
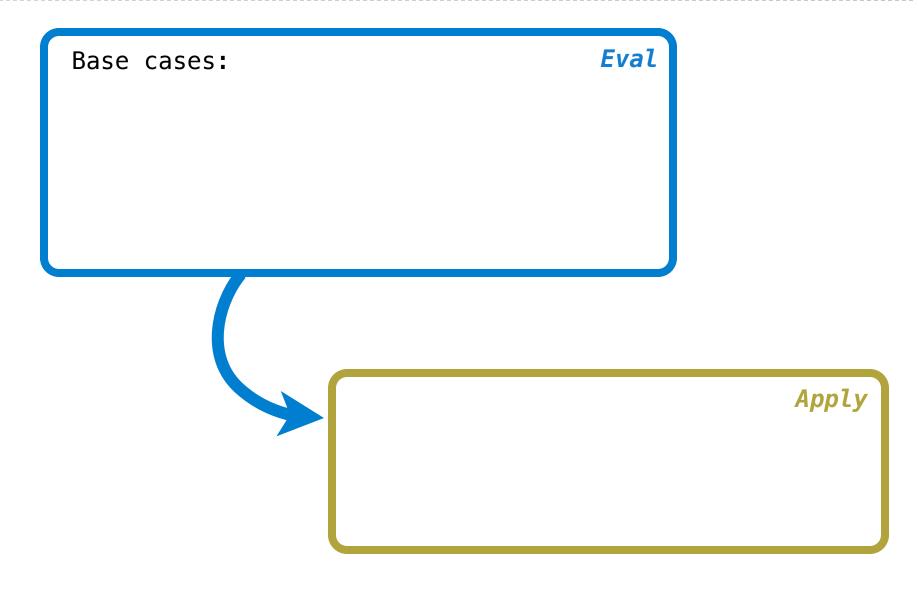
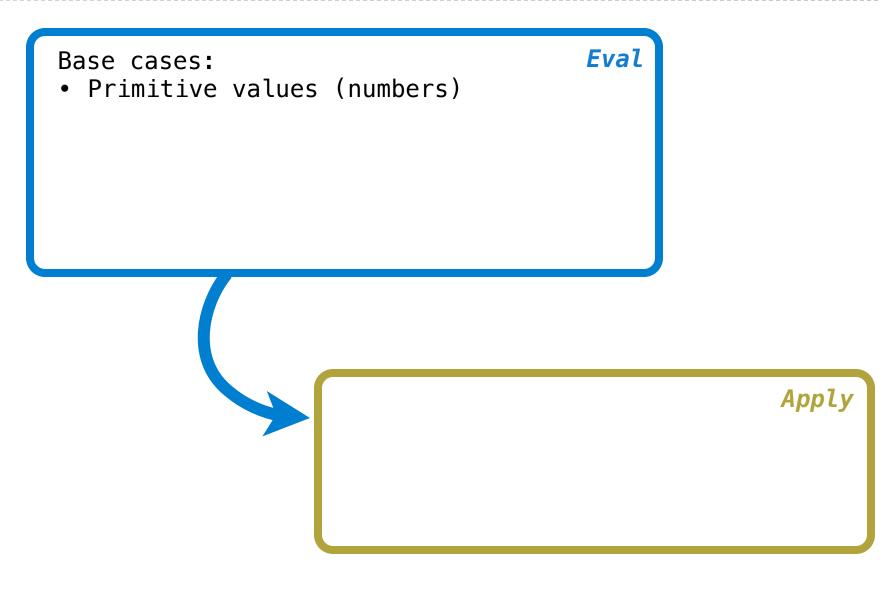
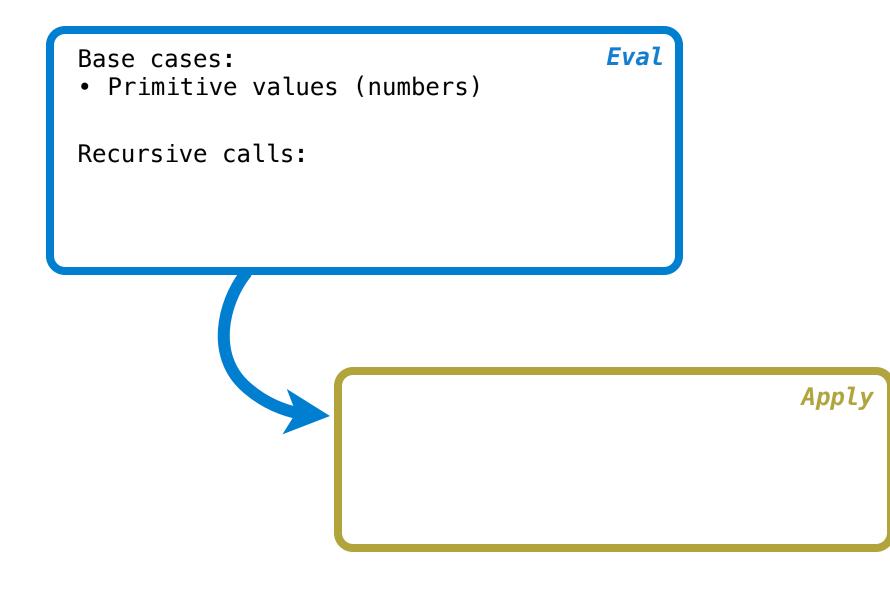
61A Lecture 29

Monday, November 5









Base cases:

• Primitive values (numbers)

Recursive calls:

• Eval(operands) of call expressions

Apply

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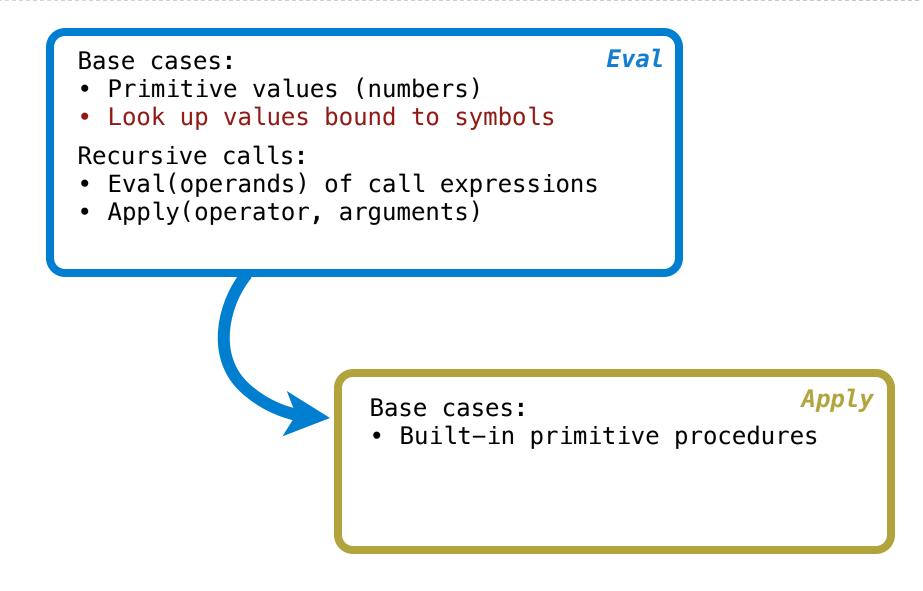
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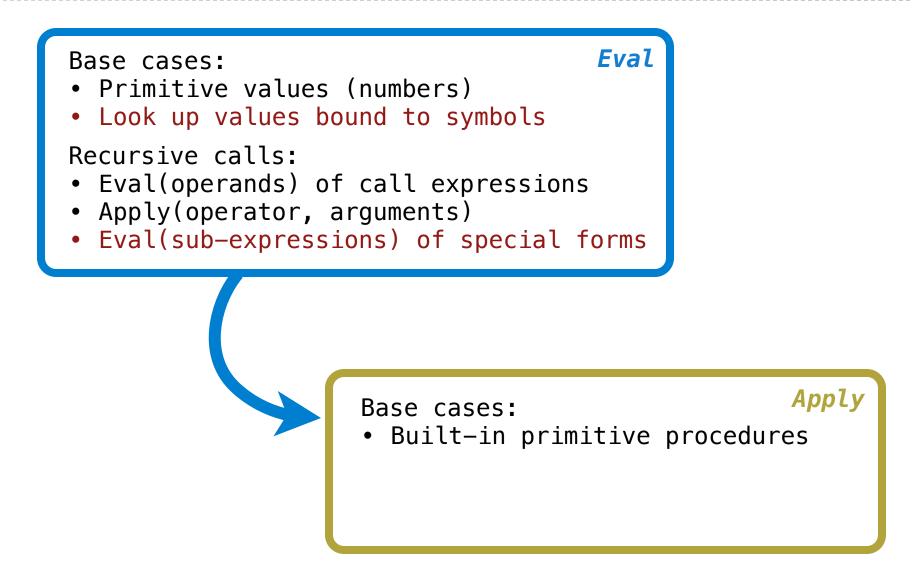
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Base cases:

Apply

• Built-in primitive procedures





Base cases:

- Primitive values (numbers)
- Look up values bound to symbols

Recursive calls:

- Eval(operands) of call expressions
- Apply(operator, arguments)
- Eval(sub-expressions) of special forms

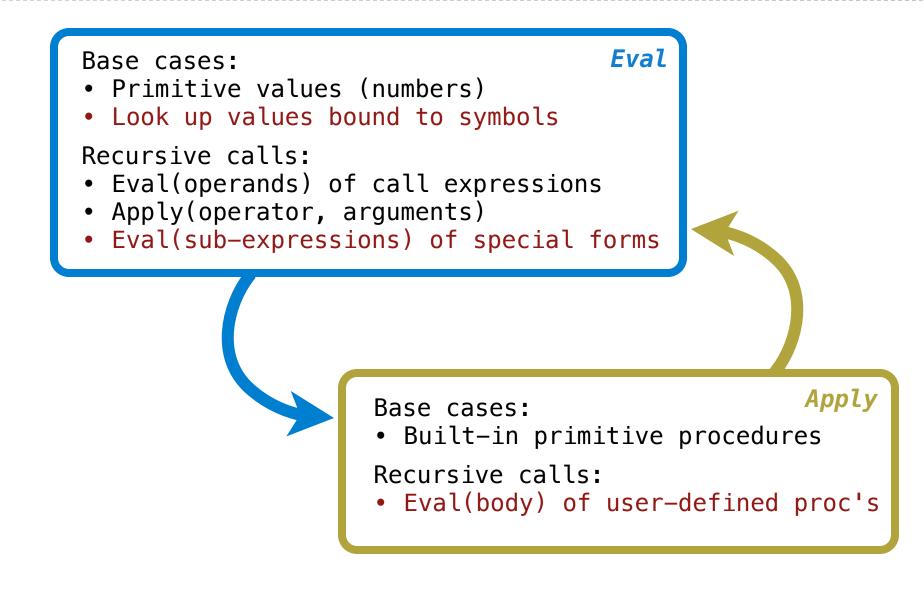
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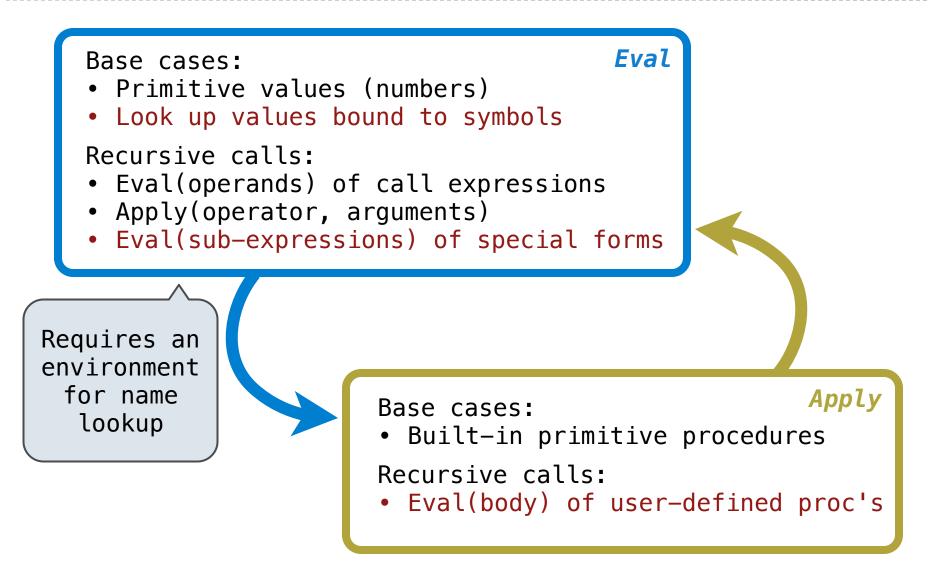
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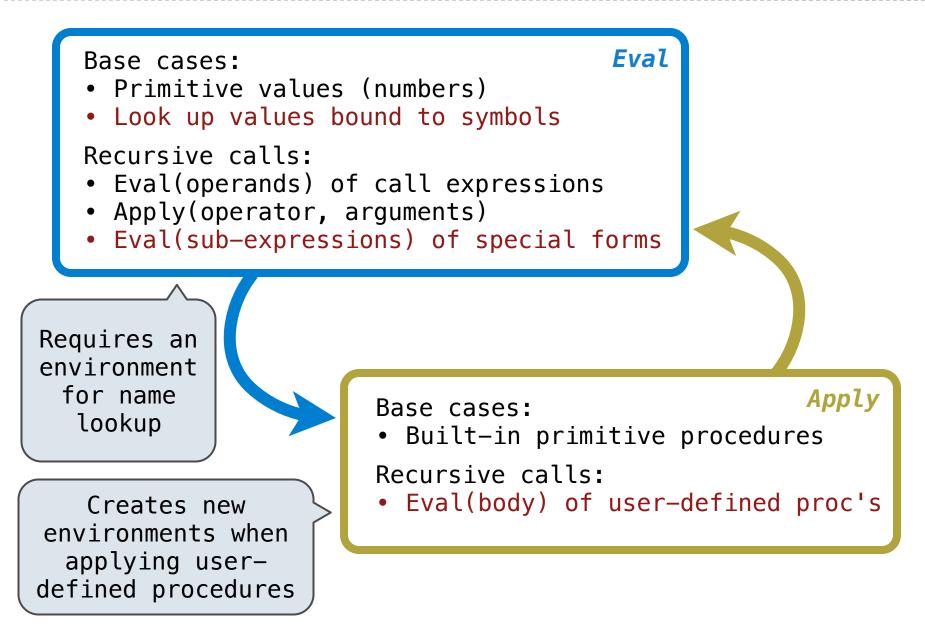
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Recursive calls:

• Eval(body) of user-defined proc's







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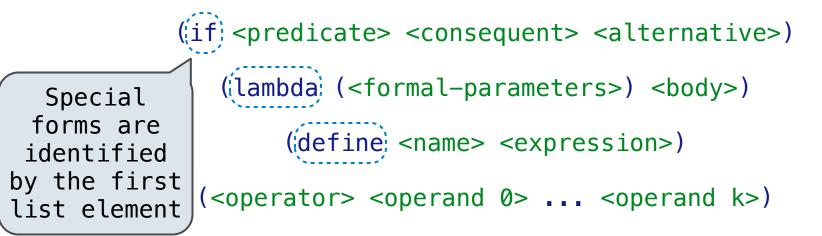
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(f (list 1 2))

Demo

Logical Special Forms

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Quotation

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Demo

Lambda Expressions

(lambda (<formal-parameters>) <body>)

(lambda (<formal-parameters>) <body>)

(lambda (x) (* x x))

```
(lambda (<formal-parameters>) <body>)
```

```
(lambda (x) (* x x))
```

class LambdaProcedure(object):

```
def __init__(self, formals, body, env):
    self.formals = formals
    self.body = body
    self.env = env
```

```
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```

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(lambda (x) (* x x))
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[no cont_a]		

[parent=g]	
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Define Expressions

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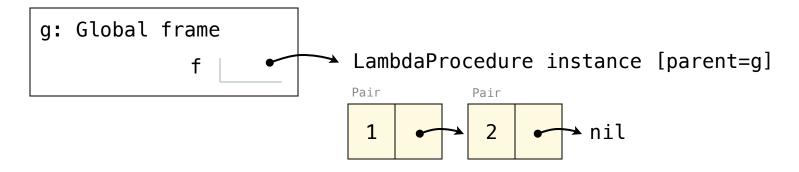
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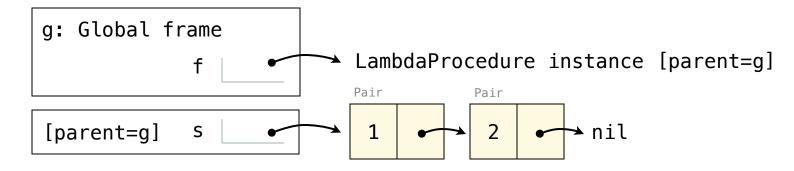
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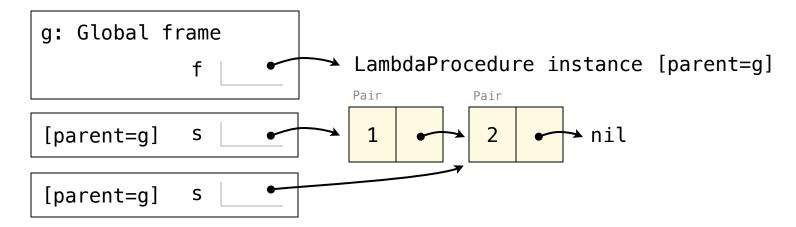
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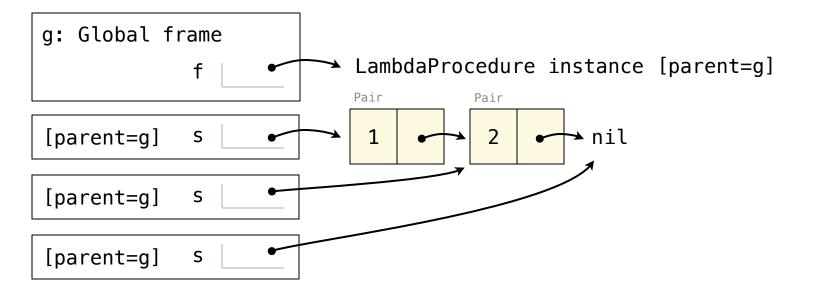
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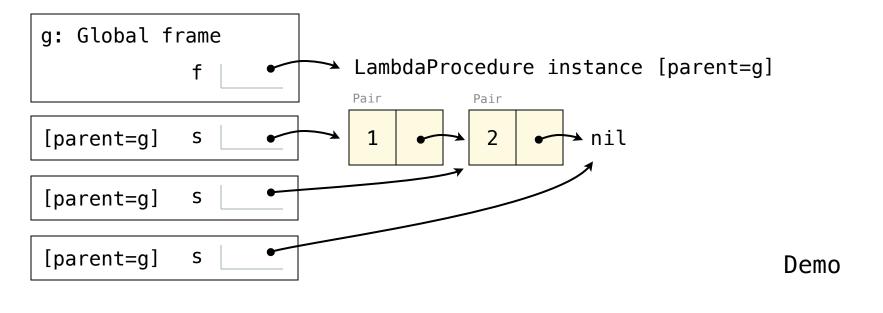
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Eval/Apply in Lisp 1.5

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```
apply[fn;x;a] =
      [atom[fn] \rightarrow [eq[fn;CAR] \rightarrow caar[x];
                     eq[fn;CDR] - cdar[x];
                     eq[fn;CONS] \rightarrow cons[car[x];cadr[x]];
                     eq[fn;ATOM] \rightarrow atom[car[x]];
                     eq[fn; EQ] \rightarrow eq[car[x]; cadr[x]];
                      T \rightarrow apply[eval[fn;a];x;a]];
      eq[car[fn];LAMBDA] \rightarrow eval[caddr[fn];pairlis[cadr[fn];x;a]];
      eq[car[fn]; LABEL] \rightarrow apply[caddr[fn]; x; cons[cons[cadr[fn];
                                                       caddr[fn]];a]]]
eval[e;a] = [atom[e] - cdr[assoc[e;a]];
       atom[car[e]]→
                  [eq[car[e],QUOTE] - cadr[e];
                 eq[car[e];COND] \rightarrow evcon[cdr[e];a];
                 T \rightarrow apply[car[e]; evlis[cdr[e]; a]; a]];
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Special form to create dynamically scoped procedures

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```

(g 3 7)