## What Are Programs?

Once upon a time, people wrote programs on blackboards Every once in a while, they would "punch in" a program

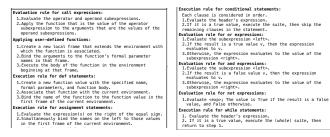
# 61A Lecture 20

Friday, October 12



Now, we type programs as text files using editors like Emacs Programs are just text (or cards) until we interpret them http://en.wikipedia.org/wiki/File:IBM\_Port-A-Punch.jpg

### How Are Evaluation Procedures Applied?



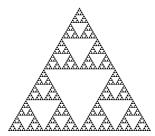
#### The most fundamental idea in computer science:

An interpreter, which determines the meaning of expressions in a programming language, is just another program.

#### **Recursive Functions**

Definition: A function is called *recursive* if the body of that function calls itself, either directly or indirectly.

Implication: Executing the body of a recursive function may require applying that function again.





Drawing Hands, by M. C. Escher (lithograph, 1948)

## Example: Pig Latin

Yes, you're in college, learning Pig Latin.

def pig\_latin(w): """Return the Pig Latin equivalent of English word w.""" if starts\_with\_a\_vowel(w):

return w + 'ay' return pig\_latin(w[1:] + w[0])

def starts\_with\_a\_vowel(w): """Return whether w begins with a vowel.""" return w[0].lower() in 'aeiou'

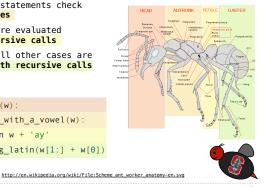
# The Anatomy of a Recursive Function

- The **def statement header** is similar to other functions
- Conditional statements check for base cases
- Base cases are evaluated without recursive calls
- Typically, all other cases are evaluated with recursive calls

#### def pig\_latin(w):

if starts\_with\_a\_vowel(w): return w + 'ay' return pig\_latin(w[1:] + w[0])

Recursive functions are like ants (more or less)



Demo

## Iteration vs Recursion

Iteration is a special case of recursion

#### $4!=4\cdot 3\cdot 2\cdot 1=24$

	Using iterative control:	Using recursion:
	<pre>def fact_iter(n): total, k = 1, 1 while k &lt;= n:     total, k = total*k, k+1 return total</pre>	<pre>def fact(n): if n == 1:     return 1 return n * fact(n-1)</pre>
Math:	$n! = \prod_{k=1}^{n} k$	$n! = \begin{cases} 1 & \text{if } n = 1 \\ n \cdot (n-1)! & \text{otherwise} \end{cases}$
Names:	n, total, k, fact_iter	n, fact Demo

## The Recursive Leap of Faith

	<pre>def fact(n): if n == 1: return 1 return n * fact(n-1)</pre>
Is fact	implemented correctly?

- 1. Verify the base case.
- Treat fact(n-1) as a functional abstraction!
- 3. Assume that fact(n-1) is correct.
- Verify that fact(n) is correct, assuming that fact(n-1) correct.



Photo by Kevin Lee, Preikestolen, Norway

### Example: Reverse a String

def reverse(s):
"""Return the reverse of a string s."""

**Recursive idea:** The reverse of a string is the reverse of the rest of the string, followed by the first letter.

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reverse(s[1:]) + s[0]

Base Case: The reverse of an empty string is itself.

### **Converting Recursion to Iteration**

Can be tricky! Iteration is a special case of recursion

Idea: Figure out what state must be maintained by the function

<pre>def reverse(s): if s == '': return s return (reverse(s[1:])) + (s[0])</pre>			
What's reversed How to get e	ach		
so far?			
<pre>def reverse_iter(s): r, i = '', 0 while i &lt; len(s):     r, i = s[i] + r, i + 1 return r</pre>			

## Converting Iteration to Recursion

More formulaic: Iteration is a special case of recursion

Idea: The state of an iteration can be passed as parameters

