

61A Lecture 18

Monday, October 8

Relationship to the Python Object System

Object attributes are stored as dictionaries

Some special names, `__<name>__`, require special handling

An object has an "attribute" called `__dict__` that is a dictionary of its user-defined instance attributes

Demo

In Python, classes have classes too

The equivalent of `init_instance` can be customized (metaclass)

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- String representations of objects
- Multiple representations of abstract data types
- Property methods

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Strings are important: they represent *language* and *programs*

In Python, all objects produce two string representations

- The "str" is legible to **humans**
- The "repr" is legible to the **Python interpreter**

When the "str" and "repr" **strings are the same**, we're doing **something right** in our programming language!

The "repr" String for an Object

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```
>>> repr(min)
'<built-in function min>'
```

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>>> import datetime
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>>> str(today)
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Demo

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The behavior of str:

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- If no `__str__` attribute is found, uses repr string (demo)
- **Question:** How would we implement this behavior?
- `str` is a class, not a function

Interfaces

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An *interface* is a **set of shared messages**, along with a specification of **what they mean**

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Message passing allows **different data types** to respond to the **same message**

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An *interface* is a **set of shared messages**, along with a specification of **what they mean**

Classes that implement `__repr__` and `__str__` methods *that return Python- and human-readable strings* thereby **implement an interface** for producing Python string representations

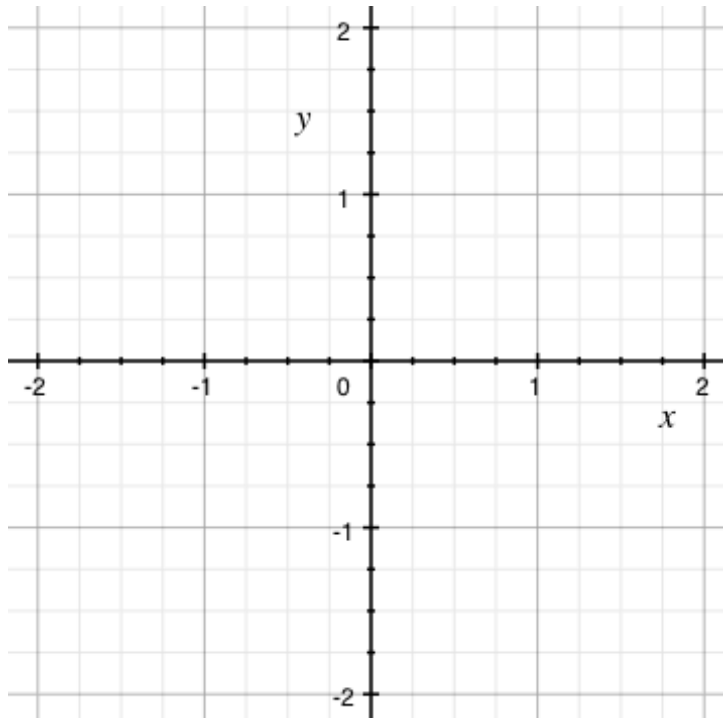
Multiple Representations of Abstract Data

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Rectangular and polar representations for complex numbers

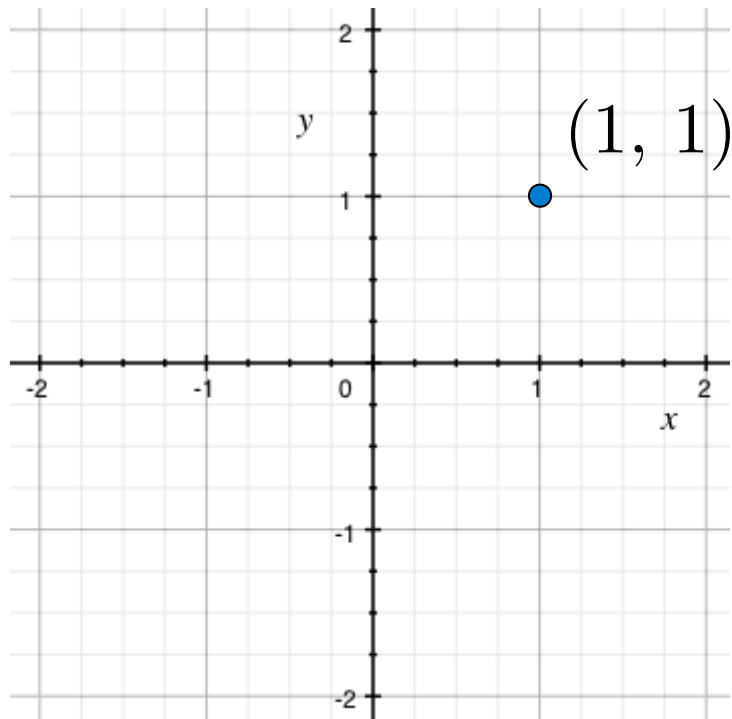
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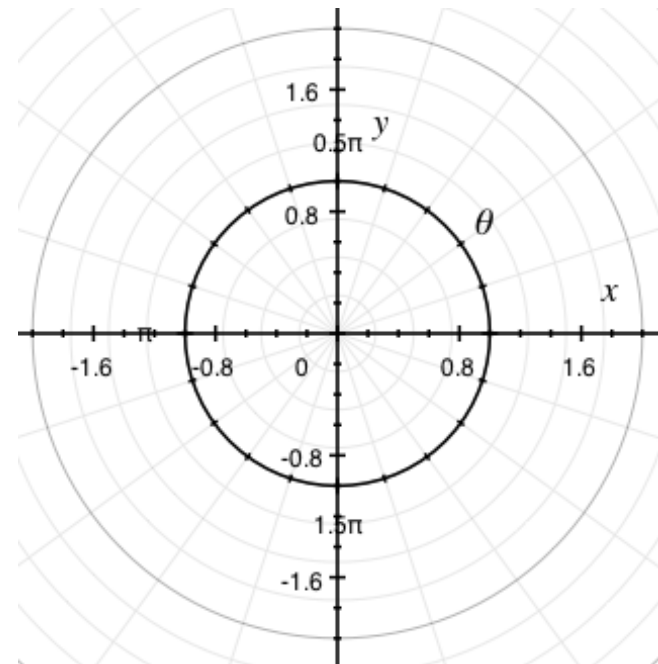
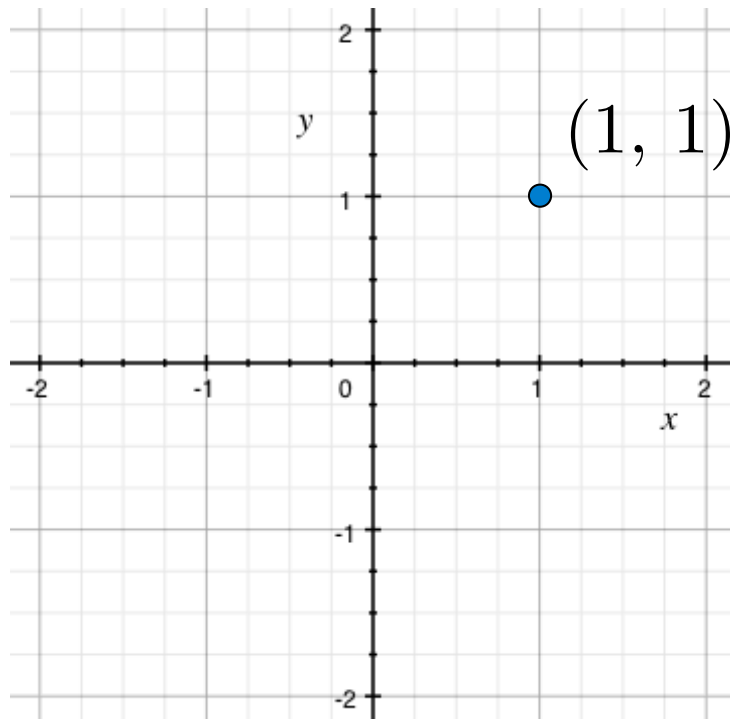
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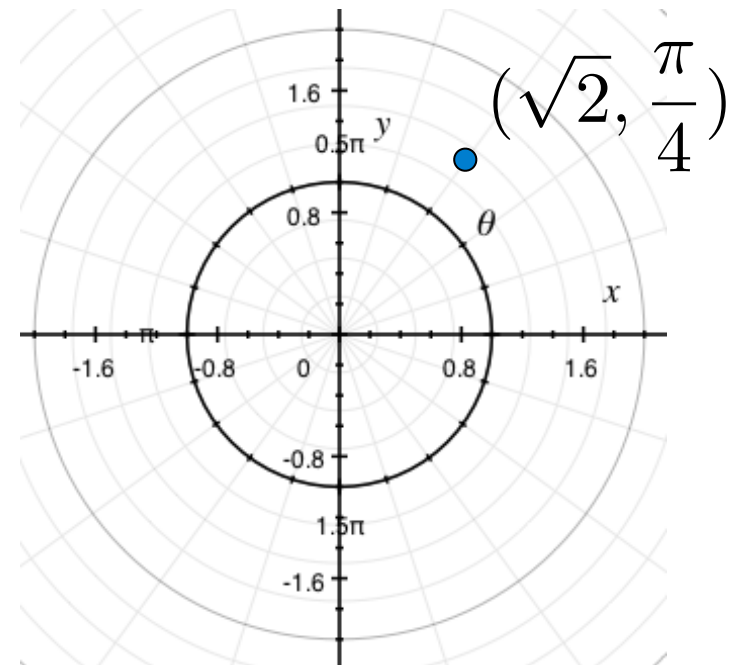
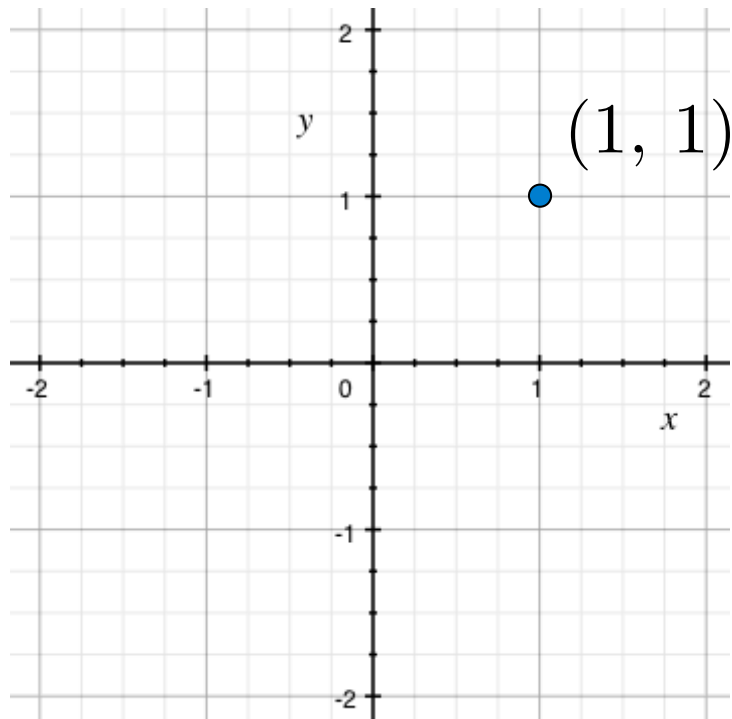
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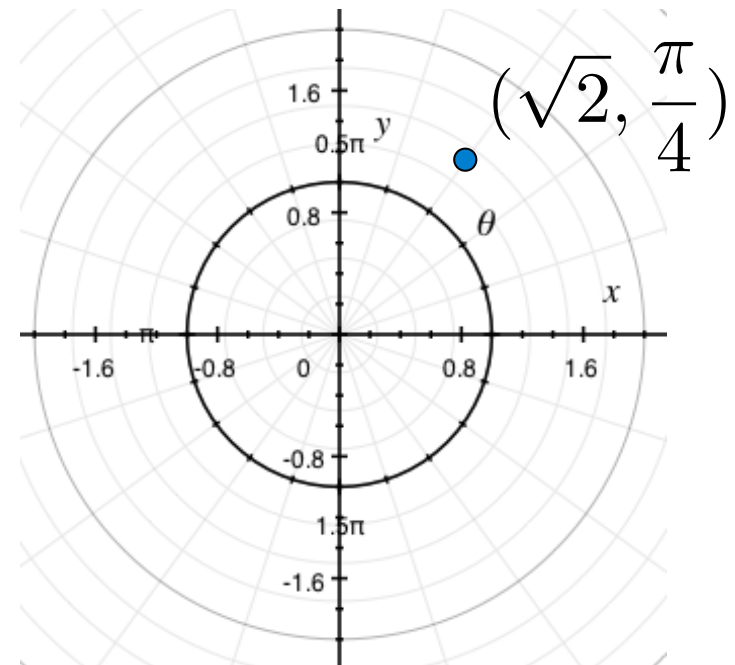
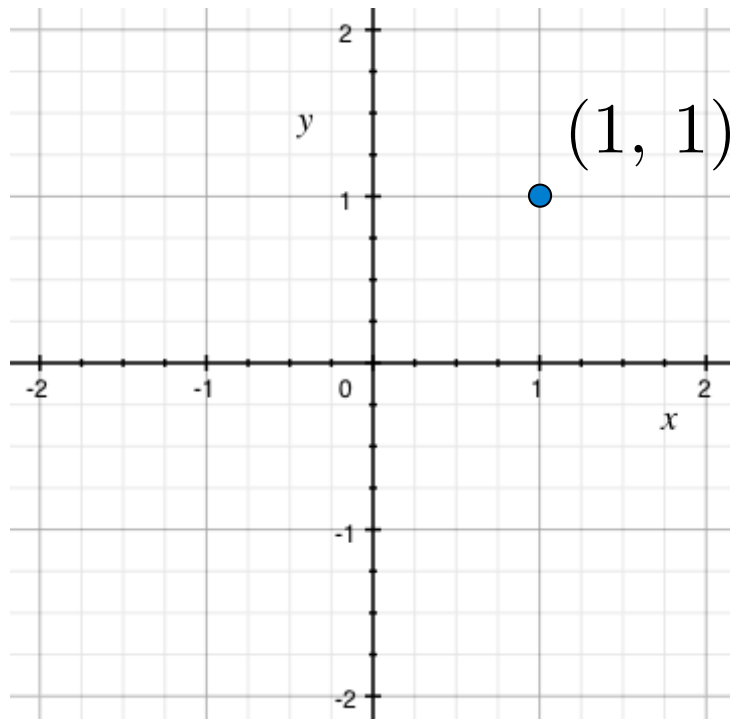
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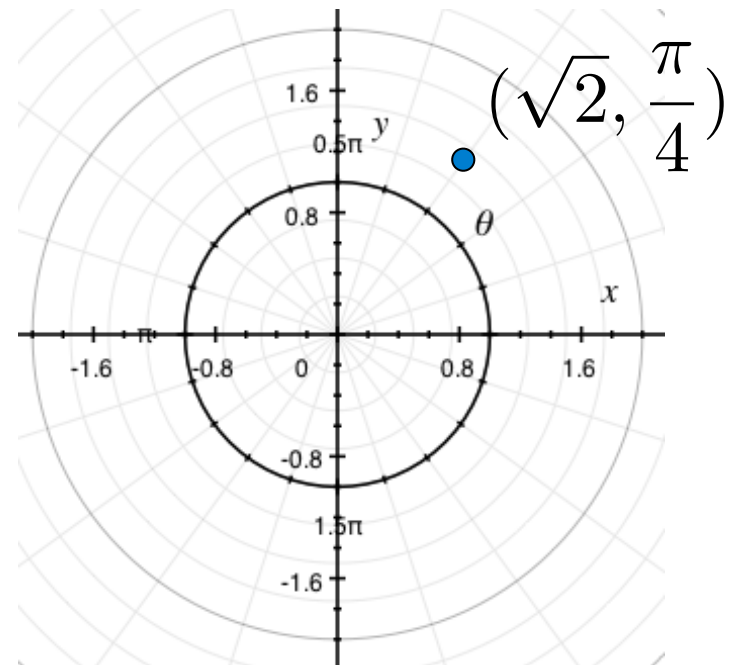
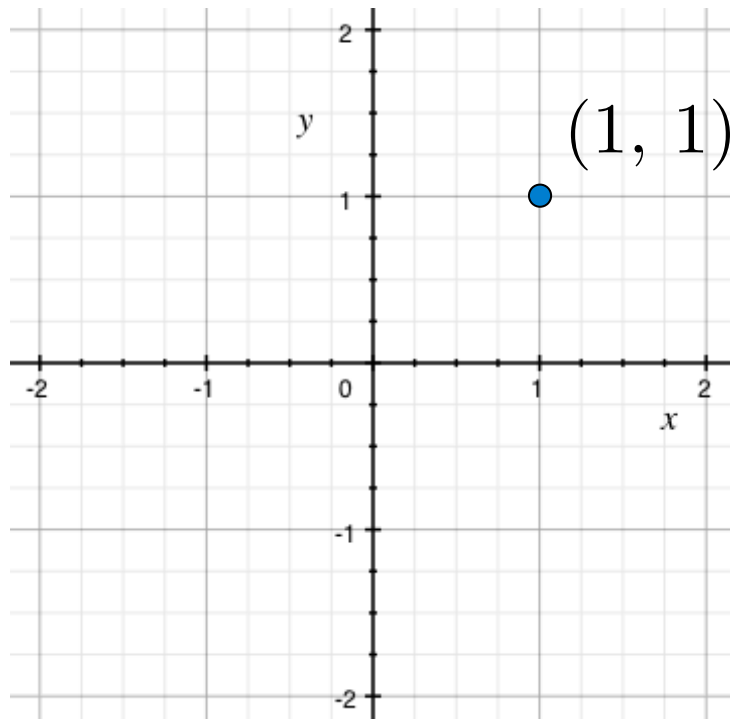
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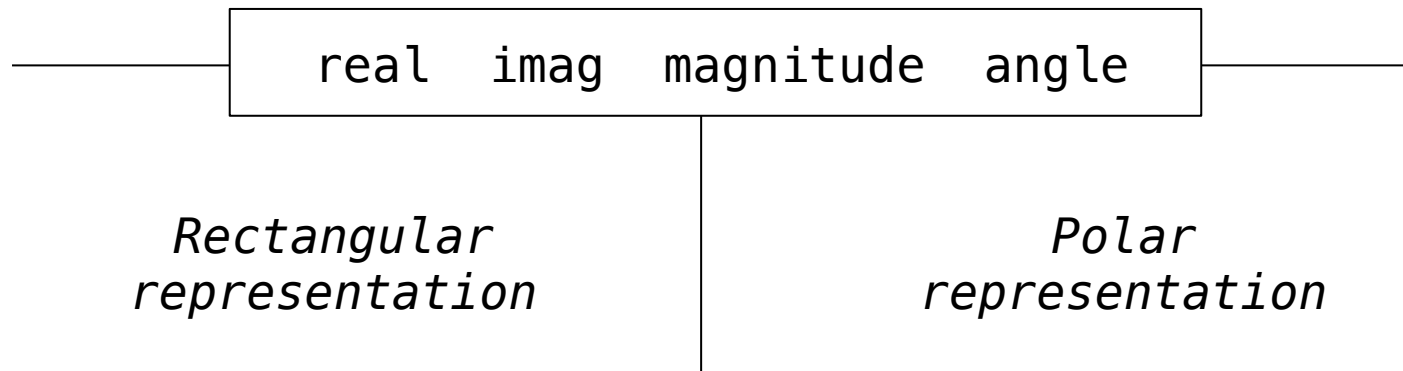
Some mathematical operations are easier on one than the other

Arithmetic Abstraction Barriers

*Rectangular
representation*

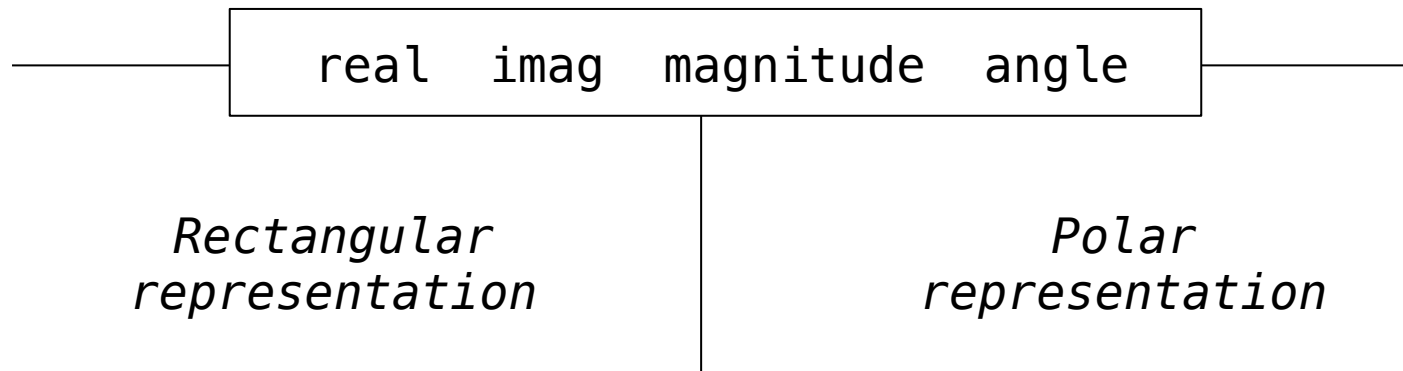
*Polar
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Arithmetic Abstraction Barriers

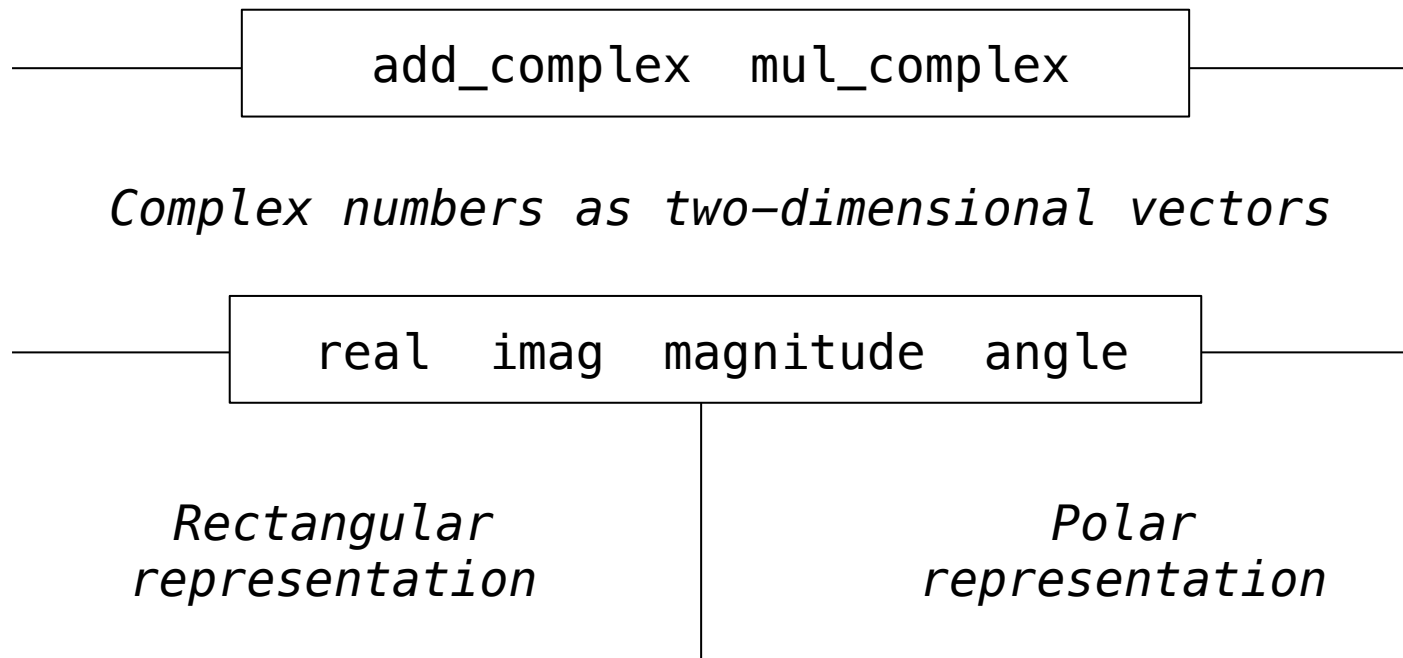


Arithmetic Abstraction Barriers

Complex numbers as two-dimensional vectors

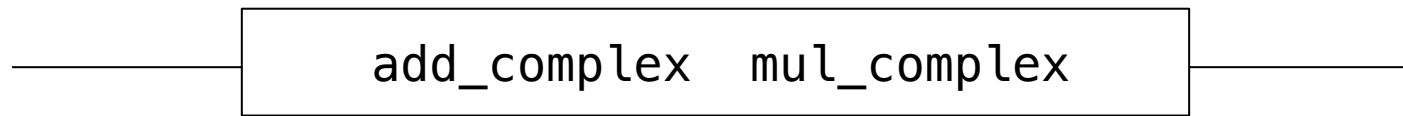


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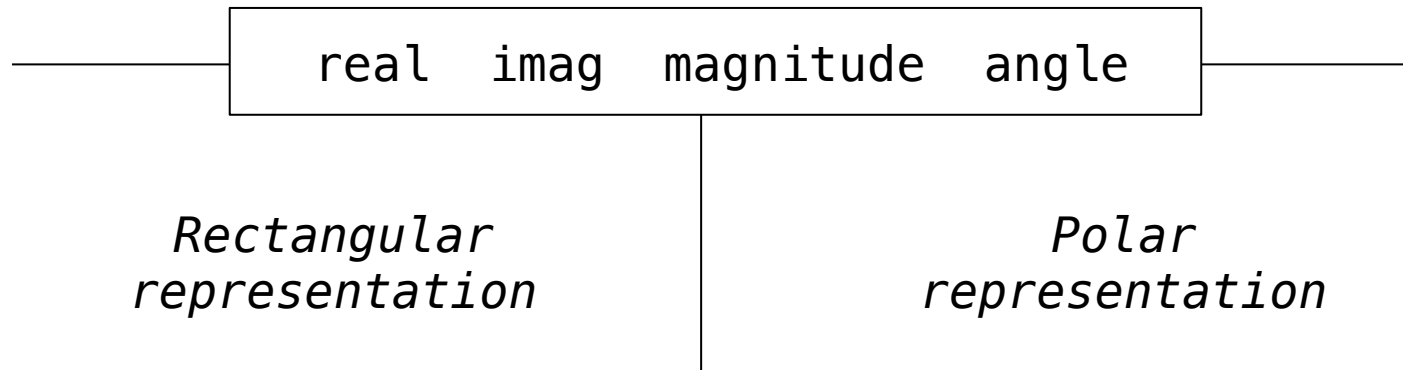


Arithmetic Abstraction Barriers

Complex numbers in the problem domain



Complex numbers as two-dimensional vectors



An Interface for Complex Numbers

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>>> def mul_complex(z1, z2):  
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Property Methods

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The Rectangular Representation

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class ComplexRI(object):
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class ComplexRI(object):  
    def __init__(self, real, imag):  
        self.real = real  
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```
class ComplexRI(object):  
  
    def __init__(self, real, imag):  
        self.real = real  
        self.imag = imag  
  
    @property  
    def magnitude(self):  
        return (self.real ** 2 + self.imag ** 2) ** 0.5
```

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Property decorator: "Call this function on attribute look-up"

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    def magnitude(self):  
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    def angle(self):  
        return atan2(self.imag, self.real)
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`math.atan2(y,x)`: Angle between x-axis and the point (x,y)

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math.atan2(y,x): Angle between x-axis and the point (x,y)

```
    def __repr__(self):  
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class ComplexMA(object):  
    def __init__(self, magnitude, angle):  
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    @property  
    def real(self):  
        return self.magnitude * cos(self.angle)
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class ComplexMA(object):  
  
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        self.magnitude = magnitude  
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    @property  
    def real(self):  
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    def real(self):
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    @property
    def imag(self):
        return self.magnitude * sin(self.angle)

    def __repr__(self):
        return 'ComplexMA({0}, {1})'.format(self.magnitude,
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Using Complex Numbers

Either type of complex number can be passed as either argument to `add_complex` or `mul_complex`

```
>>> def add_complex(z1, z2):  
    return ComplexRI(z1.real + z2.real,  
                     z1.imag + z2.imag)  
  
>>> def mul_complex(z1, z2):  
    return ComplexMA(z1.magnitude * z2.magnitude,  
                     z1.angle + z2.angle)  
  
>>> from math import pi
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>>> from math import pi  
>>> add_complex(ComplexRI(1, 2), ComplexMA(2, pi/2))  
ComplexRI(1.000000000000000002, 4.0)
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>>> add_complex(ComplexRI(1, 2), ComplexMA(2, pi/2))  
ComplexRI(1.0000000000000000002, 4.0)  
>>> mul_complex(ComplexRI(0, 1), ComplexRI(0, 1))  
ComplexMA(1.0, 3.141592653589793)
```

Special Methods

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Adding instances of user-defined classes use `__add__` method

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>>> ComplexRI(1, 2) + ComplexMA(2, 0)
ComplexRI(3.0, 2.0)
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Adding instances of user-defined classes use `__add__` method

Demo

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ComplexRI(3.0, 2.0)
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```

<http://getpython3.com/diveintopython3/special-method-names.html>

<http://docs.python.org/py3k/reference/datamodel.html#special-method-names>