## 61A Lecture 7

Monday, September 10

## Hog Contest Rules

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## Fall 2011 Winners

Keegan Mann,
Yan Duan \& Ziming Li, Brian Prike \& Zhenghao Qian, Parker Schuh \& Robert Chatham

## Choosing Names

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```
You can't depend upon code that hasn't been tested
Run your old tests again after you make new changes
```

Function Decorators
(demo)

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```
@trace1
def triple(x):
    return 3 * x
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def triple(x):
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triple = trace1(triple)
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Why not
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def triple(x):
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Functional Abstractions

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If the name "square" were bound to a built-in function, sum_squares would still work identically

Data


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## Student seating preferences at MIT


http://www.skyrill.com/seatinghabits/

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Python Objects

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- Implement an object system using built-in objects


## Native Data Types

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Properties of native data types:

1. There are primitive expressions that evaluate to native objects of these types.
2. There are built-in functions, operators, and methods to manipulate these objects.

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Numeric types in Python:

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(demo)

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>>> type(1.5)
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Working with Real Numbers Material

Care must be taken when computing with real numbers! (Demo)

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## Working with Real Numbers

Bonus Material

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## Representing real numbers:



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http://en.wikipedia.org/wiki/File:IEEE_754_Double_Floating_Point_Format.svg

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if $x$ == $y$ :
return True
return approx_eq_1(x, y) or approx_eq_2(x, y)

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>>> def near(x, f, g):
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Coming Soon: Data Abstraction

