

# 61A Lecture 25

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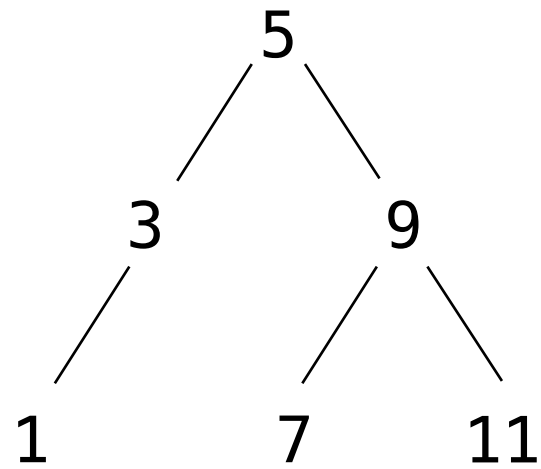
Friday, October 28

# From Last Time: Adjoining to a Tree Set

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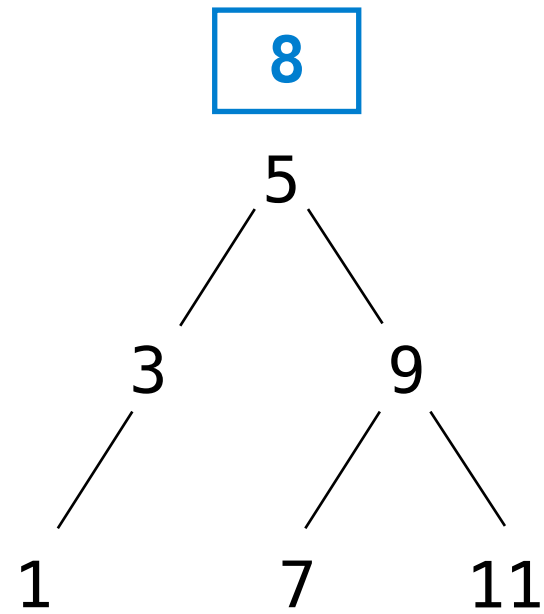
# From Last Time: Adjoining to a Tree Set

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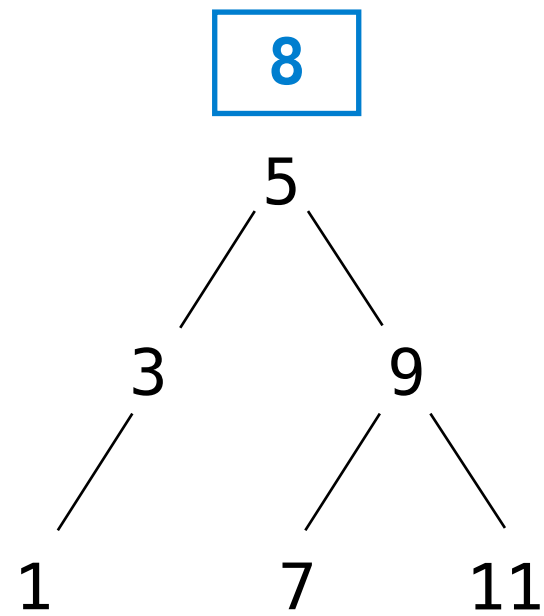
# From Last Time: Adjoining to a Tree Set

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## From Last Time: Adjoining to a Tree Set

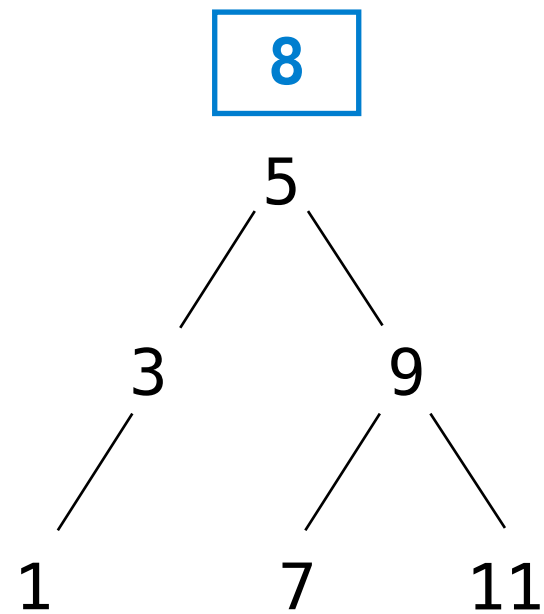
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*Right!*

## From Last Time: Adjoining to a Tree Set

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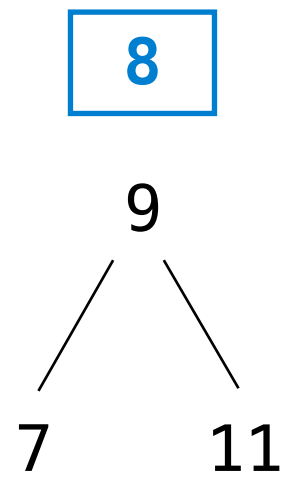
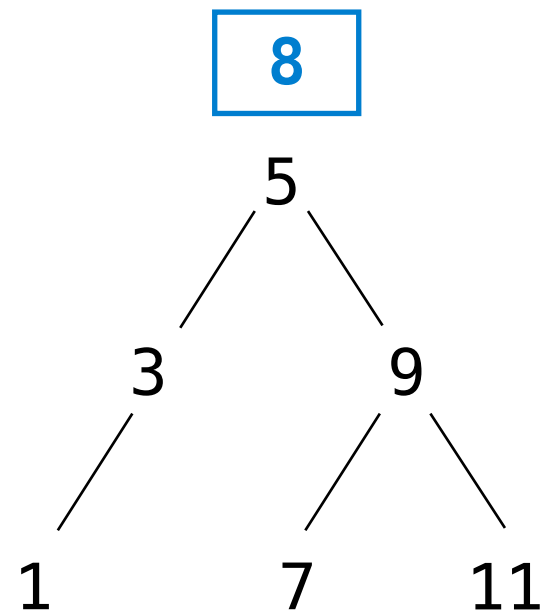


*Right!*



# From Last Time: Adjoining to a Tree Set

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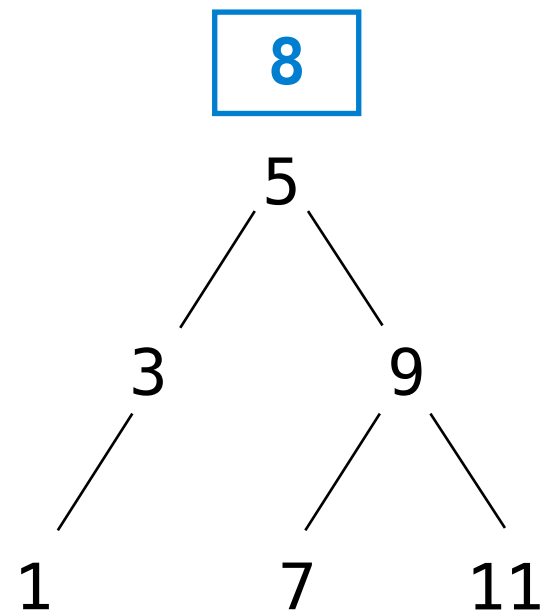


*Right!*

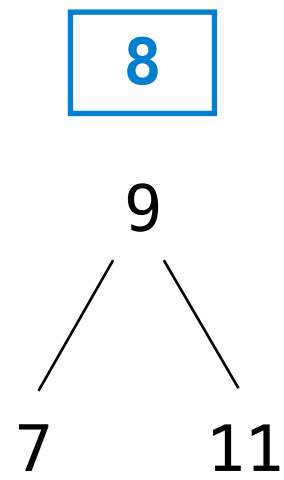


# From Last Time: Adjoining to a Tree Set

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*Right!*



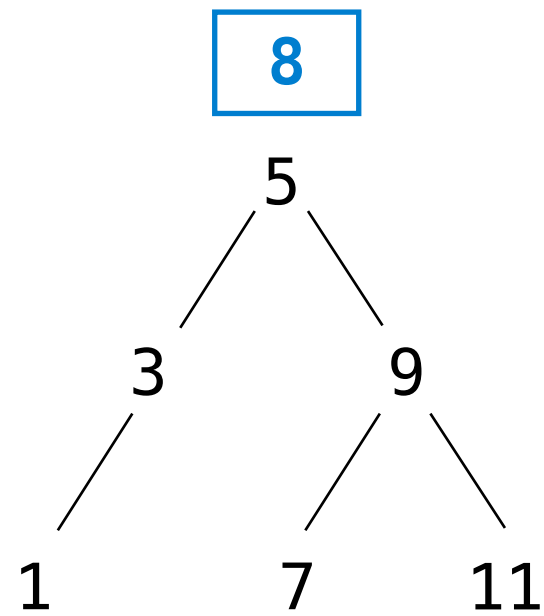
*Left!*



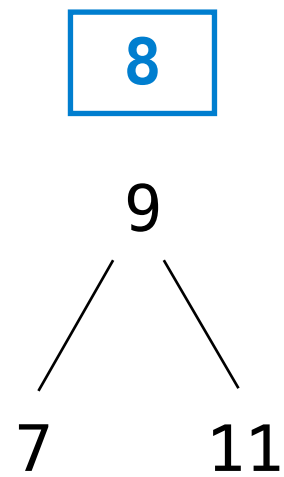


# From Last Time: Adjoining to a Tree Set

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*Right!*

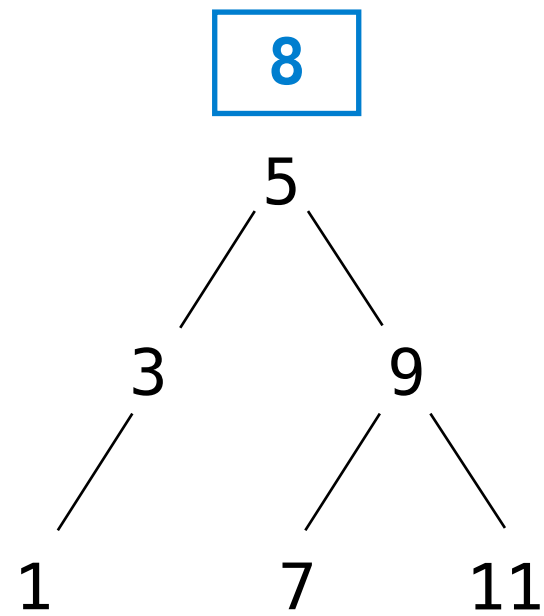


*Left!*

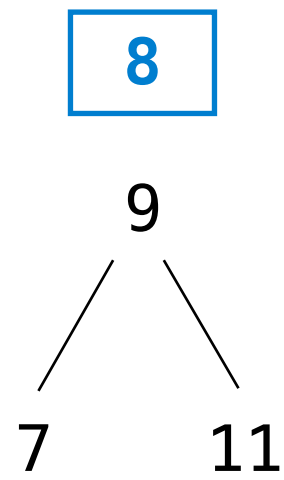


# From Last Time: Adjoining to a Tree Set

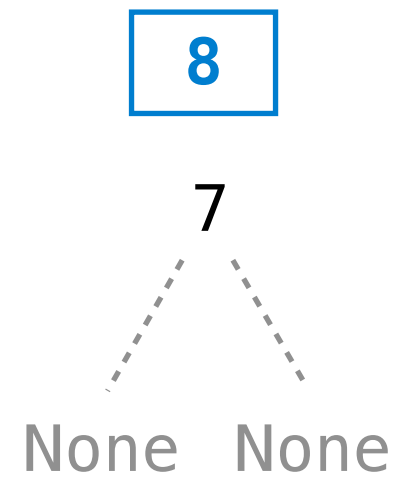
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*Right!*

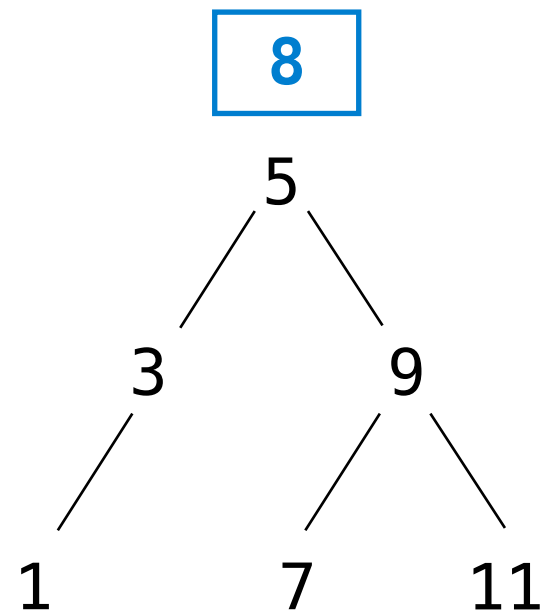


*Left!*

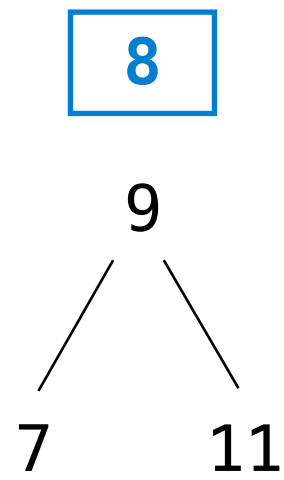


# From Last Time: Adjoining to a Tree Set

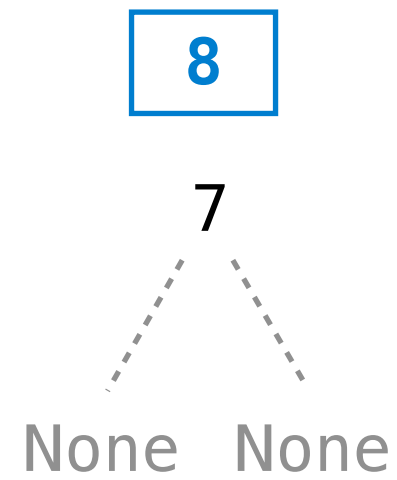
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*Right!*



*Left!*

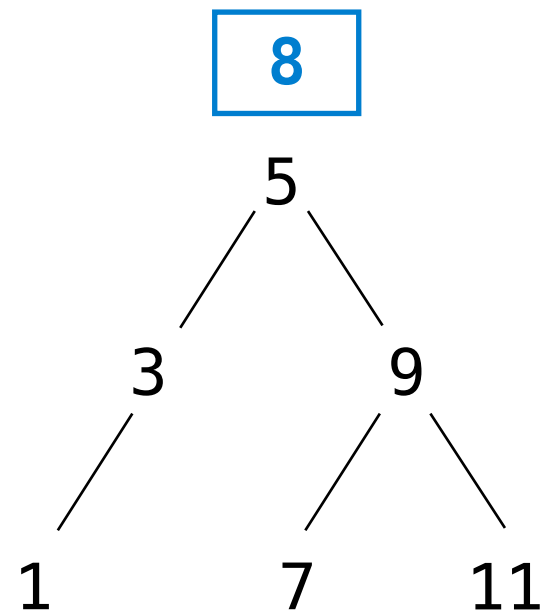


*Right!*

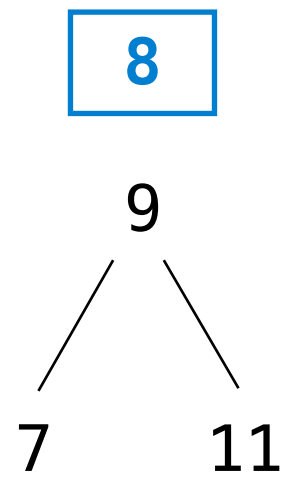


# From Last Time: Adjoining to a Tree Set

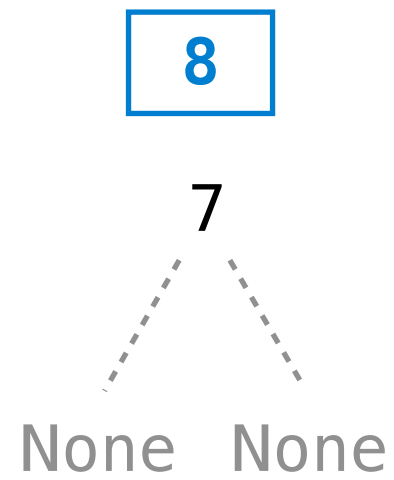
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*Right!*



*Left!*



*Right!*

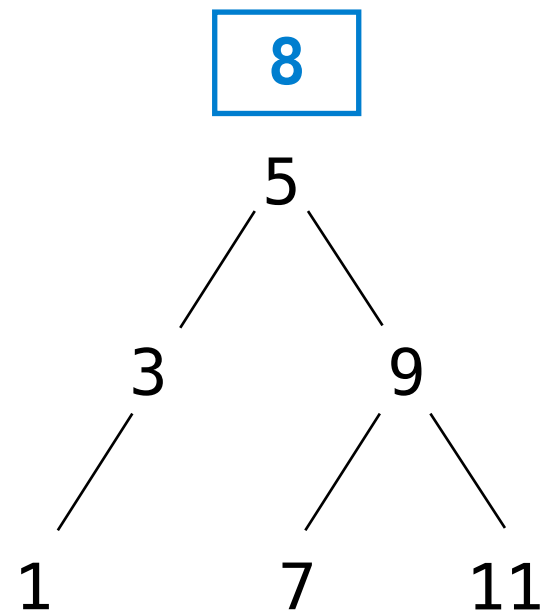


None

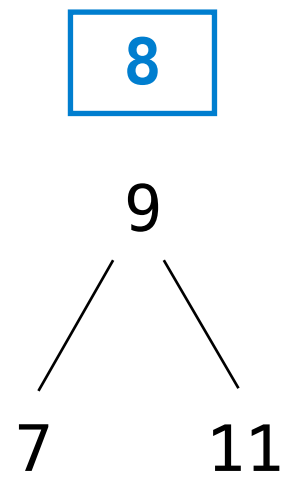


# From Last Time: Adjoining to a Tree Set

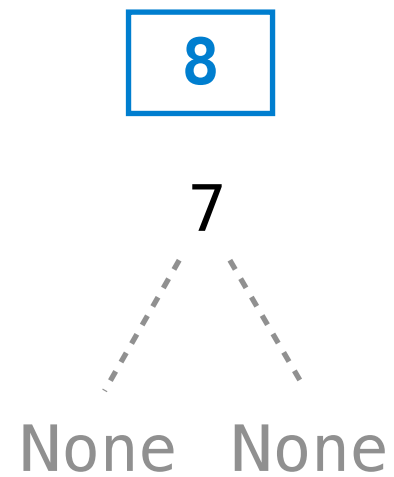
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*Right!*



*Left!*



*Right!*

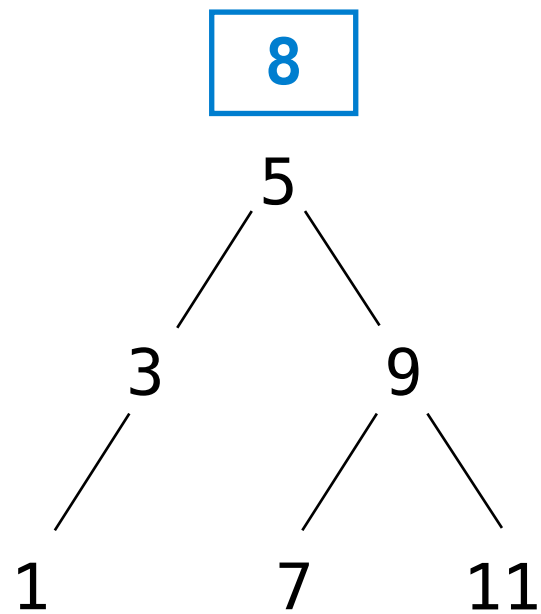


*Stop!*

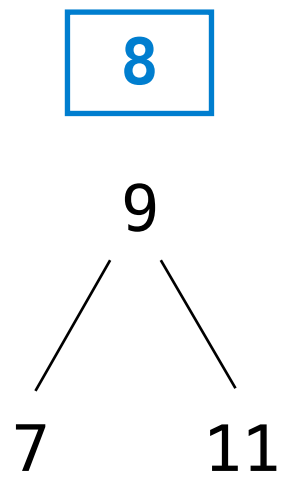


# From Last Time: Adjoining to a Tree Set

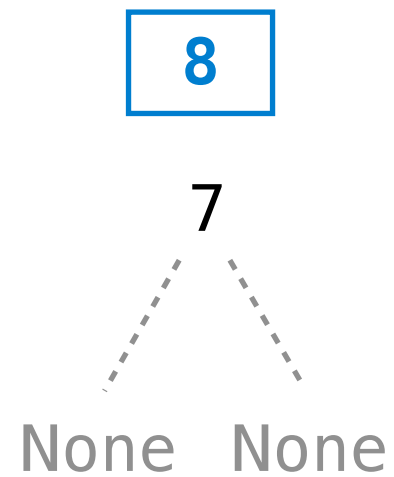
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*Right!*



*Left!*



*Right!*

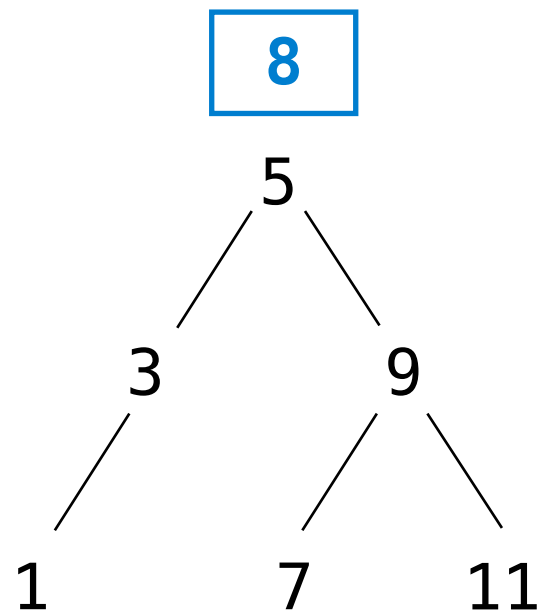


*Stop!*

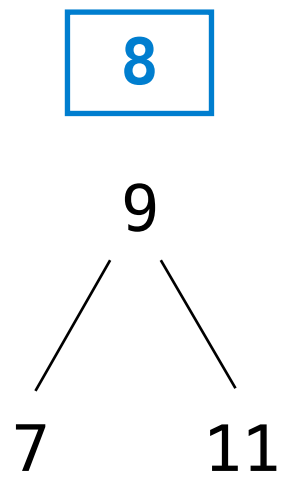


# From Last Time: Adjoining to a Tree Set

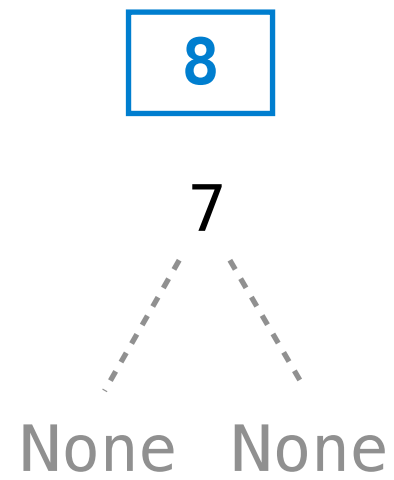
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*Right!*



*Left!*



*Right!*



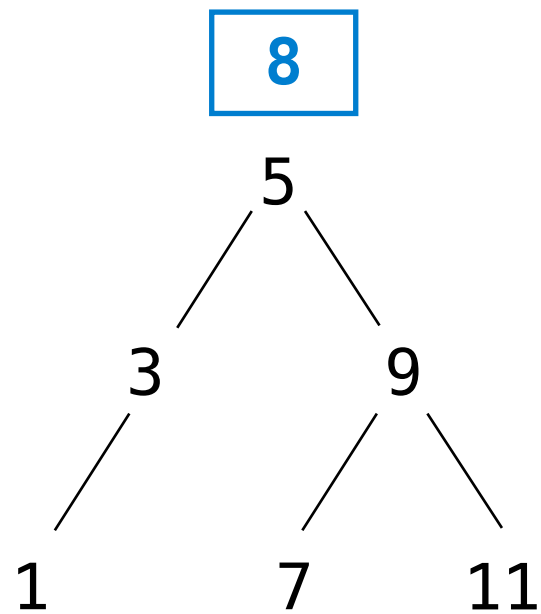
*Stop!*



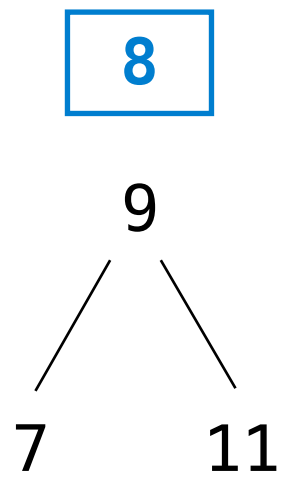
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# From Last Time: Adjoining to a Tree Set

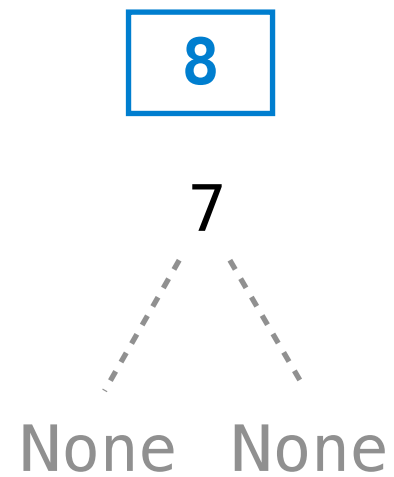
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*Right!*



*Left!*



*Right!*



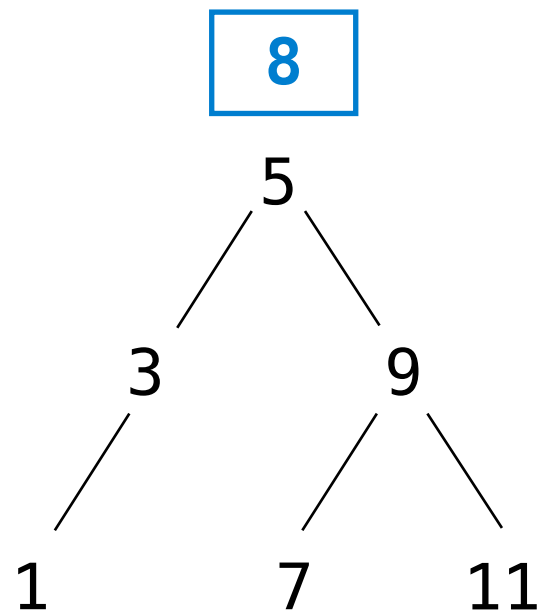
*Stop!*



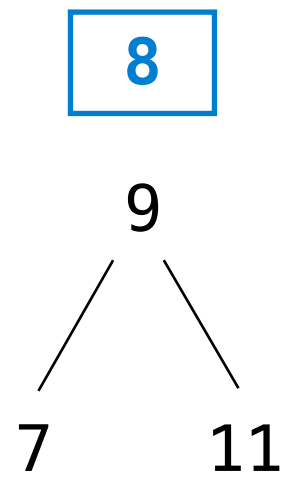


# From Last Time: Adjoining to a Tree Set

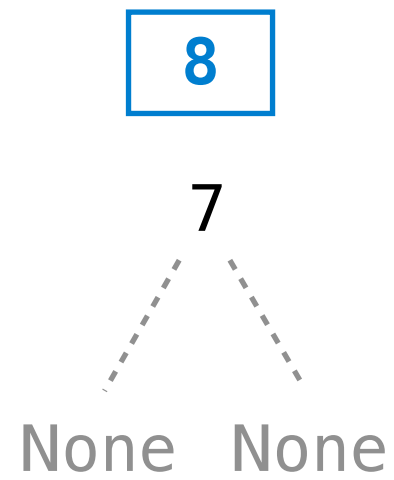
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*Right!*



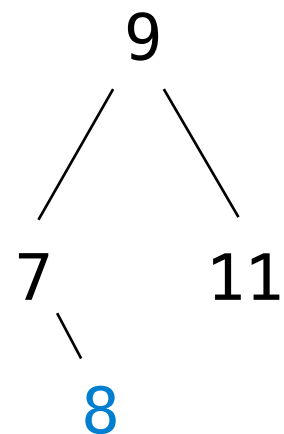
*Left!*



*Right!*



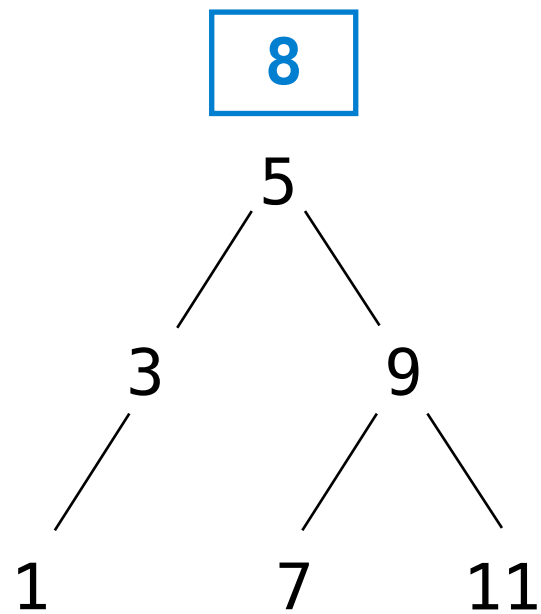
*Stop!*



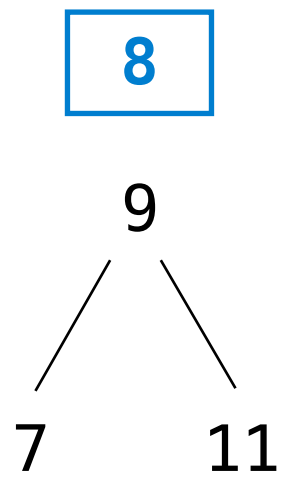
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# From Last Time: Adjoining to a Tree Set

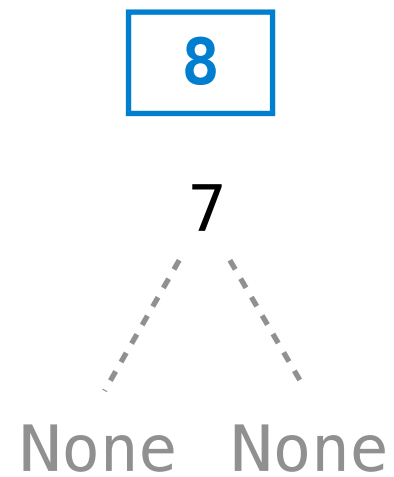
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*Right!*



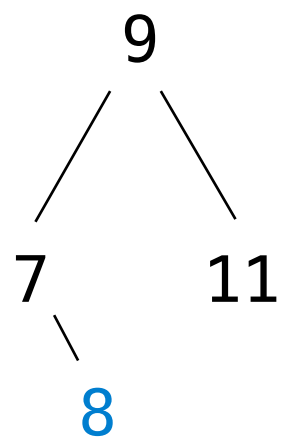
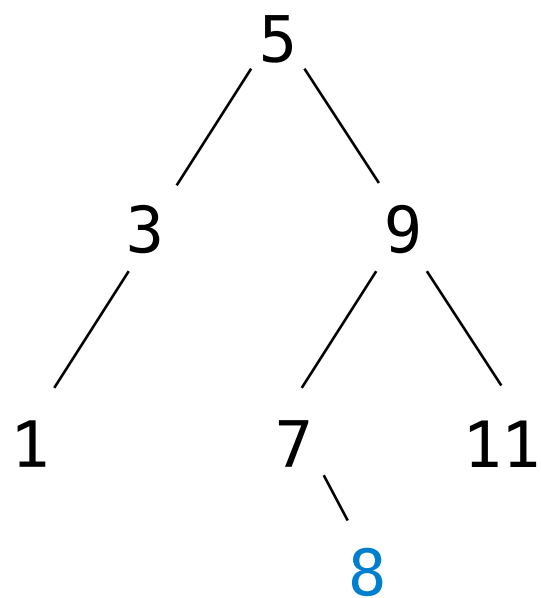
*Left!*



*Right!*



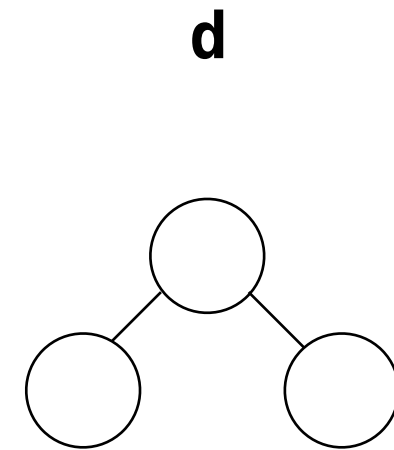
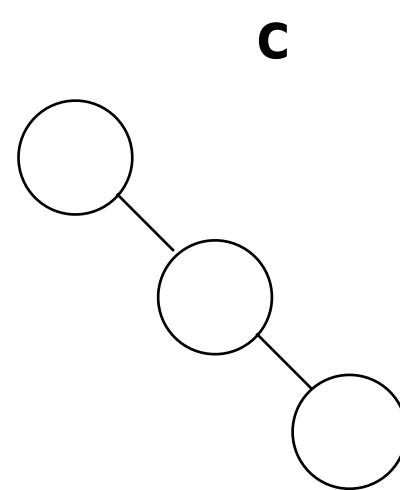
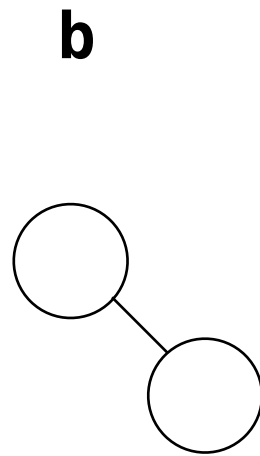
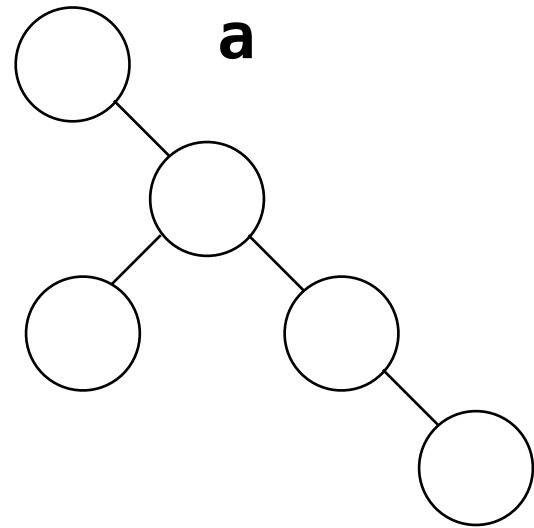
*Stop!*



8

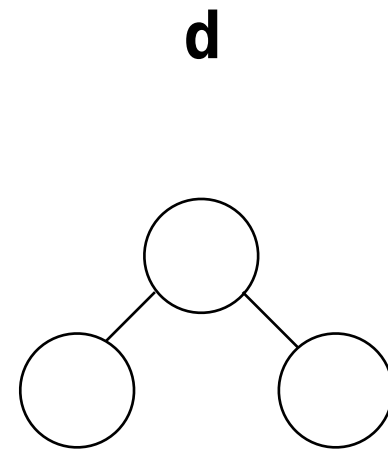
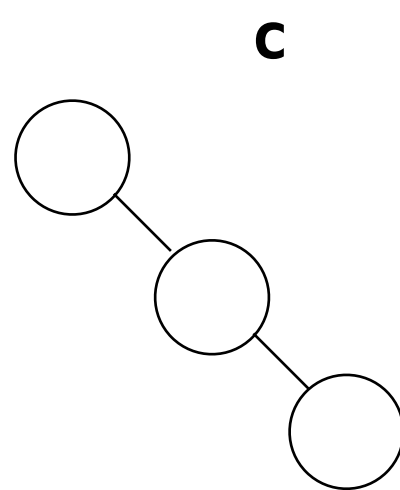
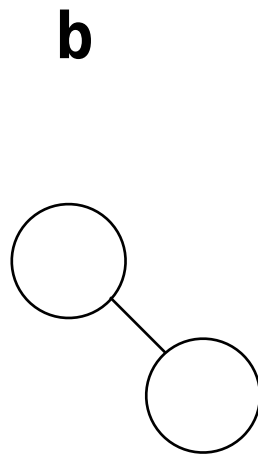
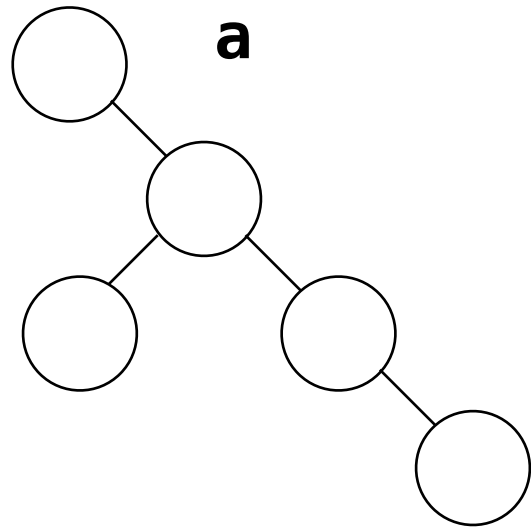
# From the Exam: Pruned Trees

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# From the Exam: Pruned Trees

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(a, b)

(a, c)

(a, d)

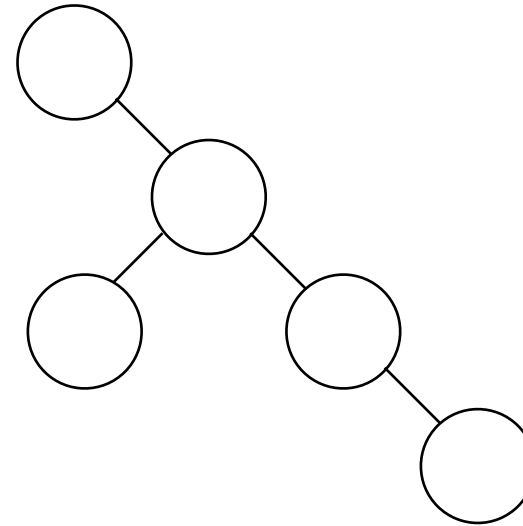
pruned

True	True	False
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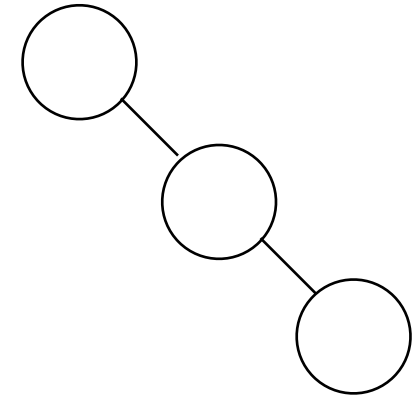
# From the Exam: Pruned Trees

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**a**



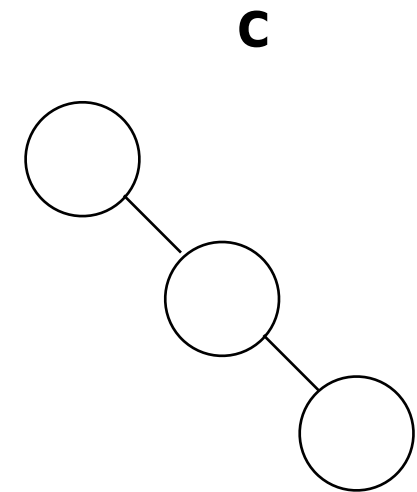
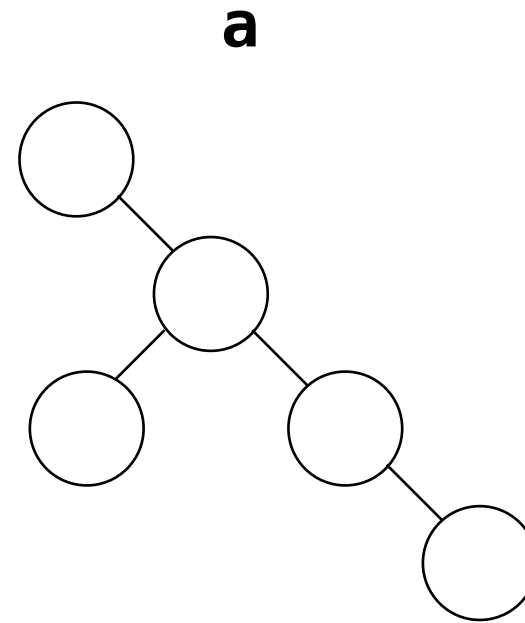
**c**



# From the Exam: Pruned Trees

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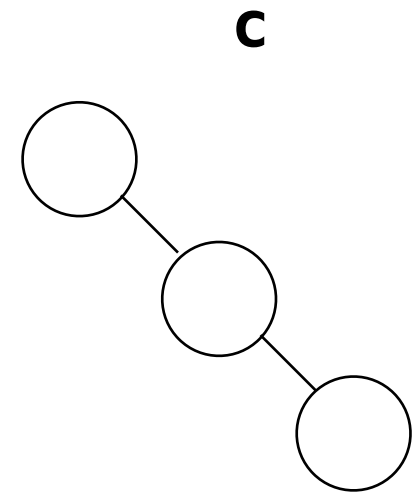
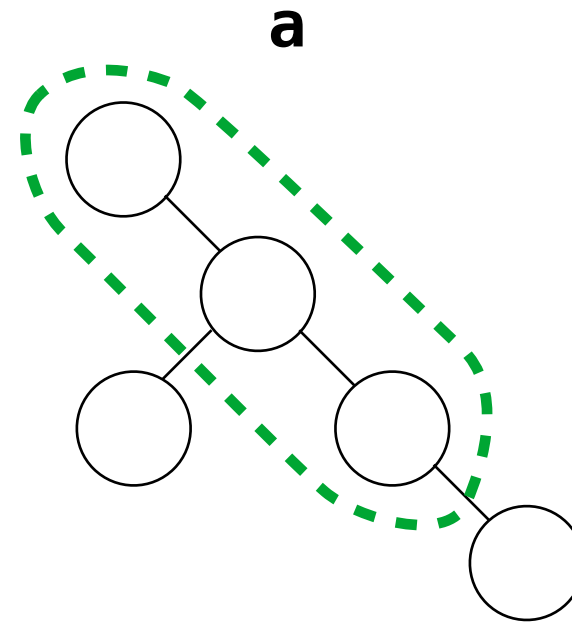
pruned(a, c)



# From the Exam: Pruned Trees

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pruned(a, c)

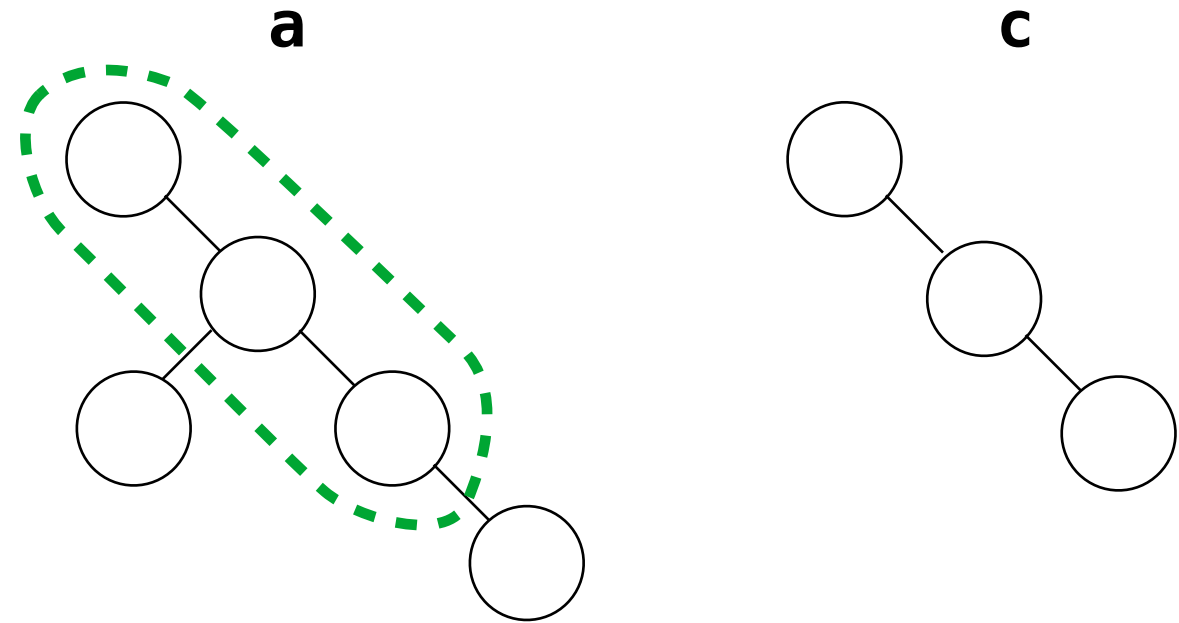


# From the Exam: Pruned Trees

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$\text{pruned}(a, c)$

*implies*





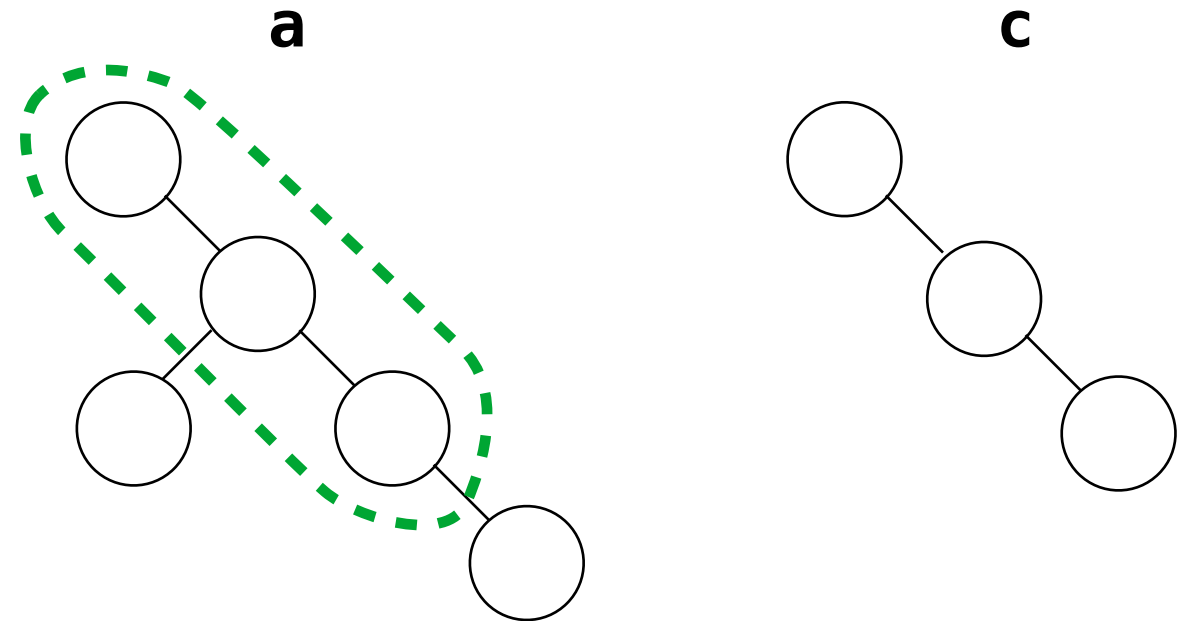
# From the Exam: Pruned Trees

---

`pruned(a, c)`

*implies*

`pruned(a.right, c.right)`



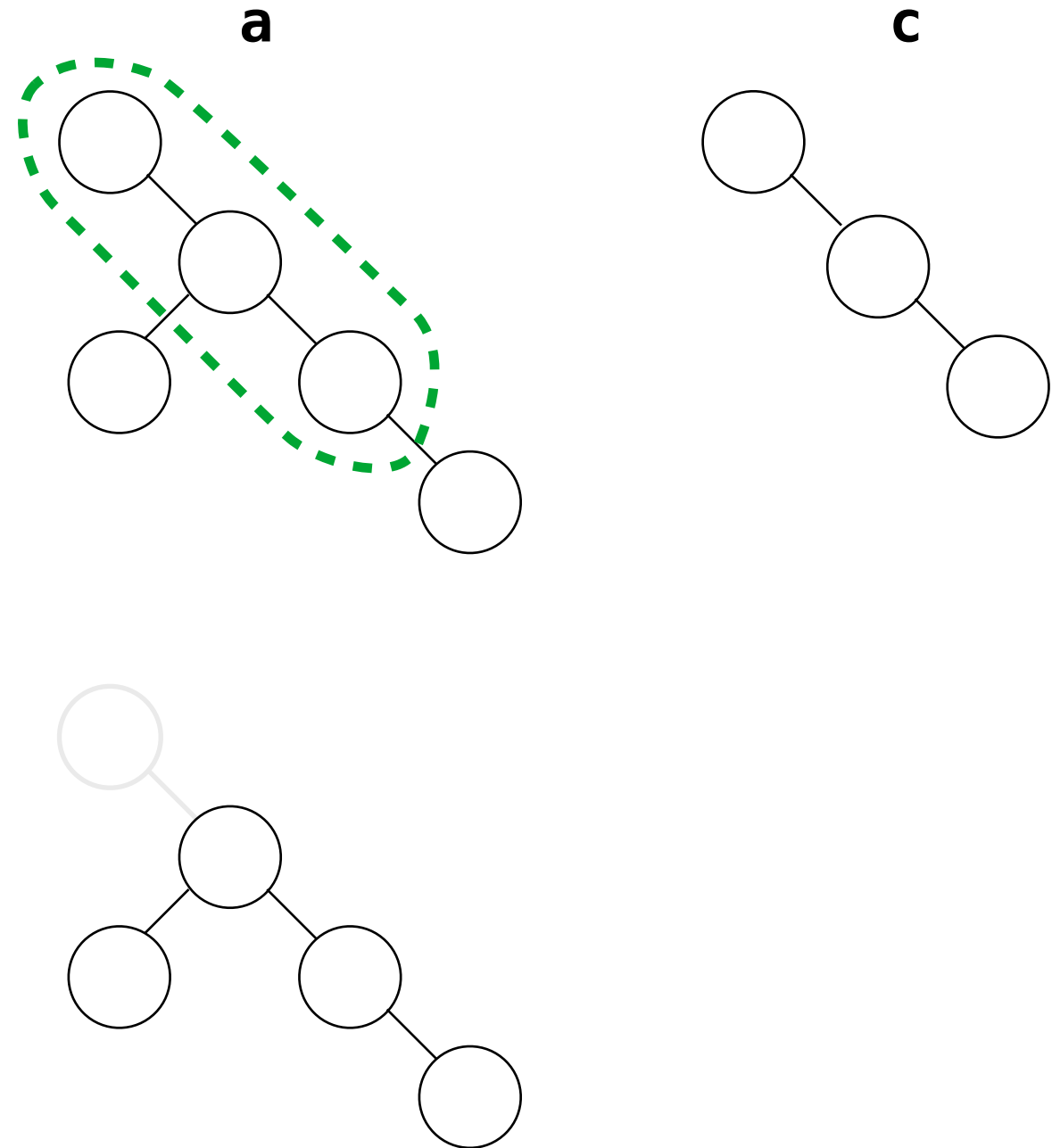
# From the Exam: Pruned Trees

---

`pruned(a, c)`

*implies*

`pruned(a.right, c.right)`



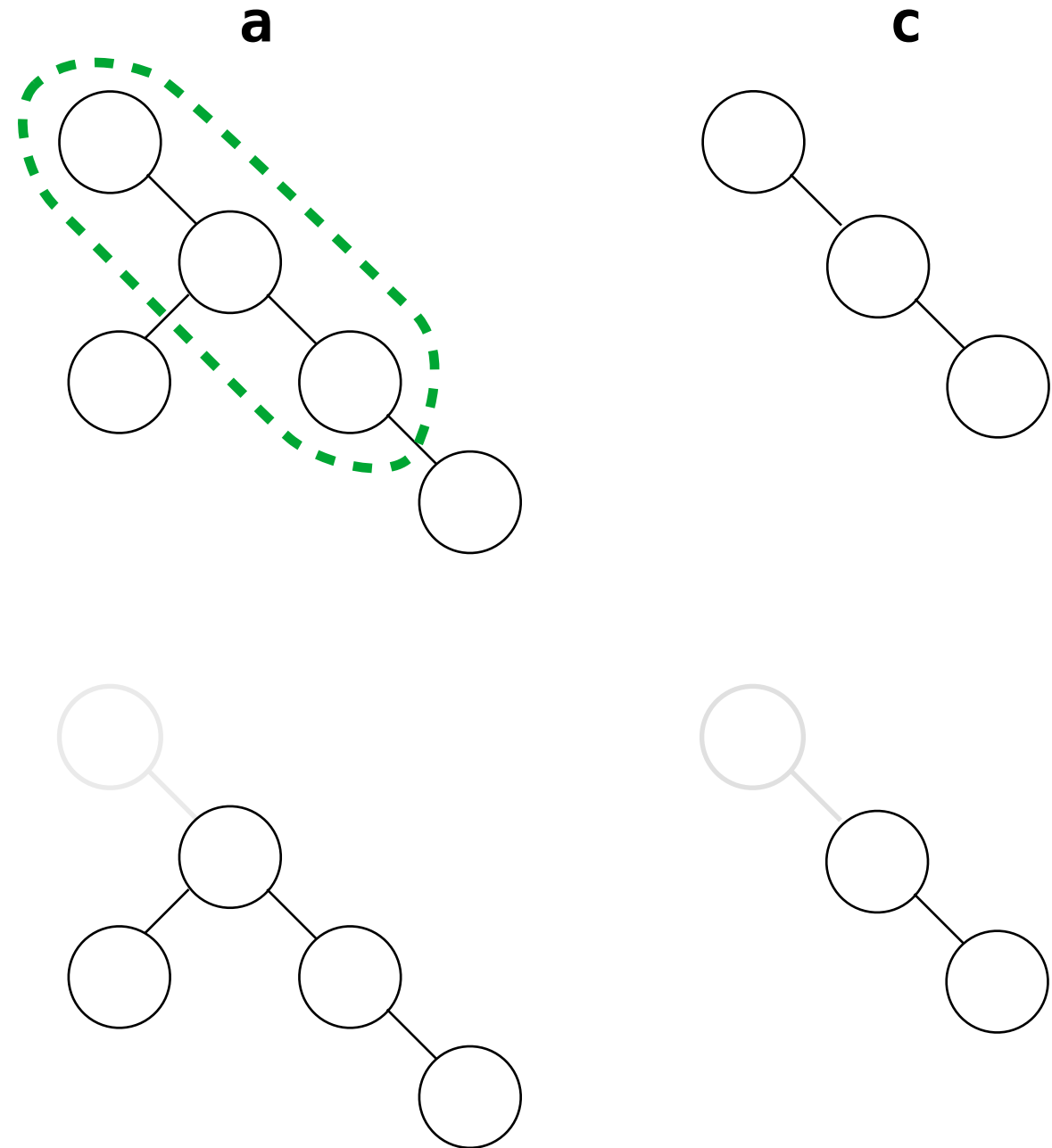
# From the Exam: Pruned Trees

---

`pruned(a, c)`

*implies*

`pruned(a.right, c.right)`



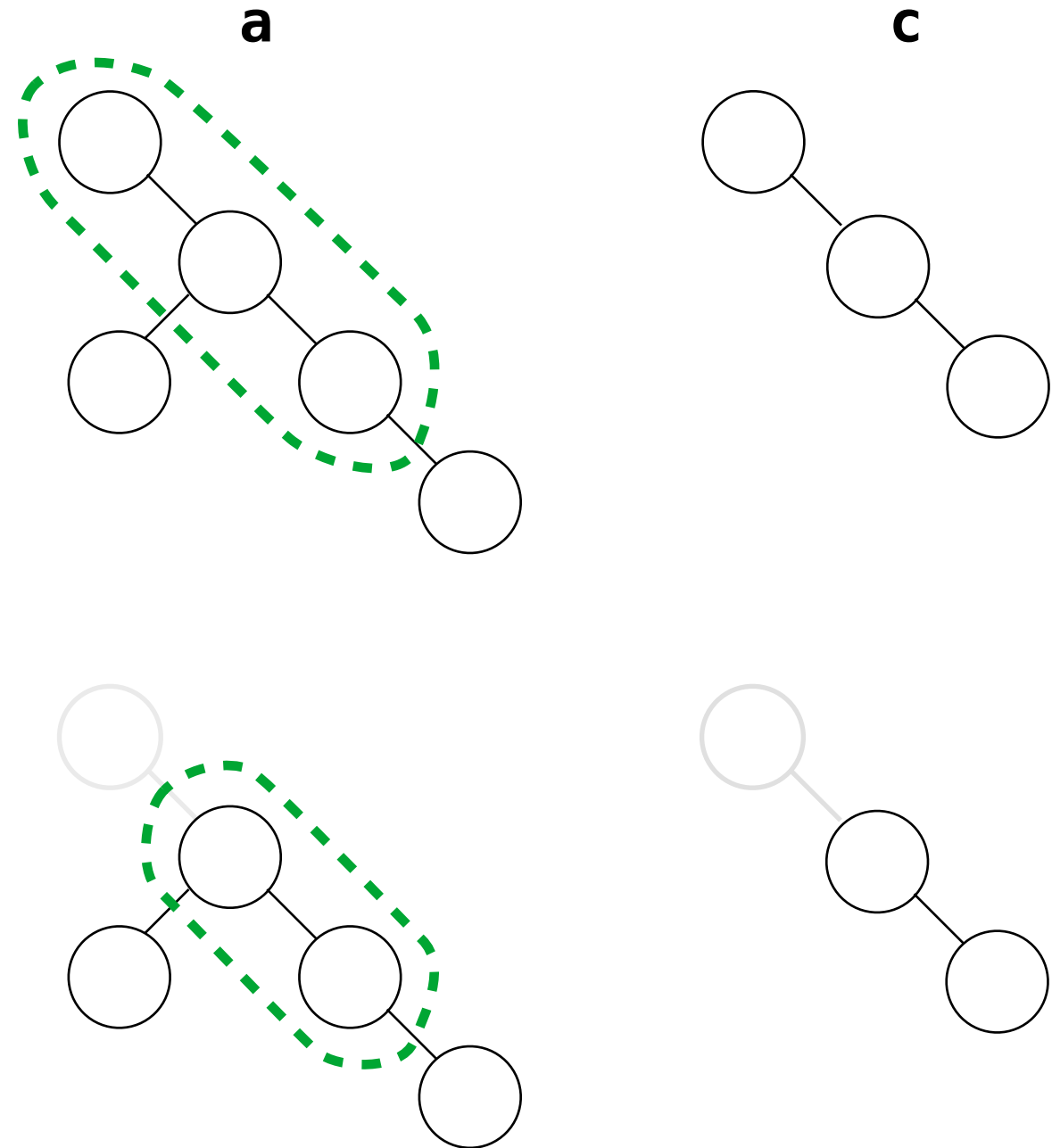
# From the Exam: Pruned Trees

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`pruned(a, c)`

*implies*

`pruned(a.right, c.right)`



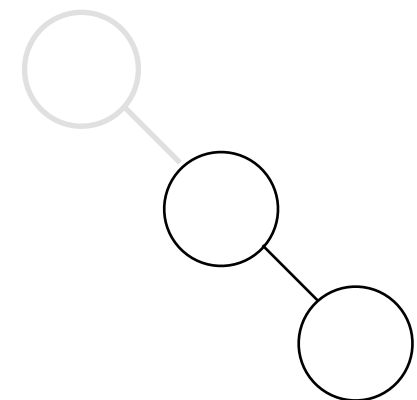
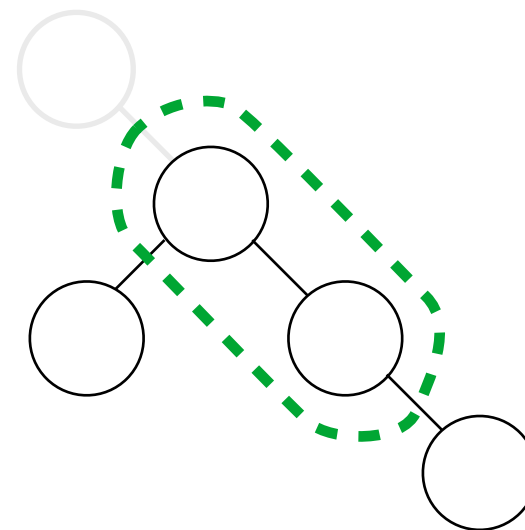
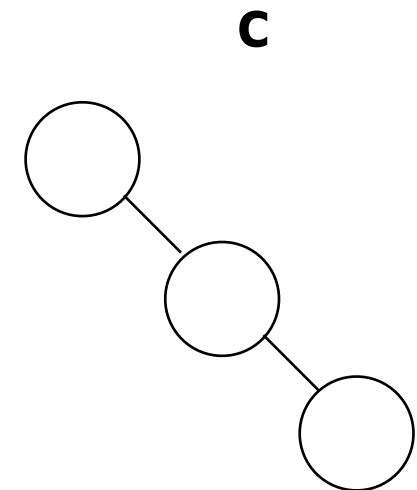
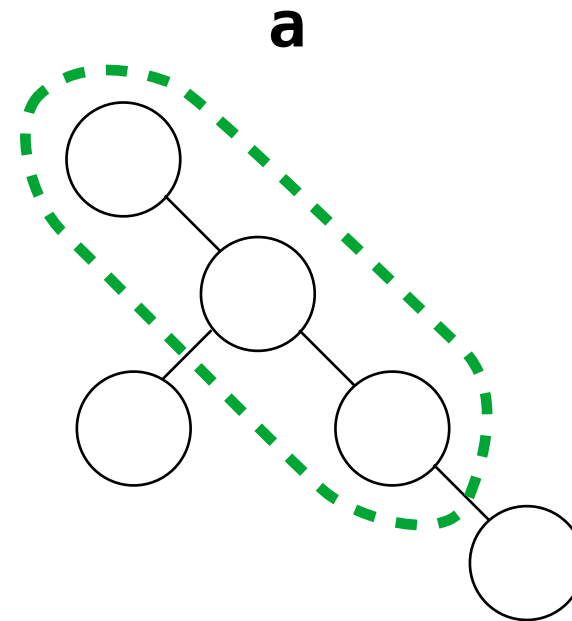
# From the Exam: Pruned Trees

---

`pruned(a, c)`

*implies*

`pruned(a.right, c.right)`



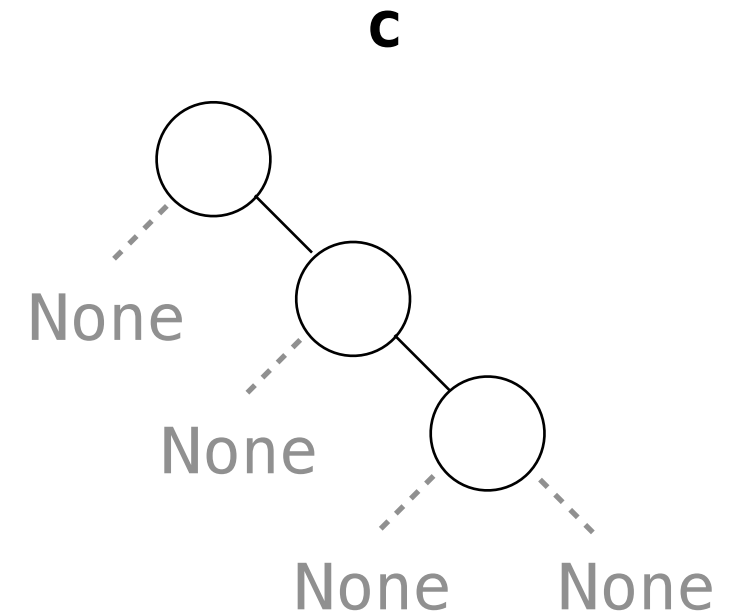
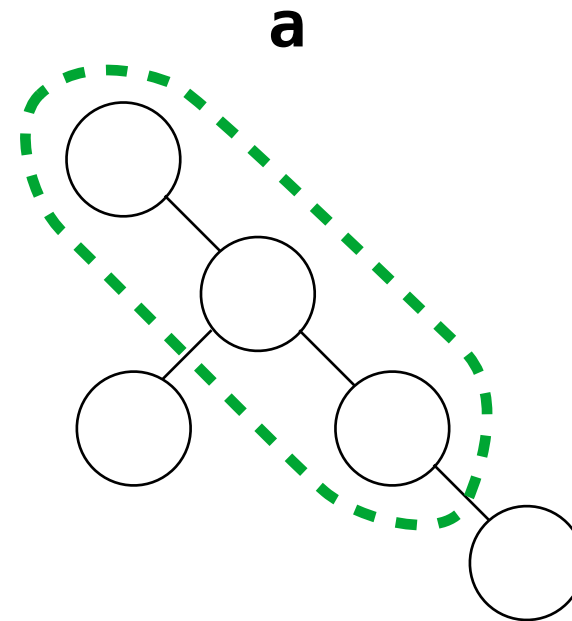
what about `c.left`?

# From the Exam: Pruned Trees

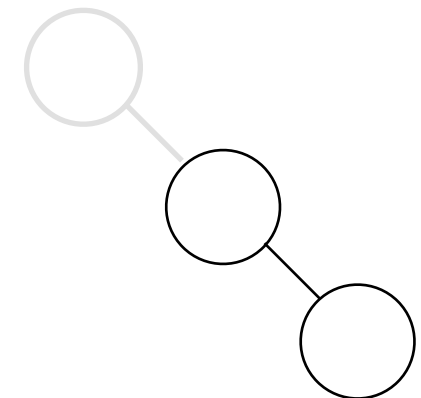
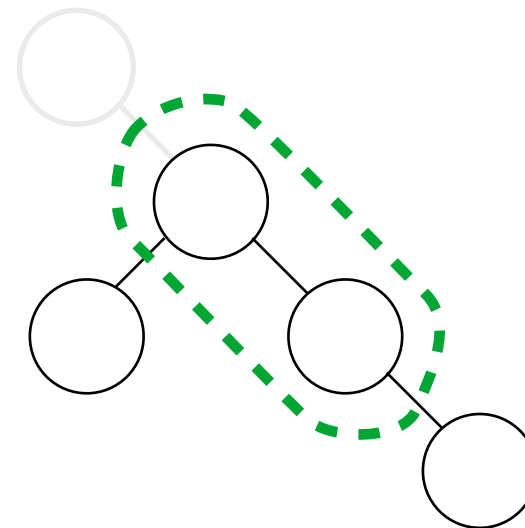
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`pruned(a, c)`

*implies*



`pruned(a.right, c.right)`



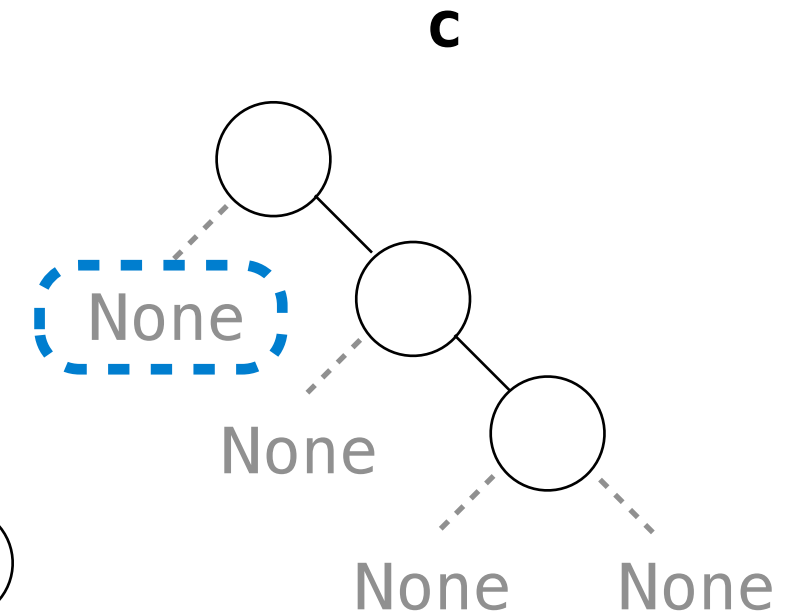
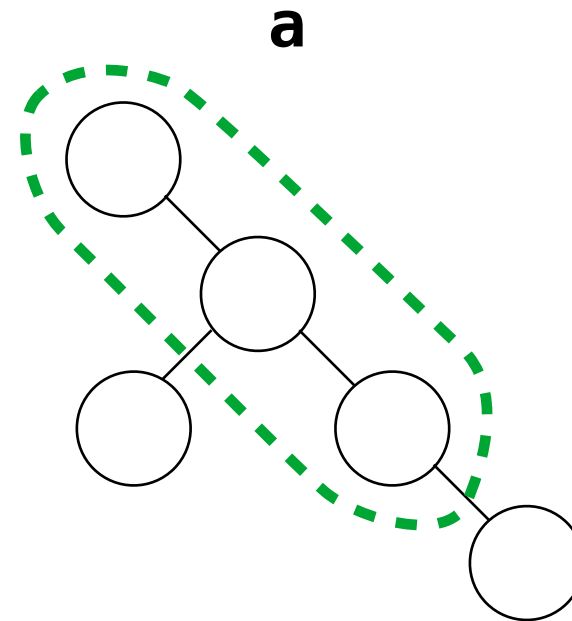
what about `c.left`?

# From the Exam: Pruned Trees

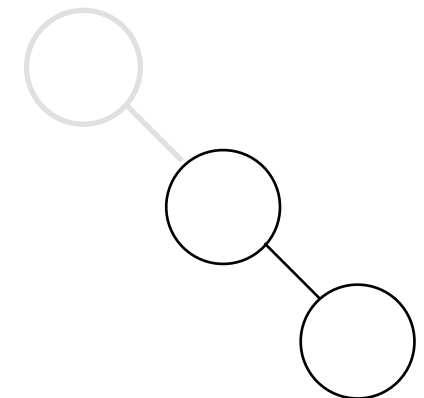
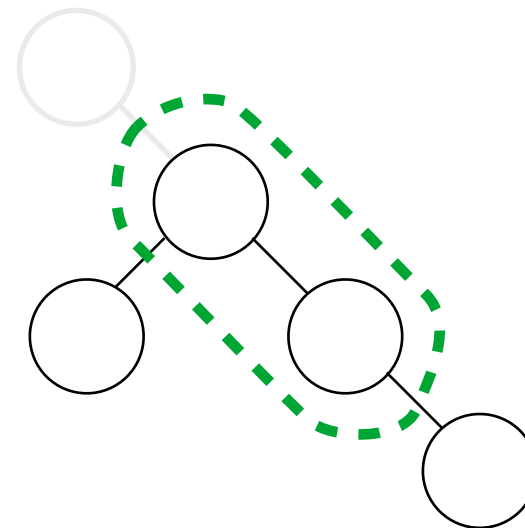
---

`pruned(a, c)`

*implies*



`pruned(a.right, c.right)`

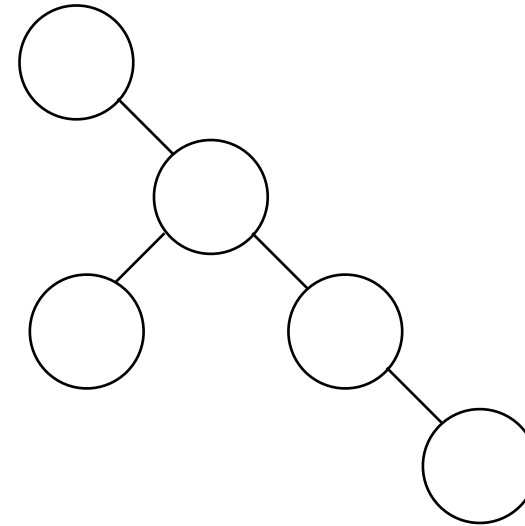


what about `c.left`?

# From the Exam: Pruned Trees

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**a**

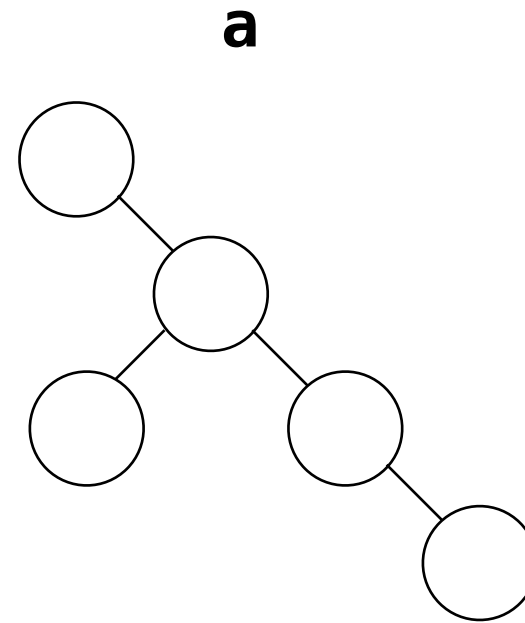




# From the Exam: Pruned Trees

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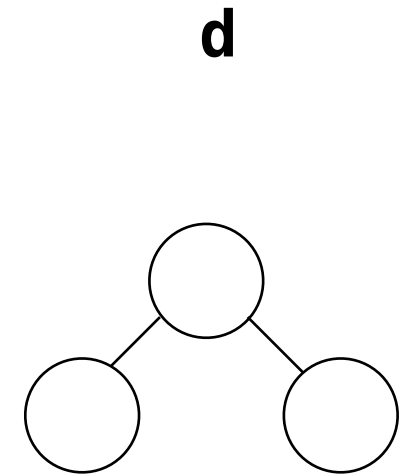
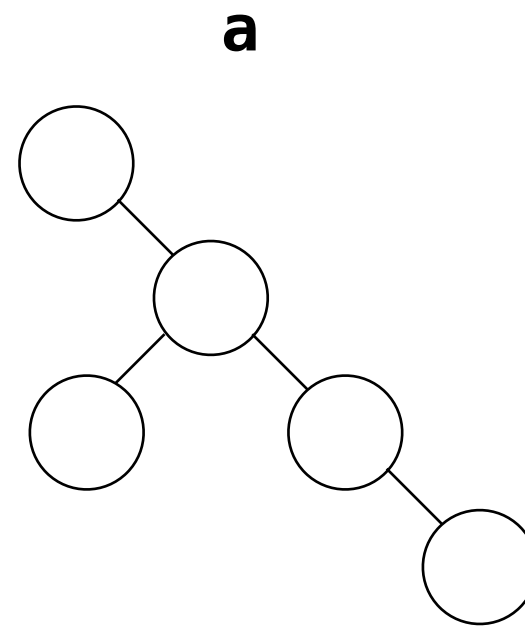
pruned(a, d)



# From the Exam: Pruned Trees

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pruned(a, d)

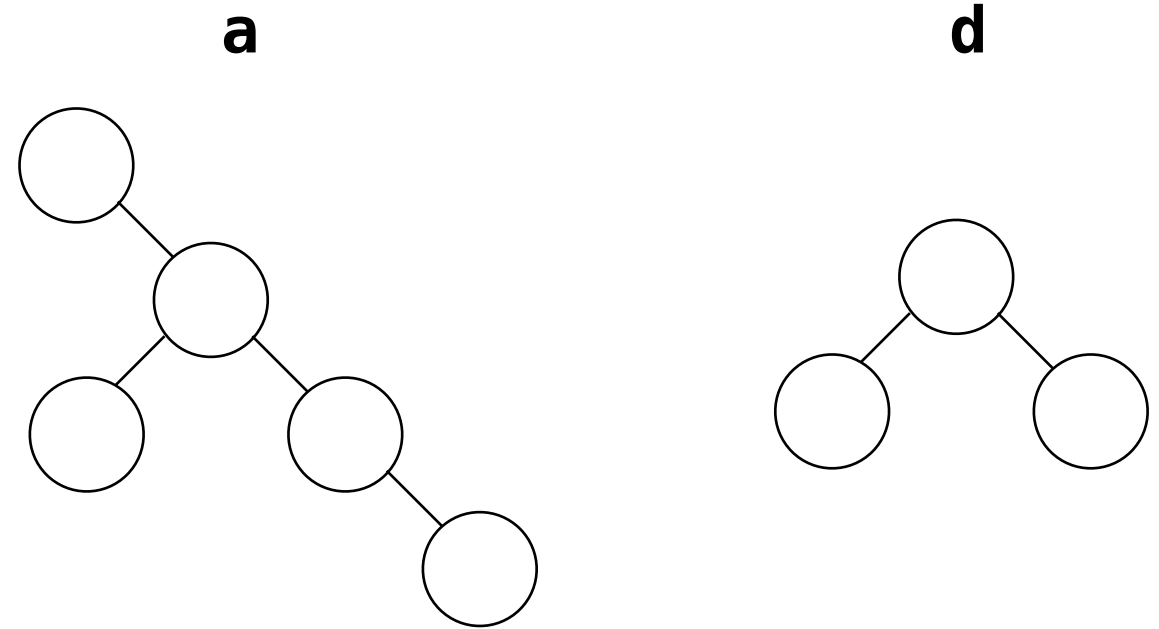


# From the Exam: Pruned Trees

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pruned(a, d)

*would imply*



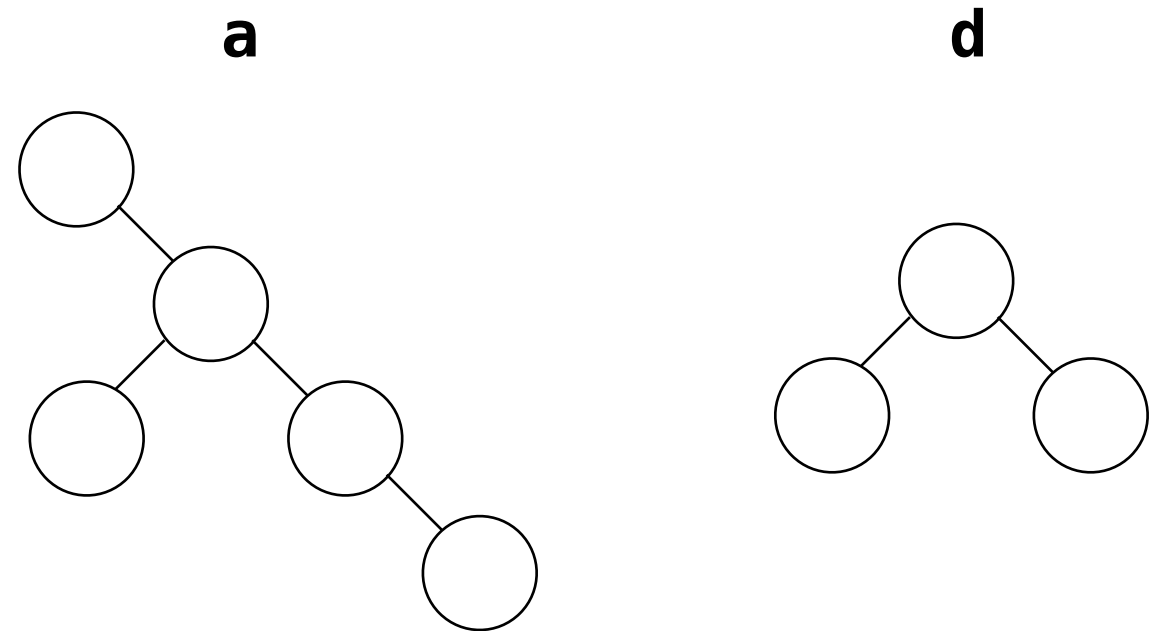
# From the Exam: Pruned Trees

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`pruned(a, d)`

*would imply*

`pruned(a.left, d.left)`



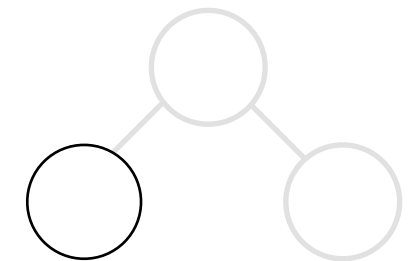
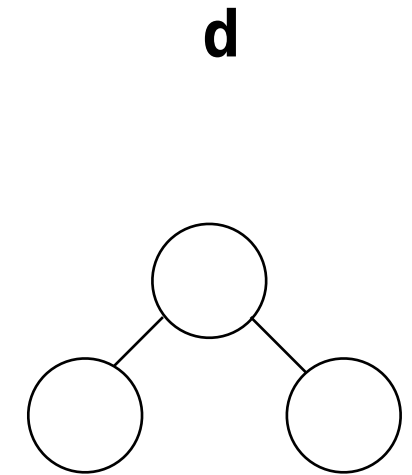
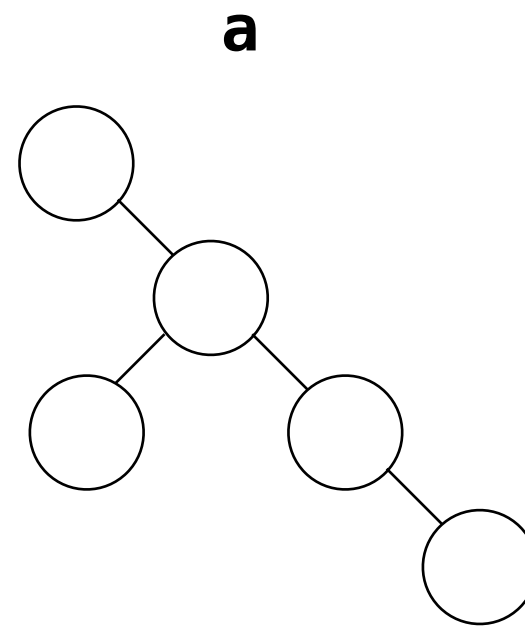
# From the Exam: Pruned Trees

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`pruned(a, d)`

*would imply*

`pruned(a.left, d.left)`



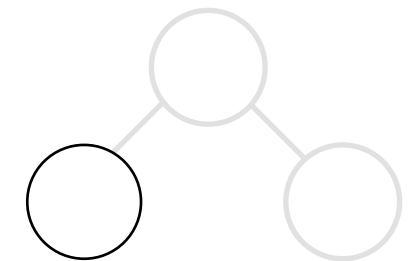
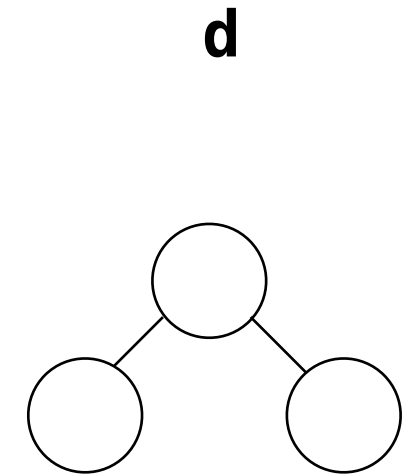
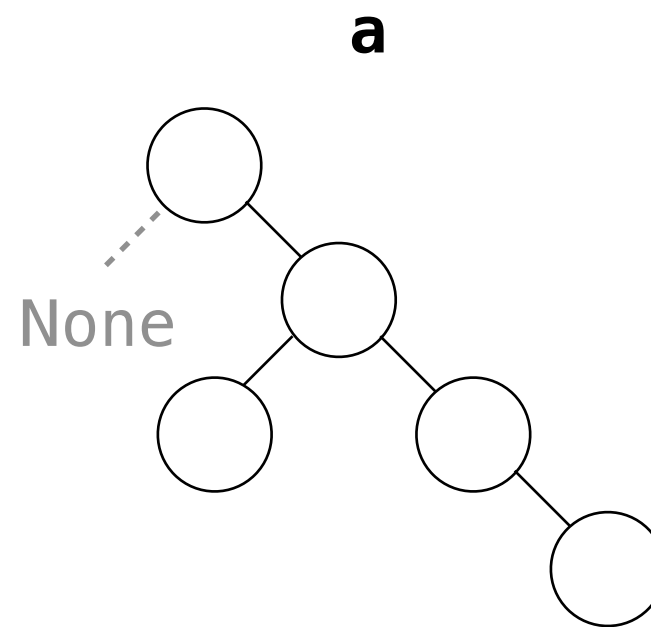
# From the Exam: Pruned Trees

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`pruned(a, d)`

*would imply*

`pruned(a.left, d.left)`



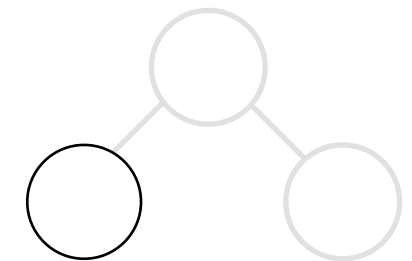
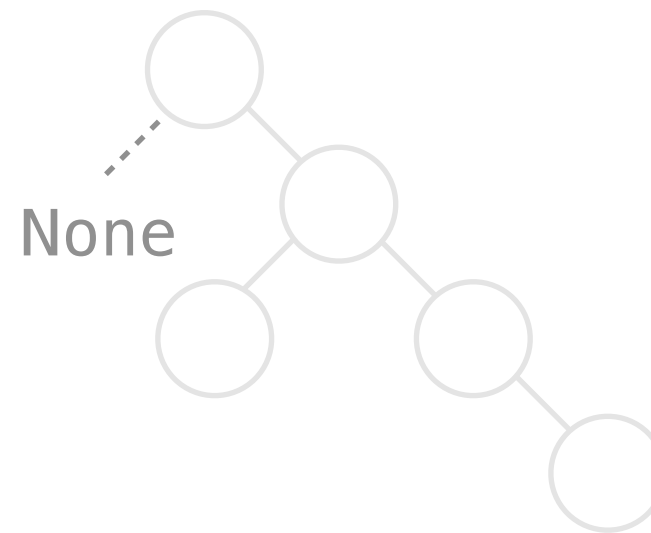
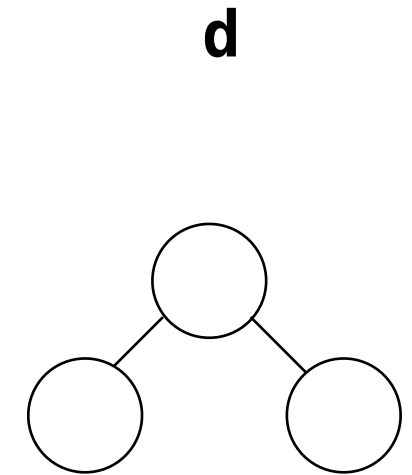
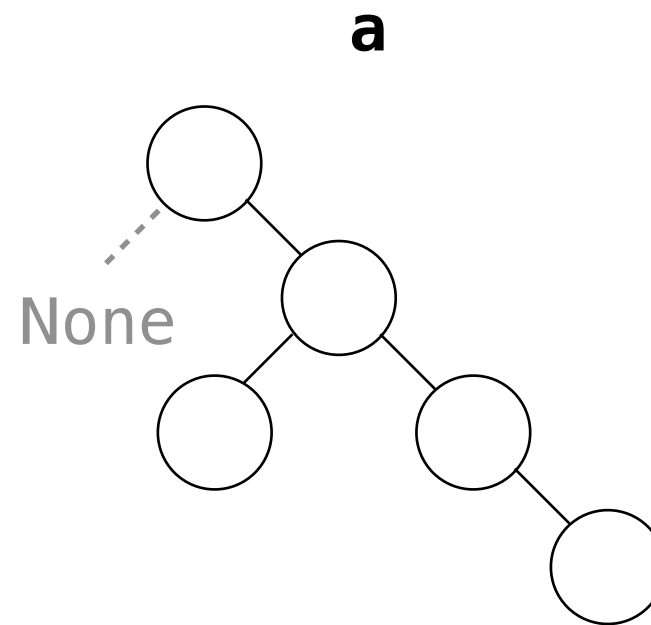
# From the Exam: Pruned Trees

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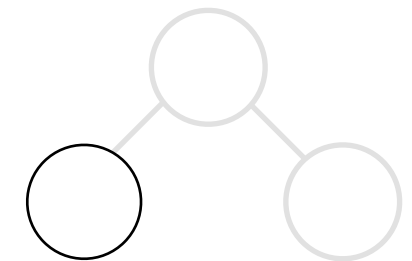
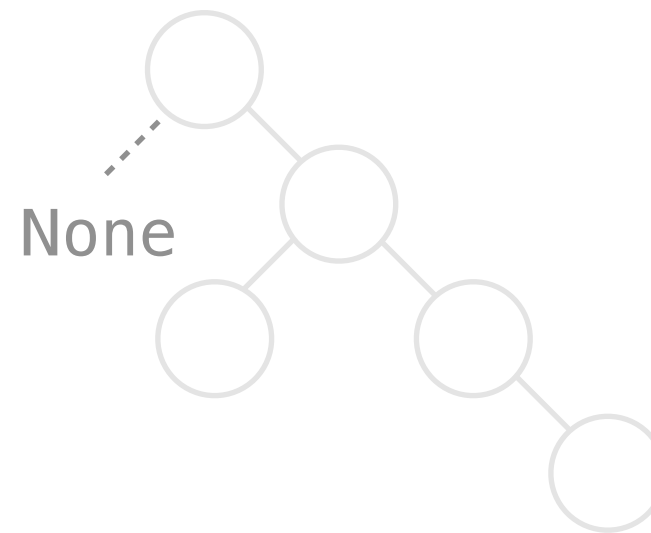
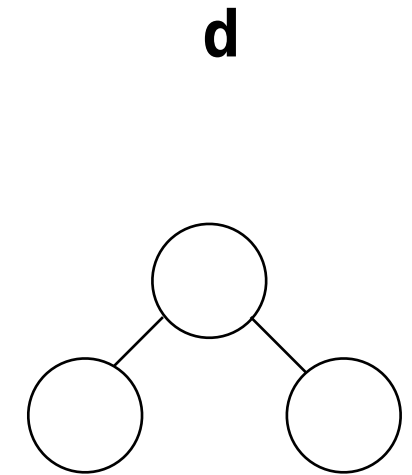
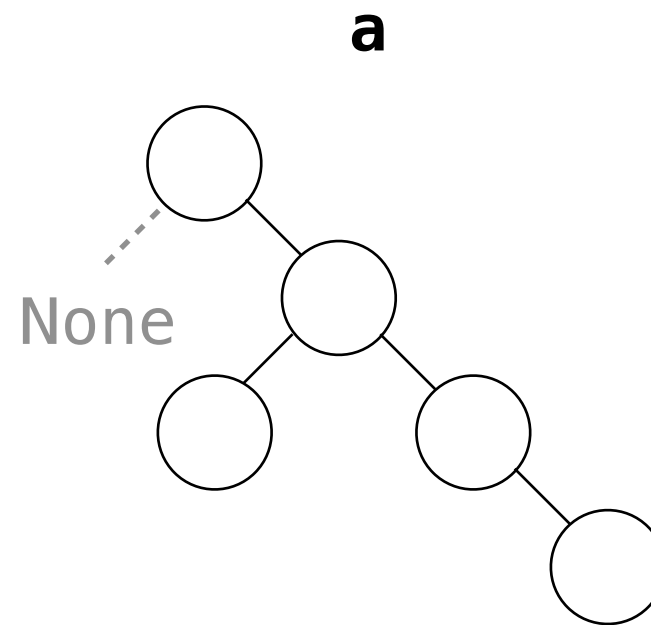
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**None**



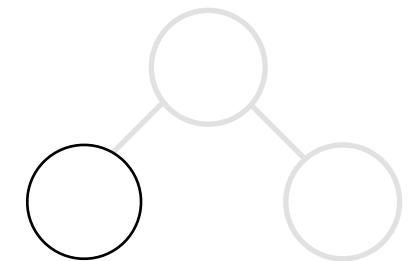
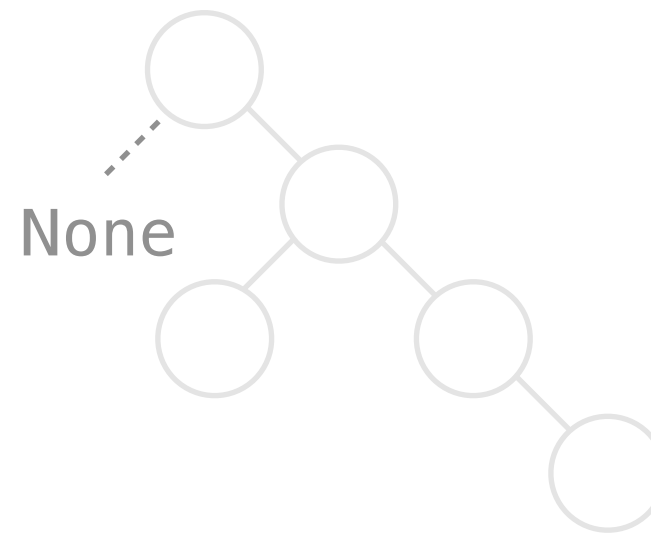
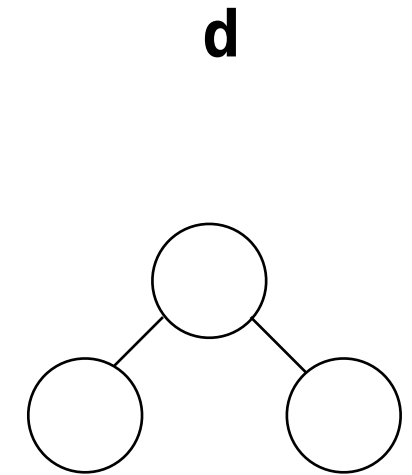
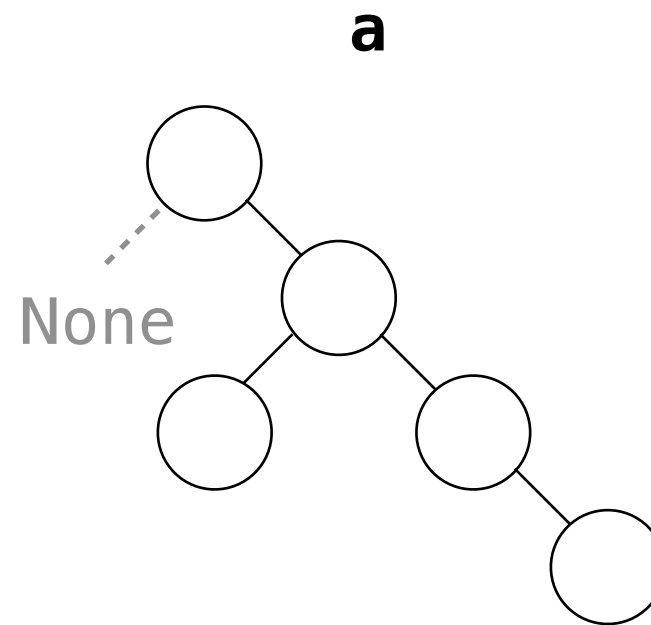
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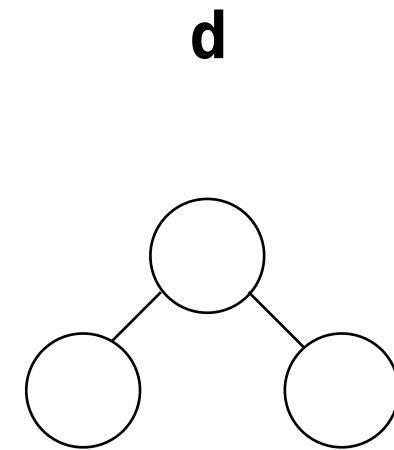
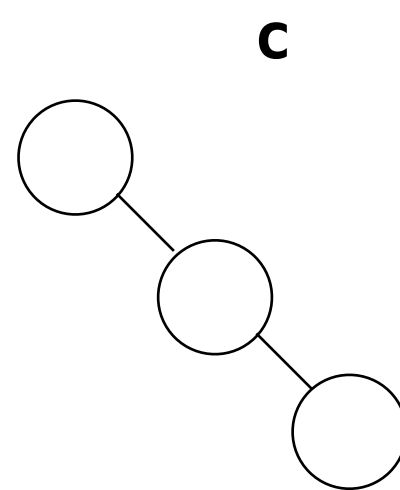
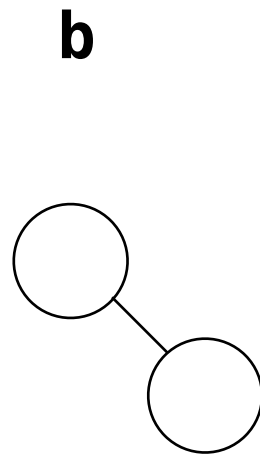
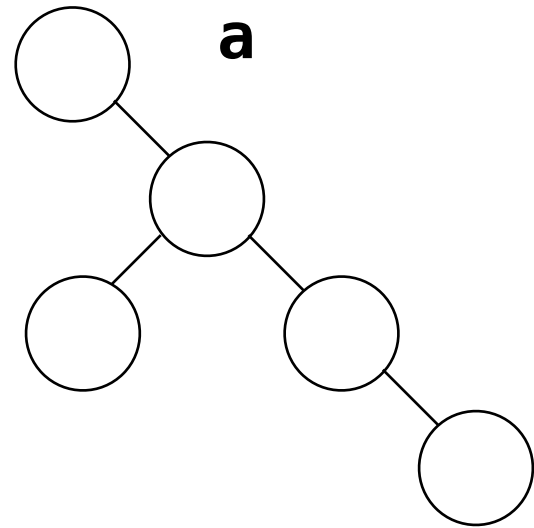


**None**

**Not None**

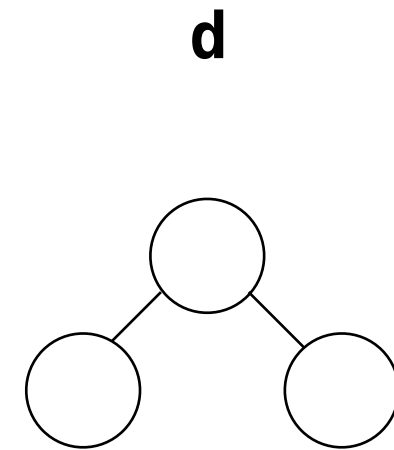
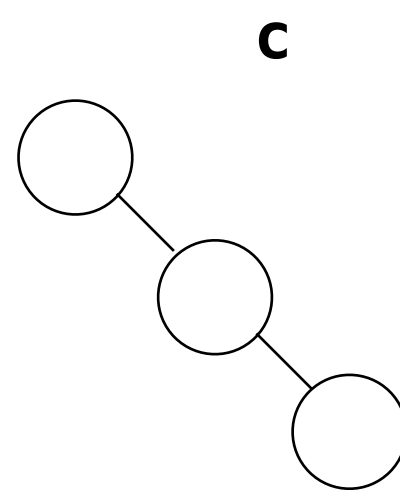
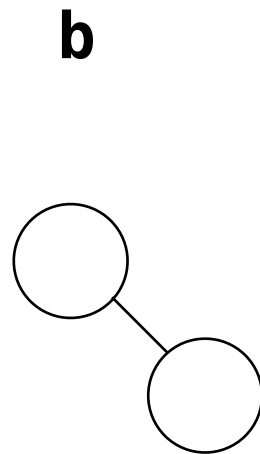
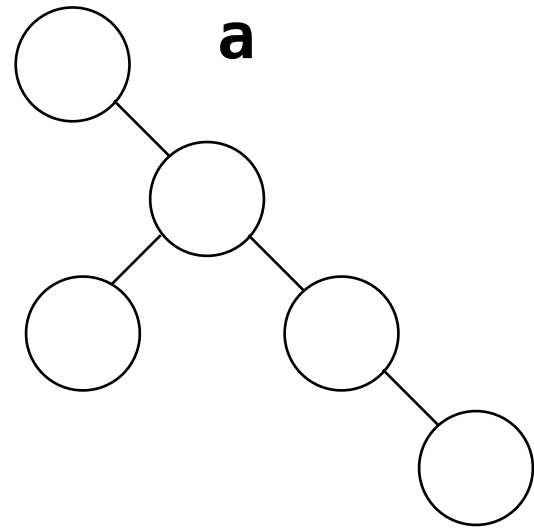
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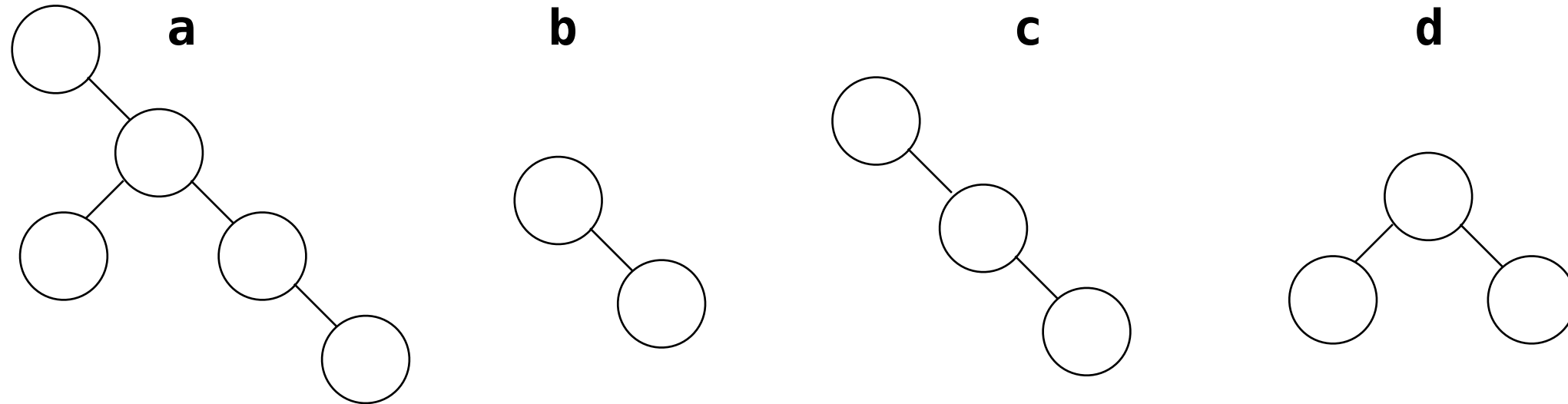
---



Recursive call: both branches are pruned as well

# From the Exam: Pruned Trees

---

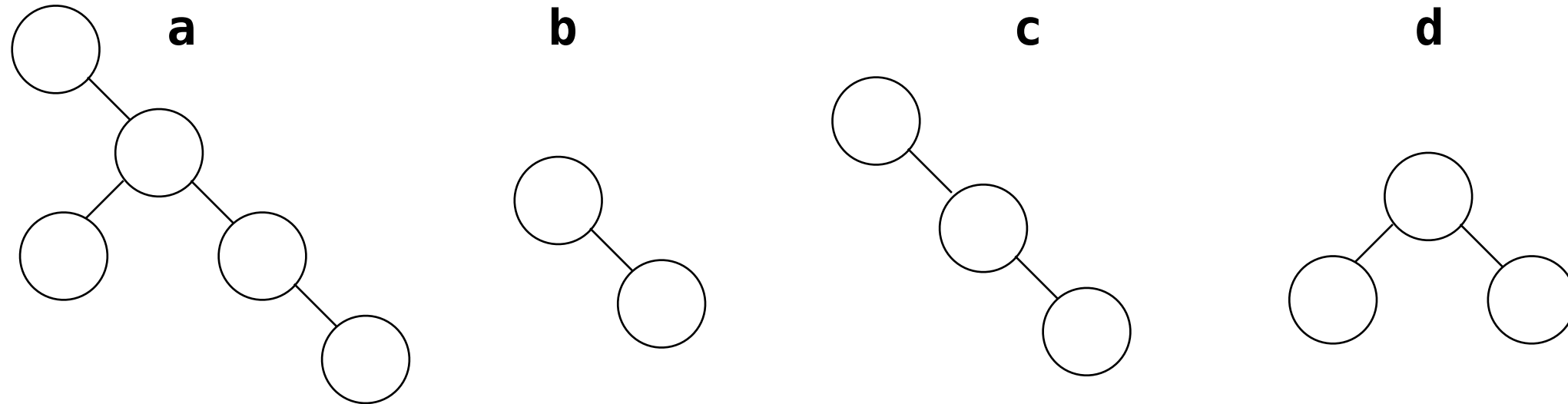


Recursive call: both branches are pruned as well

Base cases: one (or more) of the trees is None

## From the Exam: Pruned Trees

---



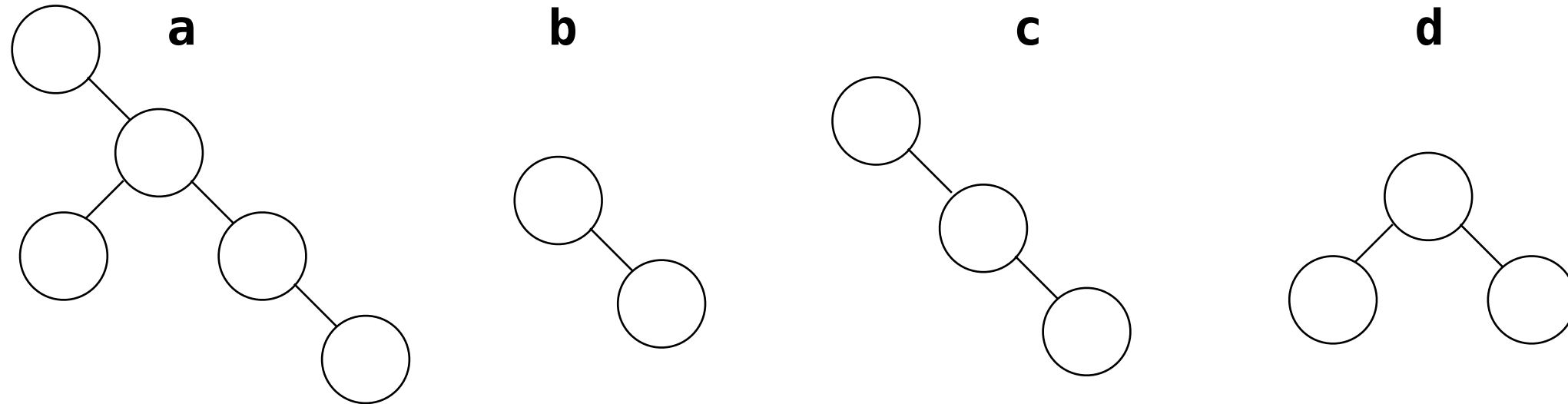
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# From the Exam: Pruned Trees

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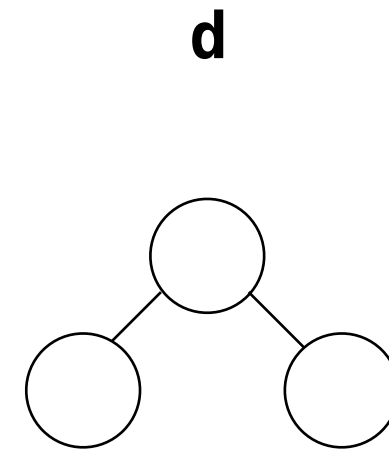
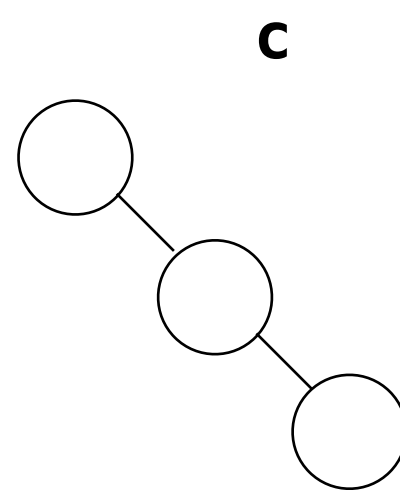
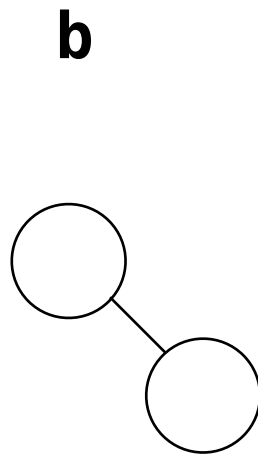
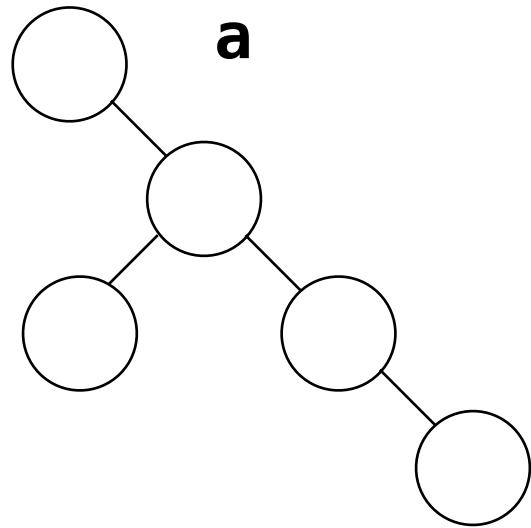
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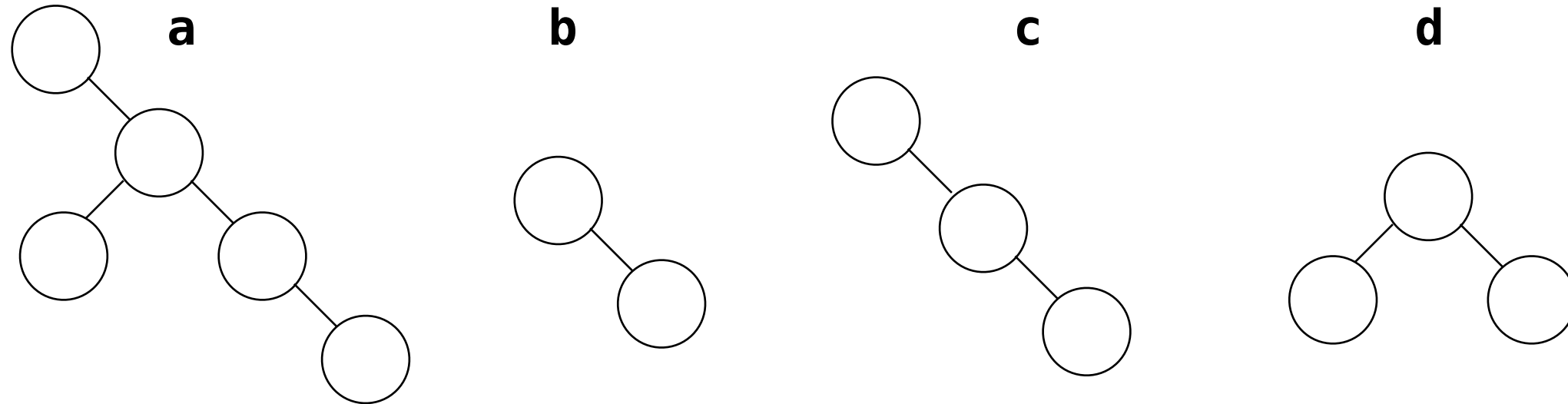
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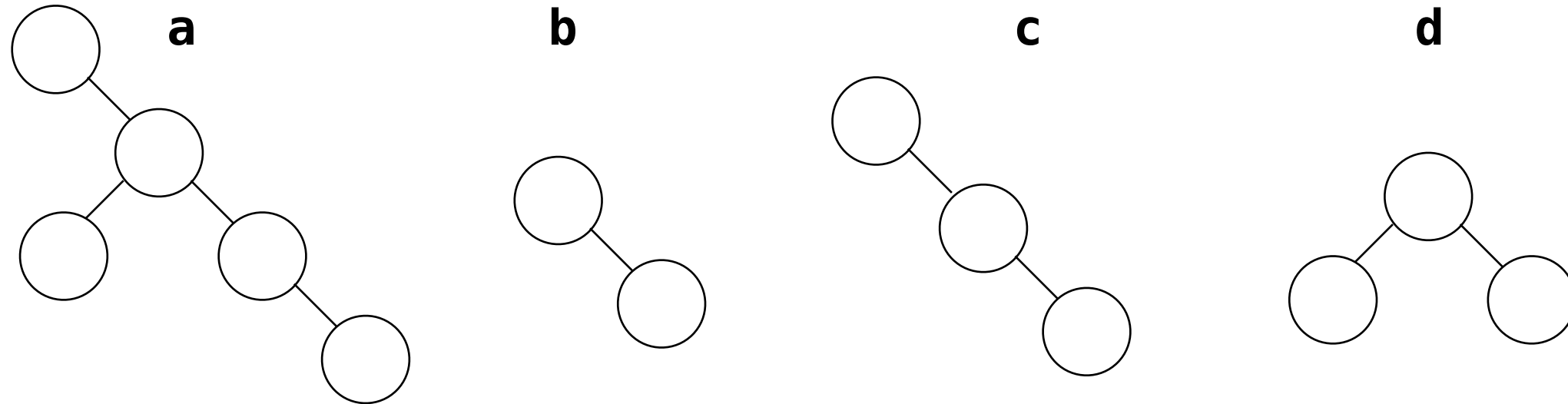
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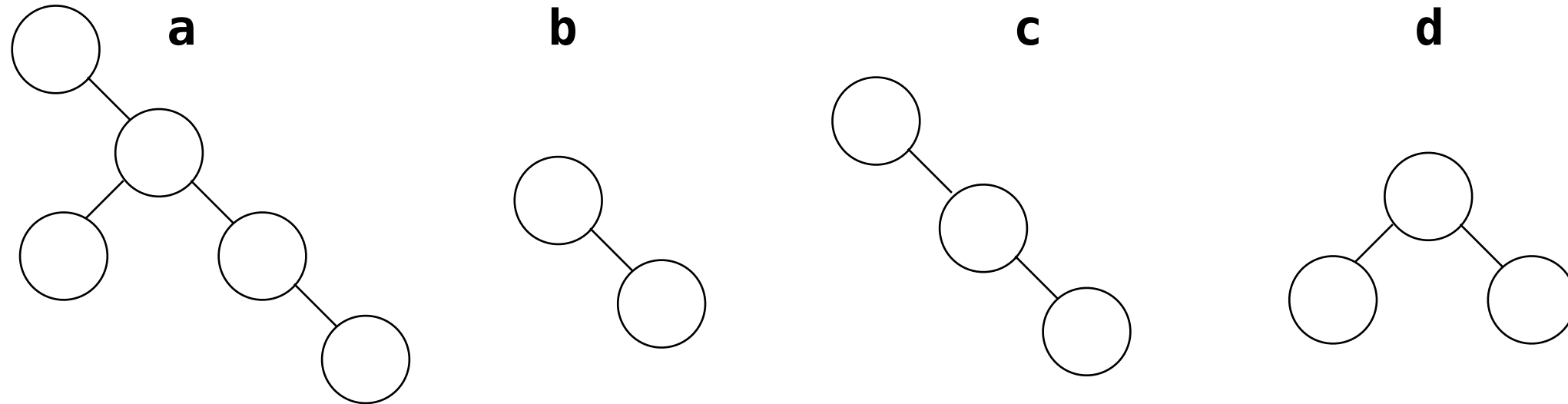
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## From the Exam: Pruned Trees

---



Recursive call: both branches are pruned as well

Base cases: one (or more) of the trees is None

```
def pruned(t1, t2):  
    if t2 is None:  
        return True  
    if t1 is None:  
        return False  
    return pruned(t1.left, t2.left) and pruned(t1.right, t2.right)
```

# Today's Topic: Handling Errors

---

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Sometimes, computers don't do exactly what we expect

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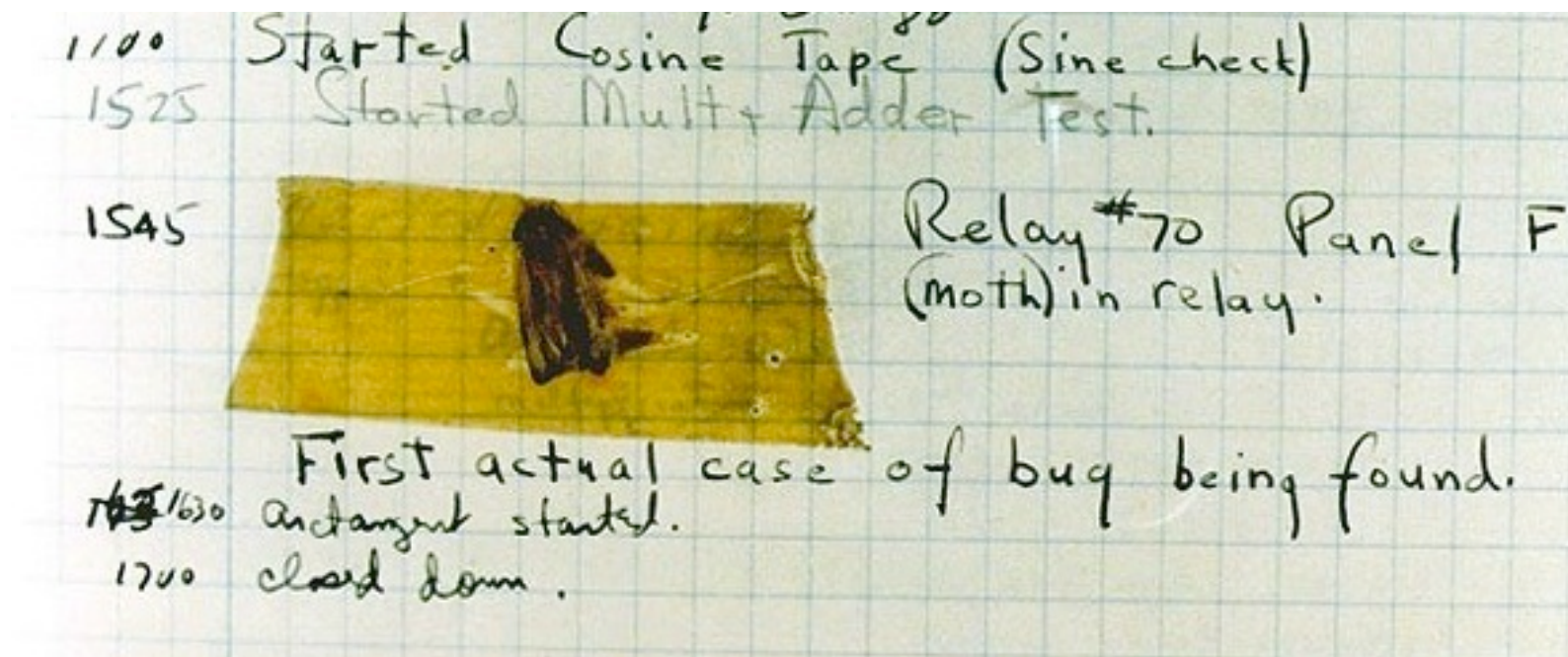
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# Today's Topic: Handling Errors

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Sometimes, computers don't do exactly what we expect

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Grace Hopper's Notebook, 1947, Moth found in a Mark II Computer

---



# Different Error Handling Policies

---

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---

A search input field with a vertical cursor on the left and a microphone icon on the right.

Google Search

I'm Feeling Lucky

# Different Error Handling Policies

---

The Google logo is centered on the page, rendered in its characteristic multi-colored font.A search input field with a vertical cursor on the left and a microphone icon on the right.

Google Search

I'm Feeling Lucky

---

---

**Versus**

---

---

# Different Error Handling Policies

---



Google Search

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**Versus**

---

```
Python 3.2 (r32:88452, Feb 20 2011, 11:12:31)
[GCC 4.2.1 (Apple Inc. build 5664)] on darwin
Type "copyright", "credits" or "license()" for more information.
```

```
>>> from math import sqrt
>>> for value in map(sqrt, [4 - x for x in range(10)]):
    print(value)
```

```
2.0
1.7320508075688772
1.4142135623730951
1.0
0.0
```

```
Traceback (most recent call last):
  File "<pyshell#3>", line 1, in <module>
    for value in map(sqrt, [4 - x for x in range(10)]):
ValueError: math domain error
```

# Exceptions

---

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A built-in mechanism in a programming language to declare and respond to exceptional conditions

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If **f** calls **g** and **g** calls **h**, exceptions can shift control from **h** to **f** without waiting for **g** to return.

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If **f** calls **g** and **g** calls **h**, exceptions can shift control from **h** to **f** without waiting for **g** to return.

However, exception handling tends to be slow.

# Assert Statements

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Demo

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`RuntimeError` -- Catch-all for troubles during interpretation

# Try Statements

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try:  
    <try suite>  
except <exception class> as <name>:  
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**Execution rule:**

# Try Statements

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The `<except suite>` is executed, with `<name>` bound to the exception

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Exception handling can prevent a program from terminating

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**Multiple try statements:** Control jumps to the except suite of the most recent try statement that handles that type of exception.



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How will the Python interpreter respond?

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    print('Never printed if x is 0')  
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def invert_safe(x):  
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# Example: Safe Iterative Improvement

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def newton_update(f):  
    """Return an update function for f using Newton's method."""  
    def update(x):  
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# Example: Safe Iterative Improvement

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Iterative improvement is a higher-order function

- The **update** argument provides better guesses
- The **done** argument indicates completion
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    """Return a guess of a zero of the function f, near guess.

    >>> from math import sin
    >>> find_root(lambda y: sin(y), 3)
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## Exception Chaining

---

The except suite of a try statement can raise another exception that adds additional information.

Demo