

























					Ha	m	nir	ng (Co	des				
O Cal	lculat	e pa	arity	bit	s as	foll	ows	5:						
$P_1 =$	xor(3	5,7,	9,11)) = 1	⊕1 €	Ð 0 €	⊕ 0 €	Ð 0 =	= 0					
$P_2 =$	xor(3	,6,7,	10,1	1)	= 0									
$P_4 =$	xor(5	,6,7,	12)		= 1									
$P_8 =$	xor(9	,10,1	1,12)	= 1									
	1	2	3	4	5	6	7	8	9	10	11	12		
	0	0	1	1	1	0	0	1	0	1	0	0		
O Wh	nen bi	its a	re re	ead	fror	n m	emo	ory,	con	nput	e ch	eck	bits:	
$C_1 =$	xor(1	,3,5,	7,9,1	1)						-				
$C_2 =$	xor(2	,3,6,	7,10	,11)										
$C_4 =$	xor(4	,5,6,	7,12)										
$C_8 =$	xor(8	,9,10),11,	12)										
CS150 Newtor	n/Pister													14.1.14

Hamming Codes														
\bigcirc C=C ₈ C ₄ C ₂ C ₁ =0000 indicates no error has occurred														
O E	xam	ples	:											
	1	2	3	4	5	6	7	8	9	10	11	12		
	0	0	1	1	1	0	0	1	0	1	0	0	no error	
	1	0	1	1	1	0	0	1	0	1	0	0	error in bit 1	
	0	0	1	1	0	0	0	1	0	1	0	0	error in bit 5	
	C 0 0 0	8 C 0 0 1	4 C 0 0 0	2 C 0 1 1	1 no er er) erro ror b ror b	or vit 1 vit 5							
CS150 Newton/Pister 14.1.15														

Hamming Codes									
○ For n data bits and k check bits, $n+k \le 2^k-1$									
O list	Grou ing o	ping f bir	of b ary 1	its for parity generation can be observed from numbers:					
	B ₁	B ₂	B ₃						
0	0	0	0						
1	1	0	0	B ₁ =1 for (1,3,5,7)					
2	0	1	0	B ₂ =1 for (2,3,6,7)					
3	1	1	0						
4	0	0	1	$B_3=1$ for (4,5,6,7)					
5	1	0	1						
6	0	1	1						
7	1	1	1						
CS150 N	Newton	Pister		14.1.16					







































